# VARIATIONS IN COMPOSITION AND PROPERTIES OF THE CALCIFEROUS AMPHIBOLES 

A. N. Winchell, University of Wisconsin, Madison, Wisconsin.


#### Abstract

By plotting the position of about two hundred analyses of common hornblende analyses on a (partial) triangle with $\mathrm{Ca}_{2}\left(\mathrm{Mg}, \mathrm{Fe}_{5} \mathrm{Si}_{8} \mathrm{O}_{22}(\mathrm{OH})_{2}, \mathrm{Ca}_{2}(\mathrm{Mg}, \mathrm{Fe})_{3}\left(\mathrm{Al}, \mathrm{Fe}_{4}\right)_{4} \mathrm{Si}_{6} \mathrm{O}_{22}(\mathrm{OH})_{2}\right.$, $\mathrm{NaCa}_{2}\left(\mathrm{Mg}, \mathrm{Fe}_{5}\right)_{5} \mathrm{AlSi}_{7} \mathrm{O}_{22}(\mathrm{OH})_{2}$, and $\mathrm{NaCa}_{2}(\mathrm{Mg}, \mathrm{Fe})_{4}\left(\mathrm{Al}, \mathrm{Fe}_{3}\right)_{3} \mathrm{Si}_{6} \mathrm{O}_{22}(\mathrm{OH})_{2}$ as its end-members, Hallimond has shown very clearly that many hornblendes have a composition which can be expressed in terms of these four formulas. By using this (partial) triangle as the base of a (partial) triangular prism it is possible to represent (in a three dimensional figure) all the most important variables in the composition of hornblende, and this makes it possible to show the relations between variations in composition and in physical properties as done in Fig. 9. Since several (less important) variables are disregarded in developing this diagram it must be considered as only an approximation. The formulas used in this figure are:


$\mathrm{Ca}_{2} \mathrm{Mg}_{5} \mathrm{Si}_{8} \mathrm{O}_{22}(\mathrm{OH})_{2}$
$\mathrm{NaCa}_{2} \mathrm{Mg}_{5} \mathrm{AlSi}_{7} \mathrm{O}_{22}(\mathrm{OH})_{2}$
$\mathrm{NaCa}_{2} \mathrm{Mg}_{4} \mathrm{Al}_{3} \mathrm{Si}_{6} \mathrm{O}_{22}(\mathrm{OH})_{2}$
$\mathrm{Ca}_{2} \mathrm{Mg}_{3} \mathrm{Al}_{4} \mathrm{Si}_{6} \mathrm{O}_{22}(\mathrm{OH})_{2}$

$$
\begin{aligned}
& \mathrm{Ca}_{2} \mathrm{Fe}_{5} \mathrm{Si}_{8} \mathrm{O}_{22}(\mathrm{OH})_{2} \\
& \mathrm{NaCa}_{2} \mathrm{CO}_{5} \mathrm{AlSi}_{7} \mathrm{O}_{22}(\mathrm{OH})_{2} \\
& \mathrm{NaCa}_{2} \mathrm{Fe}^{\prime \prime}{ }_{4} \mathrm{Fe}^{\prime \prime \prime} \mathrm{Al}_{2} \mathrm{Si}_{6} \mathrm{O}_{22}(\mathrm{OH})_{2} \\
& \mathrm{Ca}_{2} \mathrm{Fe}^{\prime \prime}{ }_{3} \mathrm{Fe}^{\prime \prime}{ }_{2} \mathrm{Al}_{2} \mathrm{Si}_{6} \mathrm{O}_{22}(\mathrm{OH})_{2}
\end{aligned}
$$

The position of any hornblende analysis in this (partial) triangular prism can be obtained by calculating the number of each kind of atom for $2400(\mathrm{O}+\mathrm{OH}+\mathrm{F})$, dividing each side of the triangle into 200 parts, and then using Si atoms -600 as one coordinate, $\mathrm{Ca}+\mathrm{Na}+\mathrm{K}-200$ as a second coordinate and $200(\mathrm{Mg}+\mathrm{Al})$ divided by $\mathrm{Mg}+\mathrm{Al}^{\prime}+\mathrm{Fe}^{\prime \prime}$ $+\mathrm{Fe}^{\prime \prime \prime}+\mathrm{Ti}+\mathrm{Mn}$ as the third (vertical) coordinate ( $\mathrm{Al}^{\prime}$ being equal to total Al atoms minus Al atoms necessary to make $\mathrm{Si}+\mathrm{Al}$ equal to 800).

In a very similar way the composition of certain oxyhornblendes is shown in Fig. 10 and the relations between composition and optical properties are shown in Fig. 12, using the following formulas for the ferriferous end-members:

$$
\begin{array}{ll}
\mathrm{Ca}_{2} \mathrm{Fe}^{\prime \prime}{ }_{3} \mathrm{Fe}^{\prime \prime \prime}{ }_{2 \mathrm{Si}}^{8} 8 \\
\mathrm{O}_{24} & \mathrm{Ca}_{2} \mathrm{Fe}^{\prime \prime} \mathrm{Fe}^{\prime \prime \prime}{ }_{4} \mathrm{Al}_{2} \mathrm{Si}_{6} \mathrm{O}_{24} \\
\mathrm{NaCa}_{2} \mathrm{Fe}^{\prime \prime}{ }_{3} \mathrm{Fe}^{\prime \prime \prime}{ }_{2} \mathrm{AlSi}_{7} \mathrm{O}_{24} & \mathrm{NaCa}_{2} \mathrm{Fe}^{\prime \prime}{ }_{2} \mathrm{Fe}^{\prime \prime \prime}{ }_{3} \mathrm{Al}_{2} \mathrm{Si}_{6} \mathrm{O}_{24}
\end{array}
$$

This diagram is based on very incomplete data and should be used with caution.
For a long time the writer has emphasized the fact that many minerals vary considerably in composition and he has published diagrams showing the relations between variations in composition and corresponding variations in physical properties for most of the common minerals. In this work hornblende has been exceptionally difficult to deal with, first, because its composition was not fully understood, and second, because it varies in composition in so many ways that no ordinary diagram can be used to represent these variations.

Under these circumstances Hallimond's excellent study of the calciferous amphiboles ${ }^{1}$ is of great assistance. It should be clearly understood that Hallimond's study does not include all the possible variations in composition in amphibole nor even all those for which there is now good

[^0]evidence of continuous variation. But it does include all the commonest variables and therefore includes most of the "common hornblendes" as well as ordinary tremolite, actinolite, ferrotremolite, pargasite, and hastingsite.

Hallimond includes oxyhornblendes ("basaltic hornblendes") in his study. However, the optic properties of oxyhornblende differ so much


FIg. 1. Relations of some hornblende formulas.
from those of common hornblende that it is necessary to deal with them separately for the purposes of the present study. Moreover, oxyhornblendes differ also in composition from common hornblendes. It is desirable to begin with common hornblendes.

## Part 1. Common Hornblendes

It is well known that Warren's work ${ }^{2}$ established the correctness of Schaller's formula ${ }^{3}$ for tremolite and also gave us the contents of the unit

[^1]cell, as well as the presence of a vacant space which can be occupied by an atom of Na , thus permitting an Al atom to replace a Si atom, the total valencies being satisfied by the simultaneous introduction of one Na atom into the vacant space. Hallimond's study makes use of these facts and also shows very clearly that there is continuous variation from the tremolite formula in two different ways (disregarding the variation from Mg to Fe ); these two ways are:

Substitution

1. $\mathrm{Ca}_{2} \mathrm{Mg}_{5} \mathrm{Si}_{8} \mathrm{O}_{22}(\mathrm{OH})_{2}$ to $\mathrm{Na}_{2} \mathrm{Ca}_{2} \mathrm{Mg}_{5} \mathrm{Al}_{2} \mathrm{Si}_{6} \mathrm{O}_{22}(\mathrm{OH})_{2} \quad \mathrm{Na}_{2} \mathrm{Al}_{2}$ for $\mathrm{Si}_{2}$
2. $\mathrm{Ca}_{2} \mathrm{Mg}_{5} \mathrm{Si}_{8} \mathrm{O}_{22}(\mathrm{OH})_{2}$ to $\mathrm{Ca}_{2} \mathrm{Mg}_{3} \mathrm{Al}_{4} \mathrm{Si}_{6} \mathrm{O}_{22}(\mathrm{OH})_{2} \quad \mathrm{Al}_{4}$ for $\mathrm{Mg}_{2} \mathrm{Si}_{2}$

Thus three formulas are obtained all possible proportions of which may be represented by a triangle, the corners of which are used to represent these formulas. However, reliable analyses of amphibole show that the substitution of $\mathrm{Na}_{2} \mathrm{Al}_{2}$ for $\mathrm{Si}_{2}$ extends only half as far as indicated, perhaps due to lack of more vacant spaces. Accordingly, $\mathrm{Na}_{2} \mathrm{Ca}_{2} \mathrm{Mg}_{5} \mathrm{Al}_{2} \mathrm{Si}_{6} \mathrm{O}_{22}$ $(\mathrm{OH})_{2}$ is not an amphibole formula; it is used merely for conveneince to complete the triangle, as shown in Fig. 1. The chief end-member formulas for non-ferrous calciferous amphiboles are therefore the following four:

1. $\mathrm{Ca}_{2} \mathrm{Mg}_{6} \mathrm{Si}_{8} \mathrm{O}_{22}(\mathrm{OH})_{2}$
2. $\mathrm{Ca}_{2} \mathrm{Mg}_{3} \mathrm{Al}_{4} \mathrm{Si}_{6} \mathrm{O}_{22}(\mathrm{OH})_{2}$
3. $\mathrm{NaCa}_{2} \mathrm{Mg}_{5} \mathrm{AlSi}_{7} \mathrm{O}_{22}(\mathrm{OH})_{2}$
4. $\mathrm{NaCa}_{2} \mathrm{Mg}_{4} \mathrm{Al}_{3} \mathrm{Si}_{6} \mathrm{O}_{22}(\mathrm{OH})_{2}$

Hallimond notes that the second of these formulas is often called the Tschermak molecule; the writer would suggest that it be called tschermakite and the corresponding ferrous formula may then be called ferrotschermakite.

Hallimond has plotted nearly two hundred of the best analyses of calciferous amphiboles on such a (partial) triangle (always assuming that Mg stands for Mg and also $\mathrm{Mn}, \mathrm{Fe}^{\prime \prime}, \mathrm{Fe}^{\prime \prime \prime}$ and Ti ). He uses the number of Si atoms $\left\{\right.$ for $\left.2400\left(\mathrm{O}+\mathrm{OH}_{2} \mathrm{~F}\right)\right\}$ as one coordinate and the number of atoms in the "vacant space" as the other coordinate. This is not quite the same as using the formulas, because Na atoms can occupy such spaces as a result of other kinds of replacements, notably 2 Na for Ca . The writer has attempted to plot analyses more strictly on the basis of the formulas, excluding all analyses containing more than about 10 per cent of other end-members (including soda-tremolite, glaucophane and all kinds of oxyhornblende) and also all analyses not accompanied by data on the physical properties of the samples concerned. The results are shown in Fig. 2.



Fig. 3. Composition of selected hornblendes.

Of course physical properties vary with variations in composition but they vary more rapidly with variations in the amount of replacement of Mg by Fe than with the variations shown in Fig. 2. Accordingly it is almost impossible to discover the relations between variations in composition and variations in physical properties without considering the $\mathrm{Mg}-\mathrm{Fe}$ variation. Since this variation is entirely independent of the variations shown in Fig. 2 and may affect all the end-members of that figure, it can be shown by adding a third coordinate at right angles to the others. This changes the (partial) triangle into (part of) a triangular column, as shown in Fig. 3.

To determine the position of any analysis on the vertical coordinate it is necessary to make certain assumptions. This coordinate may be considered to represent $Y$ of Machatschki's groups ${ }^{4}: \mathbf{X}=(\mathrm{Ca}, \mathrm{Na}, \mathrm{K}), \mathrm{Y}=$ $(\mathrm{Mg}, \mathrm{Mn}, \mathrm{Fe}, \mathrm{Al}, \mathrm{Ti})$ and $\mathrm{Z}=(\mathrm{Si}, \mathrm{Al}) . \mathrm{It}$ is impossible to represent more than one kind of variation along the vertical coordinate. It is thought that the relation between $200\left(\mathrm{Mg}+\mathrm{Al}^{\prime}\right)$ and $\mathrm{Mg}+\mathrm{Al}^{\prime}+\mathrm{Fe}^{\prime \prime}+\mathrm{Mn}+\mathrm{Fe}^{\prime \prime \prime}+\mathrm{Ti}$ will be the most useful. To find $\mathrm{Al}^{\prime}$ it is only necessary to subtract from the total Al atoms the number necessary to be added to Si to make $\mathrm{Si}+\mathrm{Al}$ $=800$ (on the basis of $2400(\mathrm{O}+\mathrm{OH}, \mathrm{F})$ atoms.) It is assumed that all Mn and $\mathrm{Fe}^{\prime \prime}$ and $\mathrm{Fe}^{\prime \prime \prime}$ and Ti atoms belong to the Y group and play the role of Mg atoms. It is now rather generally accepted that AlAl may proxy for MgSi ; it seems very probable that $\mathrm{Fe}^{\prime \prime \prime}$ and Ti do not proxy for Si, but replace Mg only; to keep the total valencies balanced this may be explained as a replacement of MgSi by $\mathrm{Fe}^{\prime \prime \prime} \mathrm{Al}$ and of MgSiSi by TiAlAl. It is a fact that practically all analyses of hornblende contain enough Al atoms to permit this assumption. Accordingly, the vertical coordinate of Fig. 3 is obtained from the relation between $\mathrm{Mg}+\mathrm{Al}^{\prime}$ and $\mathrm{Fe}^{\prime \prime}+\mathrm{Fe}^{\prime \prime \prime}$ $+\mathrm{Mn}+\mathrm{Ti}$.

Even after thus obtaining the position of more than a hundred analyses of calciferous amphiboles in this (partial) triangular column, it is not a simple matter to derive nor to show the corresponding variations in physical properties. And the variations in physical characters can not correspond with the expressed variations in composition in any simple way because there are many unexpressed variations in composition which must have their effects upon the physical properties. For example, no attention is paid to the replacement of $\mathrm{Fe}^{\prime \prime}$ by $\mathrm{Fe}^{\prime \prime \prime}$ or $\mathrm{Fe}^{\prime \prime}$ by Mn or $\mathrm{Fe}^{\prime \prime}$ by Ti , or Na by K , or OH by F . In spite of all these limitations the writer believes that an expression of the best approximation of

[^2]average conditions, which can be derived, will be useful, if only as something to be improved. After constructing about fifty diagrams showing the variations of physical properties along selected lines and planes in


Fig. 4. The tremolite-ferrotremolite series.
this (partial) triangular column, and studying their mutual relations, certain conclusions have been reached.

First, it seems possible, now, to simplify and modify the diagram for the tremolite-ferrotremolite series first published ${ }^{5}$ in 1931 to give the results shown in Fig. 4. This diagram gives the properties of two end-

[^3]members of the system. The writer is much indebted to Hallimond for an important correction ${ }^{6}$ of the published analysis of "pargasite" from Amity, N. Y., which vitiates entirely the former diagram ${ }^{7}$ for the series: $\mathrm{Ca}_{2} \mathrm{Mg}_{5} \mathrm{Si}_{3} \mathrm{O}_{22}(\mathrm{OH})_{2}-\mathrm{NaCa}_{2} \mathrm{Mg}_{5} \mathrm{AlSi}_{7} \mathrm{O}_{22}(\mathrm{OH})_{2}$. Estimates of the physical properties of this and other end-members of the system follow, derived (in part by extrapolation) from data on analyzed samples inside the (partial) triangular column:

Table 1. Approximate Properties of End-Members

| End-member | Sign | 2 V | $\mathrm{~N}_{\mathbf{g}}$ | $\mathrm{N}_{\mathrm{g}}-\mathrm{N}_{\mathrm{p}}$ | $\mathrm{Z} \wedge c$ | G |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathrm{Ca}_{2} \mathrm{Mg}_{5} \mathrm{Si}_{8} \mathrm{O}_{22}(\mathrm{OH})_{2}$ | $(-)$ | $88^{\circ}$ | 1.628 | .03 | $18^{\circ}$ | 2.98 |
| $\mathrm{NaCa}_{2} \mathrm{Mg}_{5} \mathrm{AlSi}_{7} \mathrm{O}_{22}(\mathrm{OH})_{2}$ | $(+)$ | $50^{\circ}$ | 1.63 | .02 | $25^{\circ}$ | 3.06 |
| $\mathrm{NaCa}_{2} \mathrm{Mg}_{4} \mathrm{Al}_{3} \mathrm{Si}_{6} \mathrm{O}_{22}(\mathrm{OH})_{2}$ | $(+)$ | $85^{\circ}$ | 1.64 | .02 | $28^{\circ}$ | 3.15 |
| $\mathrm{Ca}_{2} \mathrm{Mg}_{3} \mathrm{Al}_{4} \mathrm{Si}_{6} \mathrm{O}_{22}(\mathrm{OH})_{2}$ | $(-)$ | $80^{\circ}$ | 1.657 | .02 | $20^{\circ}$ | 3.13 |
| $\mathrm{Ca}_{2} \mathrm{Fe}_{5} \mathrm{Si}_{8} \mathrm{O}_{22}(\mathrm{OH})_{2}$ | $(-)$ | $75^{\circ}$ | 1.735 | .025 | $12^{\circ}$ | 3.40 |
| $\mathrm{NaCa}_{2} \mathrm{Fe}_{5} \mathrm{AlSi}_{7} \mathrm{O}_{22}(\mathrm{OH})_{2}$ | $(-)$ | $20^{\circ}$ | 1.73 | .02 | $15^{\circ}$ | 3.42 |
| $\mathrm{NaCa}_{2} \mathrm{Fe}^{\prime \prime}{ }_{4} \mathrm{Fe}^{\prime \prime \prime} \mathrm{Al}_{2} \mathrm{Si}_{6} \mathrm{O}_{22}(\mathrm{OH})_{2}$ | $(-)$ | $35^{\circ}$ | 1.74 | .02 | $18^{\circ}$ | 3.45 |
| $\mathrm{Ca}_{2} \mathrm{Fe}^{\prime \prime}{ }_{3} \mathrm{Fe}^{\prime \prime \prime}{ }_{2} \mathrm{Al}_{2} \mathrm{Si}_{6} \mathrm{O}_{22}(\mathrm{OH})_{2}$ | $(-)$ | $70^{\circ}$ | 1.75 | .03 | $18^{\circ}$ | 3.42 |

From these data it is possible to construct diagrams showing the variations in properties on the front faces of the (partial) triangular column (Fig. 5), on the rear face of the column (Fig. 6), on the base of the column (Fig. 7), and on the top of the column (Fig. 8). Finally, it is possible to show (in clinographic projection) the variations in properties in all parts of the column, as done in Fig. 9.

The last two formulas in Table 1 show the replacement of the five atoms of $\mathrm{Mg}(+\mathrm{Al})$ by $\mathrm{Fe}^{\prime \prime \prime}$ as well as $\mathrm{Fe}^{\prime \prime}$. It should be understood that in locating any analysis in the (partial) triangular column Mn is included with $\mathrm{Fe}^{\prime \prime}$ and Ti is included with $\mathrm{Fe}^{\prime \prime \prime}$. When Ti comes into the problem, the last formula may be written: $\mathrm{Ca}_{2} \mathrm{Fe}^{\prime \prime}{ }_{4} \mathrm{TiAl}_{2} \mathrm{Si}_{6} \mathrm{O}_{22}(\mathrm{OH})_{2}$.

It is important to remember that this (partial) triangular column will not correspond with the facts in every case; indeed it will only rarely correspond with all the data-it is only an estimate of the average condition. But it is believed that it will give an approximately correct idea of the composition of a sample of amphibole belonging to this system. The amphiboles belonging to this system include tremolite, actinolite, ferrotremolite, pargasite, hastingsite and "common hornblende," but do not include cummingtonite, grunerite, soda-tremolite, oxyhornblende, glauco-

[^4]
Fig. 5. Properties on the front faces of the (partial) triangular prism (hornblende).


Fig. 6. Properties on the rear face of the (partial) triangular prism (hornblende).


Fig. 7. Properties on the bottom of the (partial) triangular prism (hornblende).
phane, riebeckite, arfvedsonite and intermediate types sometimes called "soda-amphiboles."

For many years the writer has prepared diagrams showing the relations between physical properties and composition on the basis of molecular (or atomic) percentages. It was very surprising to him to find in a recent publication ${ }^{8}$ the statement: "Optic properties in general are more


FIg. 8. Properties on the top of the (partial) triangular prism (hornblende).
nearly a function of density (weight percentage) than of number of ions (molecular percentage)." As long ago as 1878 Dufet ${ }^{9}$ proved that the contrary statement is true for orthorhombic crystals. In 1894 Lavenir ${ }^{10}$ confirmed Dufet's results and extended them. ${ }^{11}$ In 1925 Porter ${ }^{12}$ proved that the index of refraction is a rectilinear function of the composition expressed in molecular percentage for rays vibrating along the axis of symmetry in monoclinic minerals, and, in general, is more simply related to molecular percentage composition than to the weight percentage composition in all crystals. But the relationship is not necessarily nor usually exactly rectilinear in triclinic crystals nor in monoclinic crystals except along the $b$ axis.

Table 2 gives the number of atoms (or ions) of each constituent in 104 analyses of calciferous amphiboles on the basis of 2400 atoms of oxygen
${ }^{8}$ Folinsbee, R. E., Am. Mineral., 26, 498 (1941).
${ }^{9}$ Bull. Soc. Fr. Min., 1, 58 (1878).
${ }^{10}$ Bull. Soc. Fr. Min., 17, 153 (1894).
${ }^{11}$ Among minerals there seem to be some as yet unexplained exceptions to this rule, as illustrated in the triphylite-lithiophilite series and in the new data for the orthorhombic pyroxene, enstenite.
${ }^{12}$ Porter, Mary W., Proc. Roy. Soc., 109, 78 (1925).

Table 2. Atomic Ratios of Calciferous Amphiboles for ( $\mathrm{O}, \mathrm{OH}, \mathrm{F}$ ) $=2400$

| No. | $\left\|\begin{array}{c} \mathrm{Si} \\ -600 \end{array}\right\|$ | Al | $\mathrm{Fe}^{\prime \prime}$ | $\mathrm{Fe}^{\prime \prime}$ | Mn | Ti | Mg | Ca | Na | K | H | F |  |  |  | 䔍 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 195 | 23 | 11 | 50 | 3 | 1 | 466 | 189 | 15 | 5 | 77 |  | 9 | 176 | 2 | 1 |
| 2 | 192 | 51 | 24 | 135 | 4 |  | 329 | 178 | 9 | 4 | 96 |  | -9 | 139 | 4 | 1 |
| 3 | 192 | 20 | 15 | 48 | 2 | 2 | 468 | 190 | 21 | 9 | 63 | 7 | 20 | 176 | 5 | 1 |
| 4 | 190 | 22 |  | 7 | 1 |  | 485 | 188 | 6 | 1 | 197 | 7 | -5 | 197 | 9 | 1 |
| 5 | 190 | 21 | 2 | 2 | 1 |  | 509 | 190 | 18 | 9 | 106 | 33 | 17 | 198 | 13 | 1 |
| 6 | 187 | 29 |  | 6 |  | 2 | 490 | 193 | 13 | 4 | 142 | 16 | 10 | 197 | 12 | 1 |
| 7 | 186 | 17 |  | 22 |  | 8 | 458 | 190 | 18 | 5 | 209 |  | 13 | 188 | 10 | 1 |
| 8 | 186 | 49 | 31 | 217 | 7 |  | 248 | 176 | 31 | , | 61 | 14 | 14 | 105 | 15 | 1 |
| 9 | 186 | 20 | 8 | 64 | 3 |  | 442 | 181 | 5 | 5 | 168 | 2 | -9 | 171 | 16 | 1 |
| 10 | 184 | 20 | 2 | 61 | 3 |  | 450 | 185 | 13 | 3 | 182 |  | 1 | 175 |  | 2 |
| 11 | 182 | 20 | 2 | 2 |  | 1 | 485 | 205 | 11 | 3 | 202 | 5 | 19 | 198 | 18 | 1 |
| 12 | 179 | 21 | 6 | 20 | 6 |  | 477 | 186 | 15 | 4 | 161 | 41 | 5 | 188 | 20 | 1 |
| 13 | 178 | 2 |  | 17 |  |  | 483 | 200 | 10 | 3 | 136 |  | 13 | 193 |  | 3 |
| 14 | 177 | 57 |  | 88 |  |  | 398 | 158 | 68 |  | 164 |  | 26 | 166 | 19 | 1 |
| 15 | 176 | 37 | 14 | 43 |  |  | 463 | 186 | 25 | 14 | 56 | 58 | 25 | 179 | 22 | 1 |
| 16 | 174 | 45 | 12 | 139 |  | 3 | 325 | 190 | 15 | 2 | 194 |  |  | 138 | 25 | 1 |
| 17 | 173 | 21 | 8 | 27 |  |  | 474 | 181 | 33 | 12 | 183 | 27 | 26 | 186 |  | 4 |
| 18 | 173 | 24 | 0 | 114 | 2 | 2 | 378 | 193 | 39 |  | 214 |  | 32 | 152 | 26 | 1 |
| 19 | 169 | 75 | 5 | 22 |  | , | 450 | 194 | 35 | 12 | 80 | 11 | 41 | 188 |  | 5 |
| 20 | 168 | 34 | 32 | 211 |  |  | 257 | 192 | 16 |  | 194 |  | 8 | 103 | 29 | 1 |
| 21 | 167 | 34 | 23 | 50 | 2 | 2 | 446 | 184 | 32 | 11 | 36 | 111 | 27 | 171 | 30 | 1 |
| 22 | 167 | 22 |  | 27 | 2 | 1 | 484 | 192 | 2 |  | 123 |  | -6 | 188 |  | 6 |
| 23 | 165 | 42 | 27 | 52 |  | 1 | 422 | 180 | 22 | 5 | 148 | 34 |  | 169 | 32 | 1 |
| 24 | 161 | 49 | 16 | 48 |  |  | 426 | 199 | 15 |  | 200 |  | 14 | 174 | 35 | 1 |
| 25 | 159 | 36 | 9 | 17 | 2 |  | 466 | 169 | 65 | 19 | 200 | 37 | 53 | 189 | 34 | 1 |
| 26 | 159 | 60 | 5 | 86 | 2 | 2 | 394 | 188 |  |  | 221 |  | -12 | 162 | 36 | 1 |
| 27 | 154 | 62 | 13 | 51 | Ni 3 |  | 401 | 196 | 31 | 14 | 212 |  | 41 | 172 | 42 | 1 |
| 28 | 151 | 106 | 7 | 56 | 2 | 5 | 429 | 203 | 13 | , | 42 |  | 20 | 175 | 38 | 1 |
| 29 | 151 | 40 | 28 | 185 |  |  | 280 | 171 | 26 | 10 | 254 |  | 7 | 114 | 33 | 1 |
| 30 | 147 | 45 | 33 | 80 | 9 | 3 | 410 | 182 | 21 | , | 136 | 41 | 12 | 153 | 44 | 1 |
| 31 | 146 | 38 | 2 | 21 |  | 1 | 486 | 187 | 8 | 2 | 148 |  | 2 | 190 |  | 7 |
| 32 | 142 | 124 | 23 | 68 | 3 | 4 | 349 | 210 | 12 | 10 | 91 |  | 32 | 162 | 48 | 1 |
| 33 | 141 | 68 | 31 | 176 |  |  | 284 | 195 | 10 |  | 217 |  | 5 | 117 | 50 | 1 |
| 34 | 140 | 83 | 33 | 147 | 2 | 4 | 325 | 192 | 33 | 12 | 98 |  | 37 | 130 | 49 | 1 |
| 35 | 139 | 160 | 2 | 194 | 4 | 11 | 279 | 203 | 13 | 38 | 17 |  | 54 | 128 |  | 8 |
| 36 | 137 | 21 | 32 | 103 | 2 | 8 | 391 | 187 | 32 |  | 243 | 19 | 19 | 146 |  | 9 |
| 37 | 124 | 118 | 37 | 151 |  | 3 | 304 | 183 | 9 | 5 | 140 |  | -3 | 129 | 57 | 1 |
| 38 | 116 | 101 | 72 | 95 | 2 | 13 | 312 | 178 | 34 | 13 | 134 | 12 | 25 | 129 | 59 | 1 |
| 39 | 114 | 67 | 66 | 103 | 3 | 1 | 380 | 206 | 31 | 1 | 119 |  | 38 | 137 |  | 10 |
| 40 | 109 | 155 | 17 | 107 | 14 | 3 | 358 | 198 | 14 | 5 | 66 |  | 17 | 150 |  | 11 |
| 41 | 107 | 133 | 39 | 100 | 2 | 12 | 337 | 184 | 29 | 10 | 61 | 64 | 23 | 142 | 62 | 1 |
| 42 | 104 | 98 | 31 | 61 |  | 8 | 429 | 200 | 22 | 3 | 160 |  | 25 | 163 | 64 | 1 |
| 43 | 104 | 110 | 60 | 96 | 2 | 16 | 322 | 187 | 28 | 12 | 157 |  | 27 | 132 | 65 | 1 |
| 44 | 102 | 124 | 27 | 116 | . | 12 | 343 | 175 | 53 | 3 | 166 |  | 31 | 141 | 66 | 1 |
| 45 | 102 | 115 | 16 | 152 |  | 10 | 289 | 199 | 83 |  | 198 |  | 82 | 126 |  | 12 |
| 46 | 101 | 118 | 40 | 104 |  | 5 | 338 | 204 | 28 |  | 180 |  | 32 | 142 | 67 | 1 |
| 47 | 95 | 125 | 22 | 125 |  |  | 352 | 197 | 27 | 7 | 203 |  | 31 | 143 | 69 | 1 |
| 48 | 89 | 212 | 9 | 156 |  | 21 | 207 | 208 | 28 |  | 129 |  | 36 | 125 |  | 13 |
| 49 | 80 | 166 | 54 | 113 | 4 | 19 | 292 | 175 | 39 | 21 | 64 | 37 | 35 | 128 | 75 | 1 |
| 50 | 79 | 183 | , | 20 |  |  | 433 | 189 | 69 | 22 | 67 |  | 80 | 189 | 79 | 1 |
| 51 | 78 | 176 | 22 | 121 |  | 11 | 289 | 183 | 79 | 10 | 176 |  | 72 | 138 | 77 | 1 |
| 52 | 77 | 146 | 11 | 40 | 2 | 4 | 457 | 189 | 79 | 15 | 100 | 31 | 83 | 179 |  | 14 |
| 53 | 76 | 178 | 8 | 18 |  |  | 433 | 183 | 73 | 25 | 93 | 81 | 81 | 190 | 80 | 1 |

Table 2-Continued

| No. | $\begin{gathered} \mathrm{Si} \\ -600 \end{gathered}$ | Al | $\mathrm{Fe}^{\prime \prime \prime}$ | $\mathrm{Fe}^{\prime \prime}$ | Mn | Ti | Mg | Ca | Na | K | H | F | $\begin{aligned} & 4 \\ & \text { to } \\ & \text { ze } \\ & +1 \\ & +1 \end{aligned}$ |  |  | U U U U ¢ ¢ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 54 | 73 | 138 | 50 | 101 | 1 | 1 | 379 | 211 | 35 | 35 | 25 | 57 | 81 | 143 |  | 15 |
| 55 | 68 | 100 | 141 | 150 | 1 | 13 | 271 | 213 | 68 | 11 |  |  | 92 | 94 | 84 | 1 |
| 56 | 68 | 163 | 28 | 294 | 17 | 22 | 128 | 184 | 30 | 13 | 176 |  | 27 | 61 |  | 16 |
| 57 | 63 | 165 | 66 | 84 | 2 | 19 | 317 | 175 | 34 | 17 | 168 |  | 26 | 134 | 88 | 1 |
| 58 | 60 | 154 | 17 | 228 | 1 | 23 | 166 | 172 | 47 | 16 | 229 |  | 35 | 80 | 93 | 1 |
| 59 | 59 | 141 | 46 | 94 | 3 | 16 | 378 | 206 | 39 | 40 | 32 | 66 | 85 | 140 |  | 17 |
| 60 | 59 | 227 | 21 | 221 | 2 | 15 | 195 | 193 | 31 | 23 | 88 |  | 47 | 104 | 95 | 1 |
| 61 | 58 | 203 | 13 | 27 | 1 | 5 | 430 | 197 | 74 | 15 | 94 | 11 | 86 | 182 | 98 | 1 |
| 62 | 57 | 203 | 43 | 187 | 2 | 21 | 202 | 230 | 33 | 21 | 52 |  | 84 | 102 | 101 | 1 |
| 63 | 56 | 162 | 10 | 20 | 1 | 9 | 463 | 193 | 67 | 18 | 43 | 138 | 78 | 185 | 99 | 1 |
| 64 | 53 | 227 | 4 | 12 | 1 |  | 430 | 190 | 78 | 10 | 127 | 12 | 78 | 194 | 103 | 1 |
| 65 | 53 | 198 | 53 | 112 | 2 | 20 | 304 | 177 | 60 | 16 | 79 |  | 53 | 131 | 102 | 1 |
| 66 | 51 | 196 | 52 | 93 | 4 | 10 | 324 | 185 | 72 | 37 | 73 | 23 | 94 | 140 | 106 | 1 |
| 67 | 51 | 194 | 34 | 98 | 1 | 17 | 348 | 189 | 44 | 16 | 116 |  | 49 | 145 |  | 18 |
| 68 | 50 | 233 | 3 | 9 | 1 |  | 426 | 192 | 75 | 9 | 128 | 14 | 76 | 195 | 107 | 1 |
| 69 | 49 | 183 | 56 | 109 | 2 | 41 | 269 | 186 | 36 | 21 | 93 | 41 | 42 | 118 | 108 | 1 |
| 70 | 48 | 174 | 45 | 177 | 2 | 6 | 213 | 177 | 18 | 26 | 336 |  | 21 | 101 |  | 19 |
| 71 | 46 | 181 | 27 | 153 |  | 15 | 295 | 191 | 55 |  | 203 |  | 46 | 125 | 110 | 1 |
| 72 | 45 | 204 | 3 | 9 | 1 | 7 | 437 | 202 | 76 | 32 | 68 | 125 | 110 | 192 |  | 20 |
| 73 | 44 | 201 | 54 | 143 |  | 10 | 277 | 186 | 57 | 23 | 163 |  | 66 | 122 | 113 | 1 |
| 74 | 44 | 189 | 36 | 160 |  | 18 | 272 | 181 | 41 | 13 | 200 |  | 35 | 117 | 115 | 1 |
| 75 | 42 | 207 | 78 | 158 | 5 | 9 | 221 | 190 | 49 | 20 | 122 |  | 59 | 104 |  | 21 |
| 76 | 42 | 258 | 25 | 132 | 4 | 4 | 259 | 181 | 60 | 12 | 145 |  | 53 | 137 | 116 | 1 |
| 77 | 41 | 209 | 31 | 182 | 3 | 17 | 254 | 189 | 73 | 19 | 62 | 39 | 81 | 113 | 109 | 1 |
| 78 | 40 | 217 | 33 | 185 | 2 | 33 | 209 | 210 | 47 | 23 | 70 |  | 80 | 102 | 118 | 1 |
| 79 | 40 | 219 | 116 | 98 |  |  | 279 | 207 | 27 |  |  |  | 34 | 122 |  | 22 |
| 80 | 38 | 178 | 108 | 215 |  | 12 | 167 | 178 | 83 | 26 | 96 | 19 | 87 | 71 | 119 | 1 |
| 81 | 37 | 238 | 19 | 59 |  | 14 | 328 | 175 | 88 | 21 | 192 |  | 84 | 163 | 121 | 1 |
| 82 | 36 | 186 | 70 | 103 |  | 28 | 289 | 188 | 79 |  | 136 |  | 67 | 121 |  | 23 |
| 83 | 36 | 214 | 3 | 72 |  | 8 | 409 | 197 | 38 | 24 | 49 | 105 | 59 | 169 | 125 | 1 |
| 84 | 36 | 208 | 51 | 162 |  | 5 | 251 | 176 | 47 | 23 | 210 |  | 46 | 115 | 122 | 1 |
| 85 | 36 | 194 | 41 | 187 |  | 13 | 254 | 181 | 40 | 10 | 204 |  | 31 | 109 | 120 | 1 |
| 86 | 31 | 228 | 33 | 133 |  | 2 | 309 | 186 | 53 | 14 | 156 |  | 53 | 137 | 130 | 1 |
| 87 | 30 | 209 | 57 | 137 |  | 15 | 276 | 197 | 50 | 23 | 132 |  | 70 | 120 | 132 | 1 |
| 88 | 29 | 206 | 37 | 111 | 2 | 31 | 305 | 185 | 31 | 19 | 136 | 39 | 35 | 131 | 135 | 1 |
| 89 | 28 | 267 | 18 | 74 | 1 | 2 | 295 | 189 | 58 | 22 | 224 |  | 69 | 161 |  | 24 |
| 90 | 27 | 209 | 82 | 372 |  |  | 34 | 197 | 39 | 34 | 138 |  | 70 | 27 | 137 | 1 |
| 91 | 19 | 252 | 29 | 128 | 2 | 31 | 259 | 201 | 67 | 27 | 77 | 17 | 95 | 127 |  | 25 |
| 92 | 19 | 233 | 65 | 96 | 2 | 11 | 317 | 185 | 19. | 15 | 150 |  | 19 | 138 | 141 | 1 |
| 93 | 17 | 263 | 16 | 38 |  | 5 | 385 | 213 | 57 | 27 | 106 | 10 | 97 | 177 | 152 | 1 |
| 94 | 17 | 200 | 44 | 107 | 1 | 26 | 323 | 186 | 58 | 12 | 197 |  | 56 | 131 | 146 | 1 |
| 95 | 14 | 211 | 44 | 149 |  | 28 | 252 | 184 | 53 | 11 | 230 |  | 48 | 111 | 148 | 1 |
| 96 | 13 | 294 | 29 | 112 | 1 | 8 | 259 | 172 | 47 | 16 | 198 |  | 35 | 142 | 150 | 1 |
| 97 | 10 | 237 | 51 | 353 | 17 | 39 | 53 | 170 | 57 | 27 | 65 |  | 54 | 36 | 153 | 1 |
| 98 | 8 | 207 | 92 | 341 | 13 | 11 | 33 | 169 | 64 | 39 | 217 |  | 72 | 19 | 154 | 1 |
| 99 | - 7 | 235 | 84 | 138 | 13 | 4 | 263 | 198 | 50 | 46 | 78 | 3 | 94 | 112 | 156 | 1 |
| 100 | 7 | 191 | 187 | 3 | 1 | 2 | 296 | 192 | 29 | 2 | 224 |  | 23 | 121 |  | 26 |
| 101 | 4 | 253 | 21 | 42 | 1 | 5 | 399 | 203 | 65 | 27 | 33 | 137 | 95 | 174 | 158 | 1 |
| 102 | -2 | 251 | 53 | 72 | 3 | 20 | 330 | 203 | 64 | 35 | 60 | 35 | 102 | 142 |  | 27 |
| 103 | $-7$ | 241 | 78 | 29 | 1 | 57 | 334 | 187 | 54 | 46 | 43 |  | 87 | 139 |  | 28 |
| 104 | $-10$ | 239 | 56 | 86 | 2 | 24 | 304 | 196 | 67 | 6 | 203 |  | 69 | 133 |  | 29 |

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(plus hydroxyl plus fluorine). For convenience the number of Si atoms is given after subtracting 600 , since it then gives directly one coordinate needed to locate the analysis in Figs. 2 and 3. Another coordinate is given in the column headed $\mathrm{Ca}+\mathrm{Na}+\mathrm{K}-200$. And the third coordinate is in the column headed $200\left(\mathrm{Mg}+\mathrm{Al}^{\prime}\right)$ divided by $\mathrm{Mg}+\mathrm{Al}^{\prime}+\mathrm{Fe}$, in which Fe stands for $\mathrm{Fe}^{\prime \prime}, \mathrm{Fe}^{\prime \prime \prime}, \mathrm{Mn}$ and Ti.

Table 3 gives the physical properties of these 104 analyzed samples of calciferous amphiboles, so far as they have been determined. More measurements of these properties on analyzed samples are much needed, especially in the case of hornblende rich in iron.


Fig. 9. Physical properties of calciferous hornblendes.

Table 3. Physical Properties of Calciferous Amphiboles

| No. | Sign | 2V | $\mathrm{N}_{\mathrm{g}}$ | $\mathrm{N}_{\mathrm{m}}$ | $\mathrm{N}_{\mathrm{p}}$ | $\mathrm{N}_{\mathrm{g}}-\mathrm{N}_{\mathrm{p}}$ | $\mathrm{Z} \wedge$ c | G |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | - |  | 1.634 | 1.626 | 1.616 | 0.018 | $18^{\circ}$ | 3.044 |
| 2 | - |  | 1.653 | 1.642 | 1.628 | 0.025 | $15^{\circ}$ | 3.131 |
| 3 | - |  | 1.639 | 1.626 | 1.611 | 0.028 | $17^{\circ}$ | 3.051 |
| 4 | - | $79^{\circ} 38^{\prime}$ | 1.6272 | 1.6155 | 1.6000 | 0.0272 | $15^{\circ} 25^{\prime}$ | 2.98 |
| 5 | - | $88^{\circ} 23^{\prime}$ | 1.6246 | 1.6132 | 1.5992 | 0.0254 | $20^{\circ} 1^{\prime}$ | 2.997 |
| 6 | - | $86^{\circ} 29^{\prime}$ | 1.6347 | 1.6192 | 1.6022 | 0.0325 | $16^{\circ} 38^{\prime}$ | 2.980 |
| 7 | - |  | 1.632 |  | 1.609 | 9.023 |  |  |
| 8 | - |  | 1.659 | 1.649 | 1.631 | 0.028 | $24-27^{\circ}$ | 3.126 |
| 9 | - | $81^{\circ} 38^{\prime}$ | 1.6450 | 1.6330 | 1.6173 | 0.0277 | $14^{\circ} 59^{\prime}$ | 3.047 |
| 10 | - | $79^{\circ} 49^{\prime}$ | 1.6410 | 1.6297 | 1.6139 | 0.0271 | $16^{\circ} 31^{\prime}$ | 3.047 |
| 11 | - | $82^{\circ}$ | 1.6307 | 1.6183 | 1.6024 | 0.0283 | $15^{\circ} 30^{\prime}$ |  |
| 12 | - | $87^{\circ} 56^{\prime}$ | 1.6299 | 1.6171 | 1.6036 | 0.0263 | $18^{\circ} 18^{\prime}$ | 3.025 |
| 13 | - | $80^{\circ}$ | 1.631 | 1.620 | 1.608 | 0.023 | $17^{\circ}$ | 2.989 |
| 14 |  |  | 1.6529 |  | 1.6267 | 0.0262 | $14^{\circ} 34^{\prime}$ | 3.116 |
| 15 | $+$ |  | 1.634 | 1.621 | 1.613 | 0.021 | $17^{\circ}$ | 3.056 |
| 16 | - |  | 1.650 | 1.641 | 1.627 | 0.023 | $20^{\circ}$ | 3.11 |
| 17 | - | $84^{\circ} 5^{\prime}$ | 1.6319 | 1.6210 | 1.6065 | 0.0254 | $16^{\circ} 54^{\prime}$ | 3.031 |
| 18 | - |  | 1.641 | 1.630 | 1.617 | 0.024 | $18^{\circ}$ | 3.09 |
| 19 |  | $83^{\circ}$ |  |  |  | 0.0241 | $16^{\circ}$ | 2.996 |
| 20 |  |  | 1.663 |  | 1.642 | 0.021 | $15^{\circ}$ | 3.211 |
| 21 | - |  | 1.637 | 1.628 | 1.618 | 0.019 | $19^{\circ}$ | 3.064 |
| 22 | - | $78^{\circ} 30^{\prime}$ | 1.632 | 1.620 | 1.607 | 0.025 | $17^{\circ} 30^{\prime}$ |  |
| 23 | - | $81^{\circ} 30^{\prime}$ | 1.0412 | 1.6304 | 1.6162 | 0.0250 | $14^{\circ} 27^{\prime}$ | 3.092 |
| 24 |  |  | 1.638 |  | 1.615 | 0.023 | $18^{\circ}$ |  |
| 25 | - | $86^{\circ} 14^{\prime}$ | 1.6244 | 1.6134 | 1.6017 | 0.0227 | $19^{\circ} 31^{\prime}$ | 3.03-3.04 |
| 26 | - | Lg. | 1.638 | 1.629 | 1.618 | 0.020 | $17^{\circ}$ | 3.06 |
| 27 | - |  | 1.650 |  | 1.628 | 0.022 |  |  |
| 28 | - |  | 1.642 | 1.634 | 1.625 | 0.017 | $12^{\circ}$ | 3.054 |
| 29 | - |  | 1.664 | 1.652 | 1.637 | 0.027 | $20^{\circ}$ |  |
| 30 | - | $84^{\circ} 8^{\prime}$ | 1.6503 | 1.6382 | 1.6237 | 0.0266 |  | 3.111 |
| 31 | - | $81^{\circ} 30^{\prime}$ | 1.634 | 1.624 | 1.612 | 0.022 | $18^{\circ}$ |  |
| 32 | - | Lg. | 1.642 | 1.631 | 1.618 | 0.024 | $16^{\circ}$ | 3.147 |
| 33 | - |  | 1.659 |  | 1.638 | 0.021 | $17^{\circ}$ | 3.188 |
| 34 | - |  | 1.647 | 1.645 | 1.631 | 0.016 | $18^{\circ}$ | 3.171 |
| 35 | + |  | 1.672 | 1.650 | 1.649 | 0.023 |  | 3.18 |
| 36 | - | $76^{\circ}$ | 1.652 | 1.642 | 1.626 | 0.026 | $16^{\circ}$ | 3.11 |
| 37 | - | $83^{\circ} 57^{\prime}$ | 1.6678 | 1.6551 | 1.6416 | 0.0262 | $15^{\circ} 30^{\prime}$ |  |
| 38 | - | $78^{\circ}$ | 1.664 | 1.655 | 1.643 | 0.021 | $19^{\circ}$ | 3.159 |
| 39 | - | $70^{\circ}$ | 1.654 | 1.646 | 1.627 | 0.027 | $17^{\circ}$ | 3.12 |
| 40 | - | $88^{\circ} 30^{\prime}$ | 1.661 |  | 1.636 | 0.025 | $16^{\circ}$ | 3.12 |
| 41 | - | $75^{\circ}$ | 1.670 | 1.662 | 1.651 | 0.019 | $19^{\circ}$ | 3.160 |
| 42 | - |  | 1.654 |  | 1.633 | 0.021 |  | 3.110 |
| 43 | - | $76^{\circ}$ | 1.671 | 1.663 | 1.653 | 0.018 | $20^{\circ}$ | 3.159 |
| 44 | - | $81^{\circ}$ | 1.652 | 1.642 | 1.629 | 0.023 | $25^{\circ}$ |  |
| 45 | - | $77^{\circ}$ | 1.666 | 1.657 | 1.643 | 0.023 | $15^{\circ}$ | 3.15 |
| 46 | - |  | 1.661 |  | 1.641 | 0.020 |  | 3.18 |
| 47 | - |  | 1.658 |  | 1.640 | 0.018 | $17^{\circ}$ | 3.182 |
| 48 | - | $79^{\circ}$ | 1.675 | 1.665 | 1.650 | 0.025 | $19^{\circ}$ | 3.18 |
| 49 | - |  | 1.680 | 1.675 | 1.652 | 0.028 | $14^{\circ} 30^{\prime}$ | 3.188 |
| 50 | $+$ | $60^{\circ} 29^{\prime}$ | 1.6351 | 1.6180 | 1.6131 | 0.0220 | $26^{\circ}$ | 3.069 |
| 51 |  | $78-82^{\circ}$ | 1.658 |  | 1.638 | 0.020 | $14^{\circ} 30^{\prime}$ |  |
| 52 | $+$ | $60^{\circ}$ | 1.645 | 1.630 | 1.622 | 0.023 | $27^{\circ}$ |  |

Table 3-Continued

| No. | Sign | 2 V | $\mathrm{N}_{\mathrm{g}}$ | $\mathrm{N}_{\mathrm{m}}$ | $\mathrm{N}_{\mathrm{p}}$ | $\mathrm{N}_{\mathrm{g}}-\mathrm{N}_{\mathrm{p}}$ | $Z \wedge c$ | G |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 53 | $+$ | $58^{\circ} 51^{\prime}$ | 1.6353 | 1.6205 | 1.6158 | 0.0195 | $26^{\circ} 57^{\prime}$ | 3.095 |
| 54 | $+$ | $74^{\circ}$ | 1.654 | 1.644 | 1.638 | 0.016 | $21^{\circ}$ | 3.20 |
| 55 | - | $75^{\circ} 44^{\prime}$ | 1.6798 | 1.6729 | 1.6598 | 0.020 | $14^{\circ} 40^{\prime}$ | 3.21 |
| 56 | - | $59^{\circ}$ | 1.701 | 1.692 | 1.673 | 0.028 | $15^{\circ}+$ |  |
| 57 | - | $77^{\circ}$ | 1.669 | 1.660 | 1.651 | 0.018 | $18^{\circ}$ | 3.164 |
| 58 | - | $77^{\circ}$ | 1.700 | 1.687 | 1.666 | 0.034 | $22^{\circ}$ |  |
| 59 | $+$ | $76^{\circ}$ | 1.654 | 1.643 | 1.636 | 0.018 | $22^{\circ}$ | 3.20 |
| 60 | - | $75^{\circ}$ |  | 1.675 |  | 0.016 | $18^{\circ}$ | 3.27 |
| 61 | $+$ | $66^{\circ}$ | 1.6429 | 1.6284 | 1.6218 | 0.0211 | $24^{\circ}$ |  |
| 62 | - | $70^{\circ}$ | 1.684 | 1.676 | 1.660 | 0.024 | $17^{\circ}$ | 3.254 |
| 63 | - | $83^{\circ}$ | 1.638 | 1.631 | 1.622 | 1.016 | $20-22^{\circ}$ | 3.090 |
| 64 | + | $70^{\circ}$ | 1.6430 | 1.6291 | 1.6221 | 1.0209 | $21^{\circ}$ |  |
| 65 | - | Lg. | 1.683 | 1.673 | 1.658 | 0.025 | $13^{\circ} 30^{\prime}$ |  |
| 66 | - | $88^{\circ}$ | 1.6665 | 1.6589 | 1.6511 | 0.0154 | $23^{\circ}$ |  |
| 67 | - | $81^{\circ}$ | 1.666 | 1.652 | 1.633 | 0.033 | $15^{\circ}$ | 3.15 |
| 68 | + | $64^{\circ}$ | 1.6416 | 1.6265 | 1.6206 | 0.0210 | $22^{\circ}$ |  |
| 69 | - | $71^{\circ}$ | 1.673 | 1.665 | 1.654 | 0.019 | $17^{\circ}$ | 3.176 |
| 70 | - | $77^{\circ} 6^{\prime}$ | 1.673 | 1.659 | 1.651 | 0.022 | $25^{\circ}$ | 3.15 |
| 71 | - |  | 1.574 |  | 1.653 | $0.021$ |  |  |
| 72 | + | $52^{\circ} 9^{\prime}$ | 1.6332 | 1.6180 | 1.6142 | 0.0190 | $27^{\circ} 30^{\prime}$ | $3.11$ |
| 73 | - |  | 1.678 |  | 1.658 | 0.020 | $24^{\circ}$ | $3.268$ |
| 74 | - |  | 1.676 |  | 1.657 | 0.019 | $18^{\circ}$ | $3.26$ |
| 75 | - |  | 1.681 |  | 1.661 | 0.020 |  | 3.292 |
| 76 | - | $86^{\circ}$ | 1.674 | 1.663 | 1.651 | 0.023 | $16^{\circ} 15^{\prime}$ | 3.171 |
| 77 | - | $81^{\circ} 42^{\prime}$ | 1.6789 | 1.6701 | 1.6583 | 0.0206 | $23^{\circ} 48^{\prime}$ | 3.285 |
| 78 | - | $66^{\circ} 30^{\prime}$ | 1.679 | 1.674 | 1.661 | 0.018 | $13^{\circ} 30^{\prime}$ | 3.278 |
| 79 | - | $80^{\circ} 4^{\prime}$ | 1.6843 | 1.6753 | 1.6648 | 0.0195 | $16^{\circ}$ |  |
| 80 | - | $38^{\circ}$ | 1.7000 | 1.6980 | 1.6804 | 0.0198 | $20^{\circ}$ |  |
| 81 | - | $85^{\circ}$ | 1.659 | 1.647 | 1.636 | 0.023 | $21^{\circ} 22^{\prime}$ | 3.13 |
| 82 | - | $86^{\circ}$ | 1.673 | 1.662 | 1.647 | 0.026 | $20^{\circ}$ | $3.18$ |
| 83 | $+$ | $63^{\circ} 1^{\prime}$ | 1.6519 | 1.6380 | 1.6329 | 0.0190 | $26^{\circ} 15^{\prime}$ | $3.186$ |
| 84 | - |  | 1.677 |  | 1.658 | 0.019 |  | $3.284$ |
| 85 | - | $65^{\circ} 38^{\prime}$ | 1.681 | 1.673 | 1.659 | 0.022 | $16^{\circ} 30^{\prime}$ | 3.234 |
| 86 | - |  | 1.671 |  | 1.652 | 0.019 |  | 3.214 |
| 87 | - |  | 1.678 |  | 1.658 | 0.020 | $16^{\circ}$ | 3.258 |
| 88 | - | $70^{\circ}$ | 1.672 | 1.664 | 1.650 | 0.022 | $15^{\circ}$ | 3.170 |
| 89 |  | $72-74^{\circ}$ | 1.668 |  | 1.635 | 0.033 | 15-17 ${ }^{\circ}$ | 3.258 |
| 90 | - | Sm. | 1.713 | 1.710 | 1.693 | 0.020 | $17^{\circ}$ |  |
| 91 | - | $73^{\circ}$ | 1.697 | 1.691 | 1.680 | 0.017 | $19^{\circ}$ | $3.267$ |
| 92 | - |  |  | 1.65 |  |  | $26^{\circ}$ | $3.13$ |
| 93 | $+$ | $64^{\circ} 5^{\prime}$ | 1.6530 | 1.6384 | 1.6327 | 0.0203 | $26^{\circ} 20^{\prime}$ | 3.18 |
| 94 | 1 | $75^{\circ}$ | 1.677 | 1.669 | 1.652 | 0.025 | $26^{\circ}$ |  |
| 95 | - | $78^{\circ}$ | 1.683 | 1.674 | 1.658 | 0.025 | $23^{\circ}$ |  |
| 96 | - | $84^{\circ}$ | 1.672 | 1.661 | 1.648 | 0.024 | $19^{\circ}$ | $3.20$ |
| 97 | - | $47^{\circ}$ | 1.722 | 1.719 | 1.698 | 0.024 | $20^{\circ}$ | 3.375 |
| 98 | - | $16^{\circ}$ | 1.714 | $1.713$ | 1.697 | 0.017 | (Y) $15^{\circ}$ |  |
| 99 |  |  |  | $1.68$ |  |  |  | 3.283 |
| 100 | - | $79^{\circ} 38^{\prime}$ | 1.6823 | 1.6743 | 1.6576 | 0.0207 | $20^{\circ}$ | 3.224 |
| 101 | - | $88^{\circ}$. | 1.641 | 1.632 | 1.622 | 0.019 | $18-19^{\circ}$ | 3.163 |
| 102 | - | $80^{\circ}$ | 1.685 | 1.674 | 1.665 | 0.020 | $26^{\circ} 30^{\prime}$ | 3.189 |
| 103 | - | $83^{\circ}$ | 1.718 | 1.700 | 1.676 | 0.042 | $13^{\circ}$ | 3.221 |
| 104 | - | $80^{\circ}$ | 1.685 | 1.671 | 1.658 | 0.027 | $22^{\circ} 6^{\prime}$ | 3.187 |

## Part 2. Oxyhornblendes

The careful study of the changes in hornblende at about $800^{\circ} \mathrm{C}$ by Barnes ${ }^{13}$ showed very clearly the relation between "common hornblende" and oxyhornblende. He proved that ordinary hornblende is changed to oxyhornblende by heating to $800^{\circ} \mathrm{C}$. and that the chemical change is loss of hydrogen (not water) and oxidation of ferrous iron. He proved that amphibole with practically no iron undergoes practically no change. Therefore ordinary hornblendes containing no iron have the same composition and the same properties as oxyhornblendes free from iron. They are more appropriately known as ordinary hornblendes because they have suffered no oxidation, but they nevertheless are end-members of the oxyhornblende system. Consequently Fig. 7 shows the composition and properties of iron-free oxyhornblendes as well as those of common hornblendes. It may therefore be used as the base of a (partial) triangular prism showing the relations between composition and properties in all parts of that portion of the hornblende system which is the subject of this study-that is, those oxyhornblendes containing the normal tenor of $\mathrm{Ca}(+\mathrm{Na}+\mathrm{K})$.

There are only a few samples of calciferous oxyhornblendes which have been analyzed and measured optically. In Table 4 available analyses are given after being recalculated to show atomic ratios for $2400(\mathrm{O}+\mathrm{OH}$, F), as well as the coordinates used in plotting these analyses, namely: $\mathrm{Ca}+\mathrm{Na}+\mathrm{K}-200$, and $200\left(\mathrm{Mg}+\mathrm{Al}^{\prime}\right)$ divided by $\mathrm{Mg}+\mathrm{Al}^{\prime}+\mathrm{Fe}^{\prime \prime}+$ $\mathrm{Mn}+\mathrm{Fe}^{\prime \prime \prime}+\mathrm{Ti}$, just as in the case of ordinary hornblendes. The optical properties of these oxyhornblendes are given in Table 5, which also shows the properties of the ordinary hornblendes from which some of these oxyhornblendes were derived by heating.

The sample of hornblende from Frankfort, Pa. (No. 13 of Table 4), which was studied optically by V. E. Barnes in 1930 was analyzed in 1935 by Ray Wilcox with the following results: $\mathrm{SiO}_{2} 41.53, \mathrm{Al}_{2} \mathrm{O}_{3} 9.31$, $\mathrm{Fe}_{2} \mathrm{O}_{3} 9.54, \mathrm{FeO} 13.69, \mathrm{MgO} 8.14, \mathrm{CaO} 10.60, \mathrm{Na}_{2} \mathrm{O} 1.04, \mathrm{~K}_{2} \mathrm{O} 0.79$, $\mathrm{H}_{2} \mathrm{O} 5.35, \mathrm{TiO}_{2} 0.67$, $\mathrm{MnO} 0.04, \mathrm{~F} 0.33$; Sum 101.03-0.14 (for $2 \mathrm{~F}=\mathrm{O}$ ) $=$ 100.89. This shows an extraordinarily high tenor of water, but supplies a hornblende very near to tschermakite, whose properties after oxidation are known.

The eighteen analyzed samples of oxyhornblendes of Table 4 are plotted in Fig. 10 according to the same rules used in plotting the analyses of ordinary hornblendes in Fig. 2. Most of these amphiboles were ordinary hornblendes as analyzed; their optical properties were measured, and then they were changed to oxyhornblendes by heating, and the optical properties remeasured. Therefore it seems reasonable to label the endmembers as if the minerals were ordinary hornblendes. The proper formulas for oxyhornblendes will be discussed later.

[^5]Table 4. Atomic Ratios of Calciferous Oxyhornblendes for ( $0, \mathrm{OH}, \mathrm{F}$ ) $=2400$

| No. | $\left\|\begin{array}{c} \mathrm{Si} \\ -600 \end{array}\right\|$ | Al | Fe ${ }^{\prime \prime \prime}$ | $\mathrm{Fe}^{\prime \prime}$ | Mn | Ti | Mg | Ca | Na | K | H | F |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 182 | 20 | $2{ }^{\text {b }}$ | $2{ }^{\text {b }}$ |  | 1 | 485 | 205 | 11 | 3 | $202{ }^{\text {b }}$ | 5 | 19 | 198 | 1 |
| 2 | 141 | 68 | $31{ }^{\text {b }}$ | $176^{\text {b }}$ |  |  | 284 | 195 | 10 |  | $217{ }^{\text {b }}$ |  | 5 | 118 | 2 |
| 3 | 110 | 110 | $64^{\text {b }}$ | $147^{\text {b }}$ | 5 | 4 | 286 | 154 | 89 | 27 | $116^{\text {b }}$ | 10 | 70 | 116 | 1 |
| 4 | 72 | 134 | 160 | 35 | 5 | 23 | 298 | 178 | 39 | 21 | 20 | 17 | 38 | 115 | 3 |
| 5 | 58 | 203 | $13^{\text {b }}$ | $27^{\text {b }}$ | 1 | 5 | 430 | 197 | 74 | 15 | $94^{\text {b }}$ | 11 | 86 | 183 | 1,4 |
| 6 | 53 | 227 | $4^{\text {b }}$ | $12^{\text {b }}$ | 1 |  | 430 | 190 | 78 | 10 | $127^{\text {b }}$ | 12 | 78 | 194 | 1,4 |
| 7 | 51 | 196 | 141 | 4 | 4 | 10 | 324 | 185 | 72 | 37 | 5 | 23 | 94 | 140 | 1 |
| 8 | 50 | 233 | $3^{\text {b }}$ | $9{ }^{\text {b }}$ |  |  | 426 | 192 | 75 | 9 | $128{ }^{\text {b }}$ | 14 | 76 | 195 | 1,4 |
| 9 | 45 | 204 |  | 9 | 1 | 7 | 437 | 202 | 76 | 32 | 68 | 125 | 110 | 192 | 1,5 |
| 10 | 38 | 178 | 274 | 53 | tr | 12 | 167 | 178 | 83 | 26 | 8 | 19 | 87 | 70 | 1 |
| 11 | 36 | 208 | $51^{\text {b }}$ | $162^{\text {b }}$ |  | 5 | 251 | 176 | 47 | 23 | $210^{\text {b }}$ |  | 46 | 115 | 2 |
| 12 | 7 | 222 | 137 | 102 |  | 28 | 222 | 200 | 67 | 20 | 46 |  | 87 | 97 | 2 |
| 13 | , | 158 | $104^{\text {b }}$ | $164^{\text {b }}$ | 1 | 7 | 176 | 164 | 29 | 14 | $516^{\text {b }}$ | 15 | 7 | 78 | 1 |
| 14 | 0 | 210 | 131 | 3 | 9 | 33 | 315 | 187 | 70 | 29 | 122* |  | 86 | 130 | 6 |
| 15 | -1 | 226 | 85 | 80 |  | 46 | 289 | 194 | 66 | 28 | 72 |  | 88 | 120 | 2 |
| 16 | -3 | 231 | 76 | 64 |  | 48 | 303 | 199 | 81 | 18 | 67 |  | 98 | 128 | 2 |
| 17 | -7 | 241 | 78 | 29 | 1 | 57 | 334 | 187 | 54 | 46 | 43 |  | 87 | 138 | 7 |
| 18 | -8 | 262 | 86 | 47 |  | 29 | 320 | 197 | 65 | 23 | 57 |  | 85 | 140 | 2 |

${ }^{\mathrm{b}}$ Before heating.

* From ignition.


## References for Table 4

1. Barnes, V. E., Am. Mineral., 15, 393 (1930). No. 1 is tremolite from Ossining, N. Y. No. 3 is hornblende from Eganville, Ont. No. 5 is pargasite from Warwick, N. Y. No. 7 is hornblende from Lanark Co., Ont. No. 8 is pargasite from Amity, N. Y. No. 9 is hornblende from Argenteuil Co., Quebec. No. 10 is hornblende from Renfrew Co., Ont. No. 13 is hornblende from Frankfort, Pa.
2. Kunitz, W., N. Jahrb. Min. B. B. 60, 176 (1930). No. 2 is actinolite from New Hampshire, No. 11 is hornblende from Arendal. No. 12 is basaltic hornblende from Tejedatal. No. 15 is basaltic hornblende from Isleta Crater. No. 16 is basaltic hornblende from Madeira. No. 18 is basaltic hornblende from Grosspriessen.
3. Larsen, E. S., et. al., Am. Mineral., 22, 889 (1937). Basaltic hornblende from Dry Gulch, San Juan Co., Colo.
4. Winchell, A. N., Am. Mineral., 16, 259 (1931). No. 5 is pargasite from Warwick, N. Y. No. 6 is pargasite from Edenville, N. Y. No. 8 is pargasite from Amity, N. Y.
5. Harrington, B. J., Am. Jour. Sci., 173, 49 (1907). Pargasite from Grenville, Argenteuil Co., Quebec.
6. Ichimura, T., Mineral. Mag., 22, 561 (1931). Brown hornblende, Shabō-zan, Japan.
7. Parsons, A, L., U. Toronto Geol. Siud., 29, 29 (1930). Amphibole from Lochkow, Bohemia.


Fig. 10. Composition of selected oxyhornblendes.

Table 5. Optical Properties of Calciferous Oxyhornblendes

| No. | Sign | 2 V | $\mathrm{N}_{\mathrm{g}}$ | $\mathrm{N}_{\mathrm{m}}$ | $\mathrm{N}_{\mathrm{p}}$ | $\mathrm{N}_{\mathrm{g}}-\mathrm{N}_{\mathrm{p}}$ | $\mathrm{Z} \wedge c$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | - | $82^{\circ}$ | 1.6307 | 1.6183 | 1.6024 | 0.0183 | $15 \frac{1}{2}^{\circ}$ | Before heating |
| 1 | - | $82^{\circ}$ | 1.6308 | 1.6178 | 1.6026 | 0.0182 | $18^{\circ}$ | After heating |
| 2 |  |  | 1.659 |  | 1.638 | 0.021 | $17^{\circ}$ | Before heating |
| 2 |  |  | 1.676 |  | 1.655 |  |  | After heating |
| 3 | - | $63^{\circ}$ | 1.6702 | 1.6656 | 1.6539 | 0.0163 | $32^{\circ}$ | Before heating |
| 3 | - | $61^{\circ}$ | 1.7193 | 1.7060 | 1.6666 | 0.0527 | $4^{\circ}$ | After heating |
| 4 | - | Lg. | 1.735 | 1.715 | 1.675 | 0.060 | $5^{\circ}$ | Natural |
| 5 | + | $66^{\circ}$ | 1.6429 | 1.6284 | 1.6218 | 0.0211 | $24^{\circ}$ | Before heating |
| 5 | + | $86^{\circ}$ | 1.6526 | 1.6402 | 1.6287 | 0.0239 | $21^{\circ}$ | After heating |
| 6 | $+$ | $70^{\circ}$ | 1.6410 | 1.6256 | 1.6188 | 0.0222 | $21^{\circ}$ | Before heating |
| 6 | $+$ | $71^{\circ}$ | 1.6430 | 1.6291 | 1.6221 | 0.0209 | $21^{\circ}$ | After heating |
| 7 | - | $88^{\circ}$ | 1.6665 | 1.6589 | 1.6511 | 0.0154 | $23^{\circ}$ | Before heating |
| 7 | - | $66^{\circ}$ | 1.7100 | 1.6961 | 1.6626 | 0.0474 | $5^{\circ}$ | After heating |
| 8 | $+$ | $64^{\circ}$ | 1.6416 | 1.6265 | 1.6206 | 0.0210 | $22^{\circ}$ | Before heating |
| 8 | $+$ | $70^{\circ}$ | 1.6413 | 1.6265 | 1.6190 | 0.0223 | $28^{\circ}$ | After heating |
| 9 | $+$ | $58^{\circ}$ | 1.6331 | 1.6186 | 1.6143 | 0.0188 | $27^{\circ}$ | Before heating |
| 9 | $+$ | $58^{\circ}$ | 1.6317 | 1.6204 | 1.6170 | 0.0147 | $25^{\circ}$ | After heating |
| 10 | - | $38^{\circ}$ | 1.7000 | 1.6980 | 1.6804 | 0.0198 | $20^{\circ}$ | Before heating |
| 10 | - | $65^{\circ}$ | 1.7960 | 1.7690 | 1.7020 | 0.0940 | $0^{\circ}$ | After heating |
| 11 |  |  | 1.677 |  | 1.658 |  |  | Before heating |
| 11 |  |  | 1.697 |  | 1.676 |  |  | After heating |
| 12 |  |  | 1.700 |  | 1.681 | 0.019 | $0^{\circ}$ | Natural |
| 13 | - | $45^{\circ}$ | 1.6980 | 1.6950 | 1.6801 | 0.0179 | $22^{\circ}$ | Before heating |
| 13 | - | $69^{\circ}$ | 1.7825 | 1.7564 | 1.7003 | 0.0822 | $0^{\circ}$ | After heating |
| 14 | - | $82^{\circ}$ | 1.731 | 1.711 | 1.685 | 0.046 | $1^{\circ}$ | Natural |
| 15 |  |  | 1.701 |  | 1.679 | 0.022 |  | Natural |
| 16 |  |  | 1.700 |  | 1.677 | 0.023 | $6^{\circ}$ | Natural |
| 17 | - | $83^{\circ}$ | 1.718 | 1.700 | 1.676 | 0.042 | $13^{\circ}$ | Natural |
| 18 |  |  | 1.668 |  | 1.667 | 0.021 | $3^{\circ}$ | Natural |
| A | - | $81^{\circ}$ | 1.6278 | 1.6178 | 1.6042 | 0.0236 | $20^{\circ}$ | Before heating |
| A | - | $72^{\circ}$ | 1.6367 | 1.6262 | 1.6058 | 0.0309 | $13^{\circ}$ | After heating |
| B | - | $77^{\circ}$ | 1.6267 | 1.6181 | 1.6041 | 0.0226 | $16^{\circ}$ | Before heating |
| B | - | $83^{\circ}$ | 1.6284 | 1.6175 | 1.6014 | 0.0270 | $15^{\circ}$ | After heating |
| C | - | $82^{\circ}$ | 1.6301 | 1.6201 | 1.6067 | 0.0234 | $18^{\circ}$ | Before heating |
| C | - | $70^{\circ}$ | 1.6377 | 1.6270 | 1.6053 | 0.0324 | $12^{\circ}$ | After heating |
| D | - | $78^{\circ}$ | 1.6403 | 1.6278 | 1.6085 | 0.0318 | $16^{\circ}$ | Before heating |
| D | - | $56^{\circ}$ | 1.6617 | 1.6532 | 1.6220 | 0.0397 | $11^{\circ}$ | After heating |
| E | - | $73^{\circ}$ | 1.6413 | 1.6313 | 1.6133 | 0.0280 | $15^{\circ}$ | Before heating |
| E | - | $56^{\circ}$ | 1.6728 | 1.6634 | 1.6301 | 0.0427 | $10^{\circ}$ | After heating |
| F | - | $72^{\circ}$ | 1.6792 | 1.6715 | 1.6578 | 0.0214 | $20^{\circ}$ | Before heating |
| F | - | $65^{\circ}$ | 1.7477 | 1.7288 | 1.6759 | 0.0718 | $0^{\circ}$ | After heating |
| G | - | $86^{\circ}$ | 1.6640 | 1.6510 | 1.6370 | 0.0271 | $10^{\circ}$ | Before heating |
| G | - | $65^{\circ}$ | 1.7175 | 1.6980 | 1.6507 | 0.0668 | $1^{\circ}$ | After heating |

Barnes measured the optical properties of several hornblendes (both before and after heating till oxidation occurred) which have never been analyzed. It is possible to obtain the approximate composition of these samples from Fig. 9, and thus to plot their approximate position on Fig. 10. The fact that their composition is only roughly known is suggested by indicating their position by a small circle; it is not intended to suggest that the correct position must be inside the circle. These samples are labeled: $A$ to $G$, as follows: $A$, tremolite, Russell, N.Y.; $B$, tremolite, Natural Bridge, N.Y.; C, actinolite, Pierrepont, N.Y.; $D$, actinolite, Zillertal, Tyrol; $E$, actinolite, Val Malenco, Italy; $F$, hornblende, Milford, Mass.; $G$, hornblende, Tyrol.

Table 6. Approxpmate Properties of End-Members

|  | Sign | 2 V | $\mathrm{~N}_{\mathrm{g}}$ | $\mathrm{N}_{\mathrm{g}}-\mathrm{N}_{\mathrm{p}}$ | $Z \bigwedge c$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{Ca}_{2} \mathrm{Fe}^{\prime \prime}{ }_{3} \mathrm{Fe}^{\prime \prime \prime}{ }_{2} \mathrm{Si}_{8} \mathrm{O}_{24}$ | $(-)$ | $55^{\circ}$ | 1.78 | .070 | $0^{\circ}$ |
| $\mathrm{NaCa}_{2} \mathrm{Fe}^{\prime \prime}{ }_{3} \mathrm{Fe}^{\prime \prime \prime}{ }_{2} \mathrm{AlSi}_{3} \mathrm{O}_{24}$ | $(-)$ | $60^{\circ}$ | 1.79 | .075 | $0^{\circ}$ |
| $\mathrm{NaCa}_{2} \mathrm{Fe}^{\prime \prime}{ }_{2} \mathrm{Fe}^{\prime \prime \prime}{ }_{3} \mathrm{Al}_{2} \mathrm{Si}_{6} \mathrm{O}_{24}$ | $(-)$ | $55^{\circ}$ | 1.80 | .085 | $0^{\circ}$ |
| $\mathrm{Ca}_{2} \mathrm{Fe}^{\prime \prime} \mathrm{Fe}^{\prime \prime \prime}{ }_{4} \mathrm{Al}_{2} \mathrm{Si}_{6} \mathrm{O}_{24}$ | $(-)$ | $55^{\circ}$ | 1.80 | .095 | $0^{\circ}$ |

Since the chemical change involved in converting ordinary hornblende into oxyhornblende is loss of hydrogen from hydroxyl, the oxygen atom which remains in the crystal having its valence satisfied by the simultaneous change of one atom of iron from the ferrous to the ferric state, the process can result in the oxidation of only as many atoms of iron as the number of atoms of hydrogen which are driven out of the crystal. This conclusion is confirmed by the results of the analysis of the hornblende from Renfrew Co., Ont. (after complete oxidation at about $800^{\circ} \mathrm{C}$ ) which show that even after driving out all the hydrogen an oxyhornblende may still contain ferrous iron. Therefore no oxyhornblende can contain more than two atoms of ferric iron which are due to the process of oxidation. Since the iron end-member formulas of ordinary calciferous hornblende are: $\mathrm{Ca}_{2} \mathrm{Fe}^{\prime \prime}{ }_{5} \mathrm{Si}_{8} \mathrm{O}_{22}(\mathrm{OH})_{2}, \mathrm{NaCa}_{2} \mathrm{Fe}^{\prime \prime}{ }_{5} \mathrm{AlSi}_{7} \mathrm{O}_{22}(\mathrm{OH})_{2}, \quad \mathrm{NaCa}_{2}-$ $\mathrm{Fe}^{\prime \prime}{ }_{4} \mathrm{Fe}^{\prime \prime \prime} \mathrm{Al}_{2} \mathrm{Si}_{6} \mathrm{O}_{22}(\mathrm{OH})_{2}$ and $\mathrm{Ca}_{2} \mathrm{Fe}^{\prime \prime}{ }_{3} \mathrm{Fe}^{\prime \prime \prime}{ }_{2} \mathrm{Al}_{2} \mathrm{Si}_{6} \mathrm{O}_{22}(\mathrm{OH})_{2}$, the corresponding formulas for oxyhornblende must be $\mathrm{Ca}_{2} \mathrm{Fe}^{\prime \prime}{ }_{3} \mathrm{Fe}^{\prime \prime \prime}{ }_{2} \mathrm{Si}_{8} \mathrm{O}_{24}$, $\mathrm{NaCa}_{2}-$ $\mathrm{Fe}^{\prime \prime}{ }_{3} \mathrm{Fe}^{\prime \prime \prime}{ }_{2} \mathrm{AlSi}_{7} \mathrm{O}_{24}, \quad \mathrm{NaCa}_{2} \mathrm{Fe}^{\prime \prime}{ }_{2} \mathrm{Fe}^{\prime \prime \prime}{ }_{3} \mathrm{Al}_{2} \mathrm{Si}_{6} \mathrm{O}_{24}$ and $\mathrm{Ca}_{2} \mathrm{Fe}^{\prime \prime} \mathrm{Fe}^{\prime \prime \prime}{ }_{4} \mathrm{Al}_{2} \mathrm{Si}_{6} \mathrm{O}_{24}$.

Knowing the approximately correct position of the hornblende samples $A$ to $E$ on Figs. 9 and 10, their content of iron can be obtained fairly closely from Figs 4, 5 and 6. In this way it is possible to find that actual data extend only to 20 per cent of the iron molecule in the $\mathrm{Ca}_{2} \mathrm{Mg}_{5} \mathrm{Si}_{8} \mathrm{O}_{22}$

Fig. 11. Properties on the front faces of the (partial) triangular prism (oxyhornblende).
$(\mathrm{OH})_{2}-\mathrm{Ca}_{2} \mathrm{Fe}^{\prime \prime}{ }_{3} \mathrm{Fe}^{\prime \prime \prime}{ }_{2} \mathrm{Si}_{8} \mathrm{O}_{24}$ series. For all the rest of this series the properties are obtained by extrapolation, keeping in mind that only two of the five replacing Fe atoms can be oxidized, and also using the conclusions reached by Barnes that (1) the extinction angle decreases to zero, but


Fig. 12. Optical properties of calciferous oxyhornblendes.
does not become minus, and (2) the optic angle about $\mathbf{X}$ decreases to about $55^{\circ}$, but not to any value materially less, no matter how much iron may be present. It is surprising to discover that both of these changes are completed before all the oxidation is completed.

In other parts of the system data are available to about 60 per cent of the iron molecules.

By such approximate and admittedly unsatisfactory methods the properties of the iron end-members of the calciferous oxyhornblende system have been derived as given in Table 6.

The variations in properties on the front faces of a (partial) triangular prism of the oxyhornblende system are shown in Fig. 11. Finally the variations in properties as related to variations in composition in all parts of the system are shown in clinographic projection in Fig. 12. It is obvious that this is only a first approximation.

In using this graph it should be remembered that it represents the conditions in oxyhornblendes after complete oxidation; many, if not all, natural oxyhornblendes are not completely oxidized; therefore their properties are intermediate between those of ordinary hornblende, and those of completely oxidized hornblende. It may be useful to note that the size of the extinction angle is a guide to the amount of oxidation, but, natural oxyhornblendes with an extinction angle of zero are not completely oxidized (at least in most cases). The size of the optic angle is also a guide to the amount of oxidation, but it can not be measured as easily as the extinction angle.

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[^0]:    ${ }^{1}$ Hallimond, A. F., Am. Mineral., 28, 65 (1943).

[^1]:    ${ }^{2}$ Warren, B. E., Zeit. Krist., 72, 493 (1930).
    ${ }^{3}$ Schaller, W. T., U. S. Geol. Surv., Bull. 610, 133 (1916).

[^2]:    ${ }^{4}$ Zeit. Krist., 70, 214 (1929).

[^3]:    ${ }^{5}$ Winchell, A. N., Am. Mineral , 16, 257 (1931).

[^4]:    ${ }^{6}$ Hallimond, A. F., Am. Mineral., 28, p. 79, note 107 (1943).
    ${ }^{7}$ Winchell, A. N., Am. Mineral., 16, 260 (1931).

[^5]:    ${ }^{13}$ Barnes, V. E., Am. Mineral., 15, 393 (1930).

