# The crystal structure and chemistry of high-aluminium phlogopite 

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#### Abstract

Crystal structure refinements were performed on five Al-rich phlogopite-1 $M$ crystals ( $1.50 \leqslant \mathrm{Al}^{3+} \leqslant 1.97$ atoms per formula unit) from skarns of the Predazzo and Monzoni Hills petrographic area (north-east Italy) with the aim of characterizing geometrical variation produced by $\mathrm{Al}^{3+}$ increase. The charge imbalance was mostly compensated for by substitutions of highly charged cations in the octahedral sheet $\left(\mathrm{Al}^{3+}\right.$ and/or $\mathrm{Fe}^{3+}$ for $\mathrm{Mg}^{2+}$ ). The refinements were carried out in the mean space group $C 2 / m$ and gave agreement values $(R)$ between 0.025 and 0.030 . For some additional crystals, only chemistry and/or unit cell parameters were determined. In all samples the tetrahedra are more regular and larger than those previously reported in the literature for phlogopite crystals and the misfit between tetrahedral and octahedral sheets, produced by the increase in the tetrahedral edges, is mostly compensated for by the tetrahedral ring angle rotation $\alpha$ ( $10.2^{\circ} \leqslant \alpha$ $\leqslant 12.5^{\circ}$ ), whereas the octahedral sheet features seem affected only by local crystal-chemical variations.


Keywords: Al-rich phlogopite, clintonite, crystal chemistry, structure refinement, skarns.

## Introduction

Trioctahedral micas are among the most abundant mafic minerals in the continental crust, where they play major roles in both igneous and metamorphic petrologic processes. However, problems associated with most aspects of their crystallography and crystal chemistry (such as stacking faults, chemical disorder, superstructures, twins and intergrowth with other phases) have prevented its wide use in petrogenetic works.

Aimed at characterizing the crystal-chemical processes occurring in micas, this study affords insight into the structural changes that take place in phlogopite crystals with high $\mathrm{Al}^{3+}$ contents $(1.50 \leqslant$ ${ }^{[4]} \mathrm{Al}^{3+}+{ }^{[6]} \mathrm{Al}^{3+} \leqslant 1.97$ atoms per formula unit).

## Experimental

The phlogopite samples examined in this work were taken from skarns of the Predazzo-Monzoni petrographic area in north-east Italy. Samples 1, 2 and 3 are from Canzoccoli, Predazzo; sample 4 is from Toal de la Foia, Monzoni Hills. Fassaite, vesuvianite, garnet, spinels, forsterite, melilite,
epidote, Mg-rich amphiboles, as well as pale green or white micas (clintonite) are the most abundant replacement minerals. Phlogopite commonly occurs with calcite, and sometimes with fassaite and is sometimes closely associated with other micas, such as clintonite. Phlogopite to chlorite alterations at the rim of the grains and along cleavages are sometimes observed (Morandi et al., 1984).

Several crystals selected, after crushing, from the sample rock and examined in the first instance by precession photographs, show that the $1 M$ polytype is ubiquitous in the regularly stacked crystals. Some crystals exhibit random stacking indicated by streaks connected with the $\mathrm{k} \neq 3 \mathrm{n}$ spots. Five crystals were selected for further investigation (samples: phlla, phl1b, phl2a, phl3a, phl4a) since they afforded the most accurate possible X-ray diffraction data. For some additional crystals, only the chemical data and the unit cell parameters have been reported.
Electron probe microanalyses (EPMA) were carried out with an ARL-SEMQ electron microprobe on the same crystal later used for structure refinement. Operating conditions were: accelerating voltage, 15 keV ; sample current, 20 nA ; beam diameter, $3 \mu \mathrm{~m}$. Within the expected bounds of
analytical error, the crystals are homogeneous and their mean compositions are reported in Table 1. Semi-quantitative scanning for all elements with $Z>$ 8 did not clearly reveal the presence of any other elements, although some may exist in undetectable trace amounts. The OH and $\mathrm{Fe}^{2+}$ were determined over a wide range of selected crystals, OH by thermogravimetric analysis (Seiko 5200 thermal analyser, heating rate $10 \% \mathrm{~min}$ in argon gas to prevent iron oxidation) and $\mathrm{Fe}^{2+}$ by the semi-micro volumetric method (Meyrowitz, 1970). Structural formulae were calculated on the basis of $(\mathrm{O}+\mathrm{OH}+\mathrm{F})$ $=12$.

Unit-cell dimensions were determined with a CAD4 (Enraf-Nonius) four-circle diffractometer with graphite monochromated Mo-K $\alpha$ X-radiation ( $\lambda$ $=0.7107 \AA$ ) by 25 intense reflections $\left(\theta \geqslant 15^{\circ}\right)$ which were used in centering each crystal. Leastsquares refinement of the setting angles gave the unit cell parameters in Table 2 and the orientation matrix used for data collection. For each crystal the intensity data for the half sphere of reciprocal space $\pm h \pm k+l$ were collected in the $\theta$ range, $1.5-35^{\circ}$. On the basis of the $\Delta \omega-\Delta \theta$ plot obtained for ten selected reflections, the $\omega$ scan mode was selected $\left(1.5^{\circ} \leqslant \omega \leqslant 5^{\circ}\right)$. Three standard reflections were measured to check the stability of the radiation and the crystal orientation. The data were empirically corrected for absorption (using $\psi$-scan data, North et al., 1968), Lorentzpolarization and background effects. Intensity data of symmetrically-equivalent reflections were averaged and the resulting discrepancy factor $\left(\mathrm{R}_{\text {sym }}\right)$ was calculated (Table 2).

The structure refinements were made by fullmatrix least-squares procedure, selecting reflections with $\mathrm{I} \geqslant 5 \sigma(\mathrm{I})$ and using a version of the program ORFLS (Busing et al., 1962). The initial atomic parameters were taken from Brigatti and Davoli (1990). During the refinements, carried out in the mean space group $C 2 / m$, fully ionized scattering factors were used for the non-tetrahedral cations, whereas both neutral and ionized scattering factors were used for tetrahedral and anion sites (Brigatti and Davoli, 1990).

## Results and discussion

## Chemistry

Taking into account the ideal phlogopite composition $\left.{ }^{\left[{ }^{[12]}\right.} \mathrm{K}^{[4]}\left(\mathrm{Si}_{3} \mathrm{Al}\right){ }^{[6]} \mathrm{Mg}_{3} \mathrm{O}_{10}(\mathrm{OH}, \mathrm{F})_{2}\right]$, the $\mathrm{Al}^{3+}$ for $\mathrm{Si}^{4+}$ tetrahedral substitution in the crystals studied is mostly compensated for by the exchange vector, $\mathrm{Si}_{-x} \mathrm{Mg}_{-y} \mathrm{Al}_{x+y}$, where the subscripts $x$ and $y$ refer to the tetrahedral substitution of $\mathrm{Al}^{3+}$ for $\mathrm{Si}^{4+}$ and the octahedral substitution of $\mathrm{Al}^{3+}$ (and/or $\mathrm{Fe}^{3+}$ ) for $\mathrm{Mg}^{2+}$ (and/or $\mathrm{Fe}^{2+}$ ), respectively. Only in some
samples are small amounts of $\mathrm{M}^{2+}\left(\mathrm{Ba}^{2+}\right.$ and/or $\mathrm{Ca}^{2+}$ ) present in the interlayer sites. The limit of $\mathrm{Al}^{3+}$ tetrahedral substitution ( $\mathrm{Al}^{3+} \leqslant 1.50$, Table 1) agrees well with the conclusions of Hewitt and Wones (1975), who stated that in synthetic phlogopites the tetrahedral $\mathrm{Al}^{3+}$ content does not exceed 1.65-1.70 atoms p.f.u. Our phlogopite samples are closely associated with clintonite $\left[{ }^{[12]} \mathrm{Ca}{ }^{[4]}\right.$. $\left.\left(\mathrm{SiAl}_{3}\right)^{[6]}\left(\mathrm{Mg}_{2} \mathrm{Al}\right) \mathrm{O}_{10}(\mathrm{OH}, \mathrm{F})_{2}\right]$. Nevertheless, the chemistry of the refined crystals interlayer sites does not seem markedly affected by $\mathrm{Ca}^{2+}$ for $\mathrm{K}^{+}$ substitution. Only in some samples, in which precession photographs reveal lack of regularity in the layer stacking, does this substitution become detectable (cf. sample ph14b, Table 1). This behaviour is probably due to clintonite/phlogopite interlayering. The chemical data obtained from a number of crystals indicate that, in this area, the existence of intermediate terms between clintonite and phlogopite is unlikely. Furthermore, synthetic clintonite crystals also showed a restricted solubility field [from ${ }^{[12]} \mathrm{Ca}^{[4]}\left(\mathrm{Si}_{1.6} \mathrm{Al}_{2.6}{ }^{[6]}\left(\mathrm{Mg}_{2.6} \mathrm{Al}_{0.6}\right) \mathrm{O}_{10^{-}}\right.$ $(\mathrm{OH}, \mathrm{F}, \mathrm{Cl})_{2}$ to ${ }^{[12]} \mathrm{Ca}^{[4]}\left(\mathrm{Si}_{1.17} \mathrm{Al}_{2.82}\right){ }^{[6]}\left(\mathrm{Mg}_{2.17} \mathrm{Al}_{0.83}\right)$ $\mathrm{O}_{10}(0 \mathrm{H}, \mathrm{F}, \mathrm{Cl})_{2} ;$ Olesch, 1975].

## Structural features

Some refinement data are reported in Table 2. The final atomic parameters are given in Table 3. The calculated bond lengths are listed in Table 4 and some structural parameters derived from structure refinement are shown in Table 5. Table 1 lists the octahedral and interlayer occupancies and the estimated $\mathrm{Al}^{3+}$ for $\mathrm{Si}^{4+}$ tetrahedral substitution (Alberti and Gottardi, 1988; Brigatti et al., 1991) which has been allocated to each site on the basis of structure determinations and the microprobe analyses. A supplementary table of observed and calculated structure factors is available from the authors on request.

The trends of the isotropic thermal factors ( $\beta_{\mathrm{eq}}$.) are similar to those previously found for trioctahedral micas (Brigatti and Davoli, 1990; Brigatti et al., 1991; Takeda and Ross, 1975). Of the cation sites, tetrahedral (T) atoms have the lowest values and the interlayer ( K ) the highest; of the anion sites, the basal tetrahedral oxygen atoms ( O 1 and O 2 ) have a generally higher $\beta_{\text {eq. }}$ than O 3 and O 4 . Nevertheless, comparison with isotropic tetrahedral thermal factors reported for phlogopites and biotites shows that, in our samples, they are generally larger. This observation reflects with an increase in $\mathrm{Si} / \mathrm{Al}$ tetrahedral disorder (Hazen and Burnham, 1973; Liebau, 1985).

At the end of the structure refinement, the electron density difference map showed maxima which can be attributed to the $\mathrm{H}^{+}$position only for samples phl2a

Table 1. Chemical data, mean atomic number of octahedral and interlayer sites and $\mathrm{Al}^{3+}$ for $\mathrm{Si}^{4+}$ tetrahedral substitution as determined by structure refinement ( $\mathbb{T})$ and microprobe analysis for Al -rich phlogopite samples from Predazzo-Monzoni Hills petrographic area

|  | Phlla* | Phl1b* | Phl2a* | Ph12b | Phl3a* | Phl3b | Phl3c | Phl4a* | Ph14b | Phl4c |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Weight (\%) |  |  |  |  |  |  |  |  |  |  |
| $\mathrm{SiO}_{2}$ | 38.88 | 37.68 | 36.78 | 37.65 | 35.27 | 37.12 | 39.78 | 36.95 | 36.57 | 37.44 |
| $\mathrm{TiO}_{2}$ | 0.41 | 0.33 | 0.12 | 0.09 | 0.17 | 0.19 | 0.22 | 0.06 | 0.07 | 0.04 |
| $\mathrm{Al}_{2} \mathrm{O}_{3}$ | 18.17 | 19.10 | 19.00 | 18.95 | 23.61 | 18.32 | 15.45 | 19.15 | 20.36 | 19.19 |
| $\mathrm{Fe}_{2} \mathrm{O}_{3}$ | 1.71 | 1.40 | 2.78 | 1.61 | 2.76 | 2.30 | 2.00 | 2.09 | 1.58 | 1.72 |
| FeO | 1.94 | 1.94 | 0.50 | 0.50 | 1.23 | 1.23 | 1.23 | 0.76 | 0.76 | 0.76 |
| MgO | 23.65 | 24.30 | 25.03 | 25.21 | 21.11 | 23.91 | 25.10 | 25.12 | 23.98 | 24.33 |
| MnO | 0.17 | 0.15 | - | 0.05 | 0.59 | 0.04 | 0.05 | 0.12 | 0.01 | 0.03 |
| CaO | 0.07 | - | - | - | 0.01 | - | - | 0.23 | 1.04 | 0.39 |
| BaO | - | - | 0.53 | 0.48 | 0.31 | 1.55 | 0.51 | 0.82 | 1.26 | 1.18 |
| $\mathrm{Na}_{2} \mathrm{O}$ | 0.26 | 0.27 | 0.14 | 0.19 | 0.12 | 0.13 | 0.16 | 0.11 | 0.22 | 0.19 |
| $\mathrm{K}_{2} \mathrm{O}$ | 10.29 | 10.29 | 10.49 | 10.66 | 10.56 | 10.31 | 10.54 | 9.99 | 9.42 | 9.77 |
| $\mathrm{H}_{2} \mathrm{O}$ | 4.15 | 4.15 | 4.15 | 4.15 | 4.10 | 4.10 | 4.10 | 4.30 | 4.30 | 4.30 |
| F | 0.24 | 0.38 | 0.47 | 0.45 | 0.16 | 0.79 | 0.84 | 0.27 | 0.41 | 0.64 |
| Cl | 0.05 | - | - | - | - | - | 0.01 | 0.03 | - | - |
| Total | 99.99 | 99.99 | 99.99 | 99.99 | 100.00 | 99.99 | 99.99 | 100.00 | 99.98 | 99.98 |
| Structural formulae for $(\mathrm{O}+\mathrm{OH}+\mathrm{F})=12$ |  |  |  |  |  |  |  |  |  |  |
| Si | 2.74 | 2.65 | 2.60 | 2.65 | 2.50 | 2.65 | 2.81 | 2.60 | 2.58 | 2.64 |
| Al | 1.26 | 1.35 | 1.40 | 1.35 | 1.50 | 1.35 | 1.19 | 1.40 | 1.42 | 1.36 |
| Total | 4.00 | 4.00 | 4.00 | 4.00 | 4.00 | 4.00 | 4.00 | 4.00 | 4.00 | 4.00 |
| Al | 0.24 | 0.24 | 0.18 | 0.22 | 0.47 | 0.18 | 0.09 | 0.20 | 0.27 | 0.23 |
| $\mathrm{Fe}^{3+}$ | 0.09 | 0.07 | 0.15 | 0.08 | 0.15 | 0.13 | 0.11 | 0.11 | 0.08 | 0.09 |
| $\mathrm{Fe}^{2+}$ | 0.12 | 0.11 | 0.03 | 0.03 | 0.07 | 0.08 | 0.07 | 0.04 | 0.05 | 0.05 |
| Mg | 2.48 | 2.55 | 2.63 | 2.65 | 2.23 | 2.54 | 2.64 | 2.64 | 2.52 | 2.55 |
| Mn | 0.01 | 0.01 | - | - | 0.04 | - | - | 0.01 | - | - |
| Ti | 0.02 | 0.02 | 0.01 | - | 0.01 | 0.01 | 0.01 | - | - |  |
| Total | 2.96 | 3.00 | 3.00 | 2.98 | 2.97 | 2.94 | 2.92 | 3.00 | 2.92 | 2.92 |
| Na | 0.04 | 0.04 | 0.02 | 0.03 | 0.02 | 0.02 | 0.02 | 0.02 | 0.03 | 0.03 |
| K | 0.93 | 0.93 | 0.95 | 0.96 | 0.95 | 0.94 | 0.95 | 0.90 | 0.85 | 0.88 |
| Ca | - | - | - | - | - | - | - | 0.02 | 0.08 | 0.03 |
| Ba | - | - | 0.01 | 0.01 | 0.01 | 0.04 | 0.01 | 0.02 | 0.04 | 0.03 |
| Total | 0.97 | 0.97 | 0.98 | 1.00 | 0.98 | 1.00 | 0.98 | 0.96 | 1.00 | 0.97 |
| OH | 1.95 | 1.95 | 1.96 | 1.95 | 1.94 | 1.95 | 1.93 | 2.02 | 2.02 | 2.02 |
| F | 0.06 | 0.09 | 0.11 | 0.10 | 0.04 | 0.18 | 0.19 | 0.06 | 0.09 | 0.14 |
| 0 | 9.99 | 9.96 | 9.93 | 9.95 | 10.02 | 9.87 | 9.88 | 9.92 | 9.89 | 9.84 |
| Total | 12.00 | 12.00 | 12.00 | 12.00 | 12.00 | 12.00 | 12.00 | 12.00 | 12.00 | 12.00 |
| Mean atomic number ( $\mathrm{e}^{-}$) |  |  |  |  |  |  |  |  |  |  |
| M1 Xref | 13.2(1) | 13.4(1) | 13.2(1) |  | 13.3(1) |  |  | 13.0(1) |  |  |
| M2 Xref | 12.9(1) | 12.9(1) | 12.9(1) |  | 13.2(1) |  |  | 12.7(1) |  |  |
| M1+M2 Xref $\ddagger$ | 39.0 | 39.2 | 39.0 |  | 39.7 |  |  | 38.4 |  |  |
| M1+M2 EPMA $\dagger$ | 39.0 | 39.1 | 38.8 |  | 39.8 |  |  | 38.4 |  |  |
| K Xref | 17.6(2) | 17.80(4) | 19.00(4) |  | 18.9(1) |  |  | 19.06(4) |  |  |
| K EPMA | 18.1 | 18.1 | 18.8 |  | 18.8 |  |  | 18.9 |  |  |
| Tetrahedral Al occupancies (\%) |  |  |  |  |  |  |  |  |  |  |
| $\mathrm{Al}^{[\mathrm{IVV}}$ | 32.7 | 35.0 | 35.5 |  | 36.2 |  |  | 36.3 |  |  |
| $\mathrm{Al}^{[\mathrm{IV]}}$ EPMA | 31.5 | 33.8 | 35.0 |  | 37.5 |  |  | 35.0 |  |  |

* crystals used in the structure refinement.

Note: Xref: X-ray refinement; EPMA: electron microprobe; $\ddagger: 2 \times[(2 \mathrm{M}(2)+\mathrm{M}(1)] ; \dagger$ : sum of octahedral cation electrons; $\ddagger$ : estimated from structure refinement following the method proposed by Alberti and Gottardi (1988) and adapted to layer silicates (Brigatti et al., 1991); K: interlayer site.

Table 2. Selected crystal data and unit cell parameters for Al-rich phlogopite crystals

| Samples | Dimensions $[\mathrm{mm}]$ | $\mathrm{N}_{\text {obs }}$ | $\begin{aligned} & \mathrm{R}_{\text {sym }} \\ & \times 100 \end{aligned}$ | $\begin{aligned} & \mathrm{R}_{\text {obs }} \\ & \times 100 \end{aligned}$ | $\begin{gathered} a \\ {\left[\begin{array}{l} \AA \end{array}\right]} \end{gathered}$ | $\begin{gathered} b \\ {[\AA]} \end{gathered}$ | $\underset{\left[\begin{array}{c} \AA \\ \hline \end{array}\right]}{ }$ | $\begin{gathered} \beta \\ {\left[{ }^{\circ}\right]} \end{gathered}$ | $\stackrel{V}{\square}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Phl1a* | . $33 \times .06 \times .03$ | 475 | 2.0 | 2.9 | 5.306(1) | $9.195(3)$ | 10.272(3) | 100.01(2) | 493.5 |
| Phl1b* | . $18 \times .12 \times .02$ | 513 | 2.4 | 2.8 | 5.309(2) | 9.180(5) | 10.291(4) | 100.00(4) | 493.9 |
| Phl2a* | . $27 \times .18 \times .05$ | 675 | 2.0 | 2.9 | $5.305(2)$ | 9.189(3) | 10.286(3) | 99.96(2) | 493.9 |
| Phl2b | . $10 \times .10 \times .02$ |  |  |  | 5.301(2) | 9.187(2) | 10.277(2) | 99.96(3) | 492.9 |
| Phl3a* | $.18 \times .13 \times .04$ | 456 | 2.0 | 3.0 | 5.299(1) | 9.179(2) | 10.279(3) | 99.90 (2) | 492.5 |
| Ph3b | . $12 \times .11 \times .03$ |  |  |  | 5.310(1) | $9.196(3)$ | 10.263(3) | 99.94(2) | 493.6 |
| Phl4a* | $.15 \times .12 \times .03$ | 464 | 2.3 | 2.5 | 5.307(2) | 9.199(1) | 10.291(2) | $99.89(2)$ | 494.9 |

Note: $\mathbf{R}_{\text {sym }}=\frac{\sum_{\text {het }} \sum_{i=1}^{N}\left|I_{n t_{i}}-I_{n k t}\right|}{\sum_{\text {nut }} \sum_{i=1}^{N} I_{h t}}$

* Crystals used for the structure refinements
and phl4a. The OH vector orientation is almost parallel to $\mathrm{c}^{*}$ and the $\mathrm{O}-\mathrm{H}$ separation is $0.92 \AA$. This behaviour bears out the observations reported by Bailey (1984) for true trioctahedral micas.

The crystal chemical features of Al-rich phlogo-pites- $1 M$ are discussed and compared with those of other trioctahedral true micas (phlogopite- $1 M$ and biotite- $1 M$ samples) and trioctahedral brittle mica


Fig. 1. $\langle\mathbf{T}-\mathrm{O}\rangle[\AA]$ mean bond lengths vs tetrahedral angle variance (TAV). Filled circles: Al-rich phlogopite samples from this study; open circles: phlogopite samples from the literature ( 1 , Hazen and Burnham, 1973; 2, Joswig, 1972; 3, Takeda and Morosin, 1975; 4, McCauley et al., 1973); open triangles: biotite samples from the literature (Brigatti et al., 1991; Brigatti and Davoli, 1990; Bigi and Brigatti, 1994); filled triangles: kinoshitalite (samples 26 and 27 from Brigatti and Poppi, 1993).
kinoshitalite reported in the literature (Fig. 1). These comparisons afford insight into the geometrical variations induced by high $\mathrm{Al}^{3+}$-contents.

Tetrahedral and interlayer sheets. In the $1 M$ polytype, the presence of just one symmetricallyindependent tetrahedron per unit cell implies no cation ordering. Tetrahedral cation occupancies, as calculated from the structure refinement by the method given in Alberti and Gottardi (1988), are in generally good agreement with those calculated by microprobe analysis (Table 1). The extent of $\mathrm{Al}^{3+}$ substitution is always lower than $40 \%$. The tetrahedral mean bond lengths ( $1.660 \leqslant<T$ $0>\leqslant 1.666 \AA$; Table 4) are greater than those observed for the $\mathrm{Mg}^{2+}$-true mica end members. The tetrahedra are quite regular $(1.0000 \leqslant \mathrm{TQE} \leqslant$ $1.0002 ; 0.03 \leqslant \mathrm{TAV} \leqslant 0.91 ;$ TQE and TAV as defined by Robinson et al., 1971) and slightly elongated ( $109.6^{\circ} \leqslant \tau \leqslant 110.3^{\circ} ; \tau=109.47^{\circ}$ for the ideal tetrahedron) as it is shown in Table 5. In our samples, the increase in tetrahedral $\mathrm{Al}^{3+}$ produces more flattened tetrahedra which become more regular (Tables 1 and 5, Fig. 1).

The most significant difference in respect of the crystals of the phlogopite-annite join so far refined is that the tetrahedral ring rotation angle ( $\alpha$ ) is always higher than $10^{\circ}$ (Fig. 2). The $\alpha$ values come near both to those reported for trioctahedral brittle mica kinoshitalite $\left[{ }^{[12]} \mathrm{Ba}^{[4]}\left(\mathrm{Si}_{2} \mathrm{Al}_{2}\right)^{[6]}\left(\mathrm{Mg}_{3}\right) \mathrm{O}_{10}(\mathrm{OH}, \mathrm{F})_{2}\right]$ (Brigatti and Poppi, 1993) and to dioctahedral muscovite-2M (Bailey, 1984); nevertheless, they are smaller than those found for clintonite- $1 M$, where the $\alpha$ values are about $23^{\circ}$. In the trioctahedral subgroup, the tetrahedral $\mathrm{Si}^{4+}$ for $\mathrm{Al}^{3+}$ substitution in our phlogopite samples is less marked than that observed for kinoshitalite, which has quite similar octahedral compositions (Brigatti and Poppi, 1993). The lateral misfit between tetrahedral and octahedral

TABLE 3. Final atomic positional and equivalent isotropic $\left[\mathrm{A}^{2}\right]$ and anisotropic $\left[\mathrm{A}^{2} \times 10^{4}\right]$ thermal factors for Al-rich phlogopite crystals

| Atom | x/a | y/b | z/c | $\mathrm{B}_{\text {eq }}$. | $\beta_{11}{ }^{*}$ | $\beta_{22}{ }^{*}$ | $\beta_{33}{ }^{*}$ | $\beta_{12}{ }^{*}$ | $\beta_{13}{ }^{*}$ | $\beta_{23}{ }^{*}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Phl1a |  |  |  |  |  |  |  |  |  |  |
| 01 | 0.0049(7) | 0 | 0.1716 (3) | 2.30(8) | 255(14) | 49(4) | 56(3) | 0 | 2(5) | 0 |
| O2 | 0.3333(4) | 0.2240(3) | 0.1724 (2) | 2.42(6) | 218(9) | 74(3) | 60(2) | -12(5) | 31(4) | -2(2) |
| 03 | $0.1308(4)$ | 0.1670 (3) | 0.3932(2) | 1.90(5) | 209(9) | 38(2) | 56(2) | -6(4) | 35(3) | 2(2) |
| 04 | 0.1328(6) | 0.5 | 0.3979(3) | 2.63(8) | 222(13) | 61(4) | 81(4) | 0 | 13(5) | 0 |
| M2 | 0 | $0.3317(2)$ | 0.5 | 1.55(3) | 140(5) | 36(1) | 48(1) | 0 | 24(2) | 0 |
| M1 | 0 | 0 | 0.5 | 1.58(5) | 121(7) | 36(2) | 56(2) | 0 | 26(3) | 0 |
| K | 0 | 0.5 | 0 | 3.06(5) | 325(8) | 92(3) | 63(2) | 0 | 31(3) | 0 |
| T | 0.0767(2) | 0.1668 (1) | 0.2284(1) | 1.66 (2) | 155(3) | 40(1) | 48(1) | 0 (2) | 22(1) | -1(1) |
| Phllb |  |  |  |  |  |  |  |  |  |  |
| O1 | 0.0029(6) | 0 | 0.1721 (3) | 2.48(8) | 211(11) | 76(4) | 61(3) | 0 | 9(5) | 0 |
| 02 | 0.3340(4) | 0.2228(3) | 0.1716 (2) | 2.43(5) | 191(7) | 86(3) | 58(2) | -21(4) | 28(3) | -7(2) |
| 03 | 0.1305 (3) | 0.1669(2) | 0.3928(2) | 2.02(5) | 156(7) | 72(3) | 48(2) | -4(4) | 19(3) | -1(2) |
| 04 | $0.1326(5)$ | 0.5 | $0.3985(3)$ | 2.01(7) | 133(10) | 70(4) | 55(3) | 0 | 20(4) | 0 |
| M2 | 0 | 0.3316(2) | 0.5 | 1.69(3) | 106(4) | 55(2) | 52(1) | 0 | 20(2) | 0 |
| M1 | 0 | 0 | 0.5 | 1.93(4) | 119(6) | 63(2) | 59(2) | , | 22(3) | 0 |
| K | 0 | 0.5 | 0 | 3.36(5) | 284(6) | 115(3) | 76(2) | 0 | 28(3) | 0 |
| T | 0.0761(1) | 0.1667 (1) | 0.2287(1) | 1.74(2) | 115(2) | 61(1) | 47(1) | -1(2) | 17(1) | 1(1) |
| Phl2a |  |  |  |  |  |  |  |  |  |  |
| O1 | 0.0013(5) | 0 | 0.1718(3) | 1.80(6) | 188(9) | 47(3) | 40(2) | 0 | 1(4) | 0 |
| O2 | 0.3358(3) | 0.2214(2) | 0.1721 (2) | 1.73(4) | 166(6) | 57(2) | 37(2) | -16(3) | 21(2) | -5(2) |
| O3 | 0.1313(3) | 0.1666(2) | 0.3927(2) | 1.30(3) | 119(5) | 40(2) | 32(2) | 0 (3) | 15(2) | 1(1) |
| O4 | 0.1318(4) | 0.5 | 0.3993(2) | 1.20(5) | 115(8) | 33(2) | 31(2) | 0 | $9(3)$ | 0 |
| M2 | 0 | 0.3308(1) | 0.5 | 1.11 (2) | 99(3) | 27(1) | 33(1) | 0 | 13(1) | 0 |
| M1 | 0 | 0 | 0.5 | 1.26 (3) | 110(5) | 34(2) | 35(1) | 0 | 12(2) | 0 |
| K | 0 | 0.5 | 0 | 2.52(3) | 251(5) | 80(2) | 51(1) | 0 | 19(2) | 0 |
| T | 0.0766(1) | 0.1666(1) | 0.2284(1) | 1.07(1) | 96(2) | 30(1) | 29(1) | -2(1) | 10(1) | 0 (1) |
| Phl3a |  |  |  |  |  |  |  |  |  |  |
| O1 | -0.0064(7) | 0 | $0.1738(4)$ | $2.2(1)$ | 230 (15) | 52(5) | 52(4) | 0 | -5(6) | 0 |
| O2 | 0.3395(5) | 0.2182(3) | $0.1732(3)$ | 2.19(7) | 214(10) | 67(4) | 47(3) | -21(5) | 10(4) | -5(3) |
| 03 | $0.1322(5)$ | $0.1673(3)$ | $0.3937(2)$ | $1.83(6)$ | 205(10) | 47(3) | 41(2) | 4(5) | 16(4) | 1(3) |
| 04 | $0.1306(7)$ | 0.5 | $0.3997(4)$ | 1.9 (1) | 161(15) | 58(5) | 42(4) | 0 | -10(6) | 0 |
| M2 | 0 | 0.3309(2) | 0.5 | 1.48 (3) | 126(5) | 40(2) | 40(1) | 0 | 1(2) | 0 |
| M1 | 0 | 0 | 0.5 | 1.53(5) | 129(8) | 39(3) | 43(2) | 0 | $2(3)$ | 0 |
| K | 0 | 0.5 | 0 | 2.65(5) | 263(7) | 83(3) | 53(2) | 0 | 7(3) | 0 |
| T | 0.0765(2) | 0.1667(1) | 0.2285(1) | 1.48(2) | 137(3) | 40(1) | $37(1)$ | -1(2) | 2(1) | -2(1) |
| Phl4a |  |  |  |  |  |  |  |  |  |  |
| O1 | 0.0031(6) | 0 | 0.1719(3) | 2.14(8) | 205(12) | 41(3) | 65(4) | 0 | 5(5) | 0 |
| O 2 | 0.3340(4) | 0.2225(3) | 0.1717 (2) | 2.20 (5) | 195(8) | 68(3) | 52(2) | -20(4) | 13(3) | -6(2) |
| 03 | 0.1295(3) | 0.1670(2) | 0.3920(2) | 1.57 (5) | 106(6) | 37(2) | 56(2) | 2(4) | 15(3) | 4(2) |
| O4 | $0.1319(5)$ | 0.5 | 0.3981(3) | 1.55 (7) | 114(11) | 34(3) | 54(3) | ( | $9(5)$ | 0 |
| M2 | 0 | 0.3310(2) | 0.5 | 1.42 (3) | 115(4) | 25(1) | 53(1) | 0 | 12(2) | 0 |
| M1 | 0 |  | 0.5 | 1.62 (5) | 124(7) | 30(2) | $60(2)$ | 0 | 9 (3) | 0 |
| K | 0 | 0.5 | 0 | 2.74(4) | 257(6) | 78(2) | 65(2) | 0 | 12(2) | 0 |
| T | 0.0764(1) | 0.1667(1) | 0.2287(1) | 1.39(2) | 115(3) | 25(1) | $50(1)$ | 0 (2) | 8(1) | -1(1) |

[^0]Table 4. Selected bond lengths $[\AA]$ for Al-rich phlogopite crystals

|  | Phlla | Phllb | Phl2a | Phl3a | Phl4a |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{T}-\mathrm{O} 1$ [ $\left.\mathrm{A}_{\mathrm{\circ}}\right]$ | 1.661(2) | 1.659(2) | 1.662(1) | 1.663(2) | 1.663(2) |
| $\mathrm{T}-\mathrm{O} 2[\mathrm{~A}]$ | 1.653(2) | 1.662(2) | 1.660(2) | 1.662(3) | 1.659(2) |
| T-O2' [ A ] | 1.658(3) | $1.663(2)$ | 1.664(2) | $1.665(3)$ | 1.667(2) |
| $\mathrm{T}-\mathrm{O} 3$ [ $\AA$ ] | 1.667(2) | 1.663(2) | $1.665(2)$ | 1.673(3) | 1.656(2) |
| $<\mathrm{T}-\mathrm{O}\rangle[\mathrm{A}]$ | 1.660 | 1.662 | 1.663 | 1.666 | 1.661 |
| M1-O3 ( $\times 4$ ) [ ${ }_{\text {A }}^{\circ} \mathrm{C}$ | 2.076(2) | 2.076 (2) | 2.077(2) | 2.075(3) | 2.081(2) |
| M1-O4 ( $\times 2$ ) [A] | 2.046(3) | 2.047(3) | 2.046(2) | 2.050(3) | 2.053(3) |
| <M1-O> [ A ] | 2.066 | 2.066 | 2.067 | 2.067 | 2.072 |
| $\mathrm{M} 2-\mathrm{O} 3(\times 2)[\AA]$ | 2.060(3) | 2.061(3) | 2.061(2) | 2.050(3) | 2.061(2) |
| M2-O3' $(\times 2)[\AA]$ | 2.073(2) | 2.077(2) | 2.073(2) | 2.064(2) | 2.086(2) |
| M2-O4 ( $\times 2$ ) [A] | 2.061(2) | 2.057(2) | 2.057(2) | 2.048(3) | 2.063(2) |
| $<\mathrm{M} 2-\mathrm{O}>$ [ A$]$ | 2.065 | 2.065 | 2.064 | 2.054 | 2.070 |
| $\mathrm{K}^{*}-\mathrm{O} 1(\times 2)\left[{ }_{\text {¢ }}(\mathrm{A}]\right.$ | 3.409(3) | 3.424(3) | 3.426(3) | 3.470(4) | 3.419(3) |
| $\mathrm{K}^{*} \mathrm{O} 1^{\prime}(\times 2)[\mathrm{A}]$ | 2.940 (3) | 2.936 (3) | 2.927(3) | 2.903(4) | 2.939(3) |
| $\mathrm{K}^{*}-\mathrm{O} 2(\times 4)[\mathrm{A}]$ | 3.408(3) | 3.413(3) | 3.430(2) | 3.464(3) | 3.421 (2) |
| $\mathrm{K}^{*}-\mathrm{O} 2^{\prime}(\times 4)[\mathrm{A}]$ | 2.951(3) | 2.935 (3) | 2.927 (2) | $2.903(3)$ | 2.936 (2) |
| $<\mathrm{K}^{*}-\mathrm{O}>_{\text {inner }}$ [ A$]$ | 2.947 | 2.935 | 2.927 | 2.903 | 2.937 |
| $<\mathrm{K}^{*} \mathrm{O}>_{\text {outer }}[\mathrm{A}]$ | 3.408 | 3.417 | 3.429 | 3.466 | 3.420 |
| Delta $<\mathrm{K}^{*}-\mathrm{O}>$ | 0.461 | 0.482 | 0.502 | 0.563 | 0.483 |

*K indicate interlayer cation whatever.
sheets in kinoshitalite, which could be produced by the tetrahedral edges increasing, is counterbalanced


Fig. 2. $\langle\mathrm{T}-\mathrm{O}\rangle$ basal $[\AA]$ mean bond lengths $v s$ the tetrahedral ring rotation angle $\alpha\left[{ }^{\circ}\right]$. Samples and symbols as in Fig. 1.
generally by single polyhedron and tetrahedral ring distortion but in our samples only by tetrahedral ring distortion.

Octahedral sheet. The octahedral sites follow the general trend of phlogopite, which is homoctahedral of type I (Weiss et al., 1992), the M1 and M2 mean bond lengths being quite similar within the bounds of experimental error (Table 4). Furthermore, M1 is larger than M2 for sample phl3a, which indicates that the highly-charged cations can be allocated to the M2 site $\left(\mathrm{M} 1=\mathrm{Mg}_{0.70} \mathrm{Al}_{0.16} \mathrm{Fe}_{0.07}^{2+} \mathrm{Mn}_{0.04} \square 0.03 ; \mathrm{M} 2=\right.$ $\mathrm{Mg}_{0.76} \mathrm{Al}_{0.16} \mathrm{Fe}_{0.07}^{3+} \mathrm{Ti}_{0.01}$. The cation distribution was hypothesized by structure refinement and using cation radius values calculated by Weiss et al., 1985). <M-O> mean bond lengths are quite similar to those reported in literature for phlogopite and kinoshitalite samples with comparable octahedral chemical composition and thus do not seem markedly affected by tetrahedral sheet dimensions and by tetrahedral ring distortion. The $\psi$ values are all greater than the ideal octahedral value of $54.73^{\circ}$. Both M1 and M2 octahedra show the same flattening, as in phlogopite, with the one exception of sample phl3a, where M1 is more flattened than M2 (Table 5). Figure 3 ( $a$ and $b$ ) shows the relationships between the ratio of shared and unshared octahedral edges

Table 5. Selected tetrahedral, octahedral and interlayer parameters derived from the structure refinement for Al-rich phlogopite crystals

|  | Phlla | Phl1b | Phl2a | Phl3a | Phl4a |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Tetrahedral parameters |  |  |  |  |  |
| $\alpha\left[{ }^{\circ}\right]$ | 10.2 | 10.7 | 11.1 | 12.5 | 10.7 |
| $\triangle \mathrm{z}[\mathrm{A}]$ | 0.008 | 0.005 | 0.003 | 0.006 | 0.002 |
| $\tau\left[{ }^{\circ}\right]$ | 110.1(1) | 110.3(1) | 110.1(1) | 109.6(1) | 110.3(1) |
| TAV [ $\left.{ }^{\circ}\right]$ | 0.48 | 0.89 | 0.51 | 0.03 | 0.91 |
| TQE | 1.0002 | 1.0002 | 1.0001 | 1.0000 | 1.0002 |
| Volume $_{\text {T }}\left[\AA^{3}\right]$ | 2.346 | 2.355 | 2.359 | 2.371 | 2.352 |
| Octahedral parameters |  |  |  |  |  |
| $\psi_{M 1}\left[{ }^{\circ}\right]$ | 58.99 | 58.92 | 59.00 | 59.28 | 58.75 |
| $\psi_{M 2}\left[{ }^{\circ}\right]$ | 58.97 | 58.89 | 58.93 | 59.06 | 58.74 |
| $e_{u M 1}$ | 3.0663 | 3.0647 | 3.0680 | 3.0763 | 3.0673 |
| $e_{u M 2}$ | 3.0637 | 3.0620 | 3.0610 | 3.0517 | 3.0647 |
| $e_{s M 1}$ | 2.7690 | 2.7727 | 2.7697 | 2.7597 | 2.7843 |
| $e_{S M 2}$ | 2.7680 | 2.7717 | 2.7672 | 2.7505 | 2.7832 |
| $\mathrm{OQE}_{M 1}$ | 1.0114 | 1.0110 | 1.0116 | 1.0131 | 1.0103 |
| $\mathrm{OQE}_{M 2}$ | 1.0113 | 1.0109 | 1.0114 | 1.0121 | 1.0104 |
| $\mathrm{OAV}_{M 1}\left[{ }^{\circ}\right]$ | 37.22 | 35.95 | 37.87 | 42.55 | 33.67 |
| $\mathrm{OAV}_{M 2}\left[{ }^{\circ}\right]$ | 37.10 | 35.95 | 37.42 | 39.55 | 34.12 |
| $V^{\text {Volume }}{ }_{M 1}\left[\AA^{3}\right]$ | 11.561 | 11.576 | 11.571 | 11.542 | 11.668 |
| $V^{\text {Volume }}{ }_{M 2}\left[\AA^{3}\right]$ | 11.536 | 11.556 | 11.514 | 11.351 | 11.644 |
| Sheet thickness [ $\AA$ ] |  |  |  |  |  |
| tetrahedral | 2.253 | 2.257 | 2.259 | 2.250 | 2.254 |
| octahedral | 2.129 | 2.134 | 2.130 | 2.112 | 2.149 |
| interlayer separation | 3.480 | 3.487 | 3.484 | 3.515 | 3.481 |

$\alpha$ (tetrahedral rotation angle) $=\sum_{i=1}^{6} \alpha_{i} / 6$ where $\alpha_{i}=1120^{\circ}-\phi_{i} / 2$ and where $\phi_{\mathrm{i}}$ is the angle between basal edges of neighbouring tetrahedra articulated in the ring;
$\Delta \mathrm{Z}=\left[\mathrm{Z}_{\left(\mathrm{O}_{\text {baxi }}\right)_{\text {max }}}-\mathrm{Z}_{\left(\mathrm{O}_{\text {basa }}\right)_{\text {min }}}\right][\operatorname{csin} \beta]$;
$\tau$ (tetrahedral flattening angle) $=\sum_{i=1}^{3}\left(\mathrm{O}_{\text {apical }}-\mathrm{T}-\mathrm{O}_{\text {basal }}\right)_{\mathrm{i}} / 3$;
TAV (tetrahedral angle variance) $=\sum_{i=1}^{6}\left(\theta_{i}-109.47\right)^{2} / 5$ (Robinson et al., 1971);
TQE (tetrahedral quadratic elongation) $=\sum_{i=1}^{4}\left(l_{i} / l_{0}\right)^{2} / 4$ where $l_{0}$ is the centre to vertex distance for an undistorted tetrahedron whose volume is equal to that of the distorted tetrahedron with bond length $l_{i}$ (Robinson et al., 1971);
$\psi$ (octahedral flattening angle) $=\cos ^{-1}$ [octahedral thickness/( $\left.2<\mathrm{M}-\mathrm{O}\right\rangle$ )] (Donnay et al., 1964);
$e_{w}, e_{s}$ : mean lengths of unshared and shared edges, respectively (Toraya, 1981);
OQE (octahedral quadratic elongation) $=\sum_{i=1}^{6}\left(l_{i} / l_{0}\right)^{2} / 6$ where $l_{o}$ is the centre to vertex distance for an undistorted octahedron whose volume is equal to that of the distorted octahedron with bond length $l_{i}$ (Robinson et al., 1971);
OAV (octahedral angle variance) $=\sum_{i=1}^{12}\left(\theta_{i}-90^{\circ}\right)^{2} / 11$ (Robinson et al., 1971)
( $\mathrm{e}_{\mathrm{u}} / \mathrm{e}_{\mathrm{s}}$ ) and the octahedral flattening $\psi$ angle for both M1 and M2 sites. The Al-rich phlogopite samples vary widely in the case of the M1 site: between biotites and phlogopites, samples phl4a and phllb are
grouped with biotites, samples phl1a and phl 2 a are intermediate, whereas sample phl3a is grouped with phlogopite. As regards the M2 site, our samples lie in an intermediate field between biotite and phlogopite.


Fig. 3. Variation shown by the ratio of unshared and shared octahedral edges ( $e_{\mathrm{u}} / \mathrm{e}_{\mathrm{s}}$ ) as a function of the octahedral flattening angle ( $\psi\left[^{\circ}\right]$ ) for M1 (a) and for M2 (b) sites. Samples and symbols as in Fig. 1.

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[^0]:    $* \exp \left[-\left(h^{2} \beta_{11}+\ldots+2 h k \beta_{12}+\ldots\right)\right]$

