# The crystal structure of pararobertsite and its relationship to mitridatite 

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#### Abstract

The crystal structure of pararobertsite, $\mathrm{Ca}_{2}\left(\mathrm{H}_{2} \mathrm{O}\right)_{2}\left[\mathrm{Mn}_{3}^{3+} \mathrm{O}_{2}\left(\mathrm{PO}_{4}\right)_{3}\right] \cdot \mathrm{H}_{2} \mathrm{O}, P 2_{1} / c, a=8.814(4), b=$ 13.233(5), $c=11.056(4) \AA, \beta=101.184(7)^{\circ}, V=1265.0(9) \AA^{3}, Z=4$ has been solved by direct methods and refined to $R=0.042$ for $1319 F_{\mathrm{o}}>4 \sigma\left(F_{\mathrm{o}}\right)$ using MoK $\alpha$ X-ray data. In the structure of pararobertsite, Z -shaped edge-sharing chains of $\mathrm{Mn}^{3+} \mathrm{O}_{6}$ octahedra link to one another via shared O vertices and $\mathrm{PO}_{4}$ tetrahedra to form a compact sheet of composition ${ }_{\infty}^{2}\left[\mathrm{Mn}_{3}^{3+} \mathrm{O}_{2}\left(\mathrm{PO}_{4}\right)_{3}\right]^{4}$ oriented parallel to $\{100\}$. The space between the compact sheets is filled with a thick open assemblage of $\mathrm{CaO}_{5}\left(\mathrm{H}_{2} \mathrm{O}\right)_{2}$ polyhedra and isolated water molecules. The structure bears strong similarities to the mitridatite $\left(\mathrm{Fe}^{3+}\right)$ structure and, therefore, to its robertsite $\left(\mathrm{Mn}^{3+}\right)$ isotype.


## Introduction

The mineral pararobertsite from from the Tip Top pegmatite, Custer County, South Dakota was described by Roberts et al. (1989), who named the mineral for its close chemical and crystallographic relationship to robertsite, $\mathrm{Ca}_{6}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}$ $\left[\mathrm{Mn}_{9}^{3+} \mathrm{O}_{6}\left(\mathrm{PO}_{4}\right)_{9}\right] \cdot 3 \mathrm{H}_{2} \mathrm{O}$ in the asymmetric unit, $\mathrm{Z}=4$. Robertsite is isostructural with mitridatite, $\mathrm{Ca}_{6}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\left[\mathrm{Fe}_{9}^{3+} \mathrm{O}_{6}\right.$ $\left.\left(\mathrm{PO}_{4}\right)_{9}\right] \cdot 3 \mathrm{H}_{2} \mathrm{O}$, whose structure was determined by Moore and Araki (1977). This study was undertaken to elucidate the structural relationship between pararobertsite and robertsite.

## STRUCTURE DETERMINATION

Single-crystal X-ray precession and diffractometer studies showed pararobertsite to be monoclinic, space group $P 2_{1} / c, a$ $=8.814(4), b=13.233(5), c=11.056(4) \AA, \beta=101.184(7)^{\circ}, V$ $=1265.0(9) \AA^{3}, Z=4$. The cell parameters were refined from the peak positions obtained from the structure data collection. These cell parameters compare closely to those reported by Roberts et al. (1989), $a=8.825, b=13.258, c=11.087 \AA, \beta=$ $101.19^{\circ}$.

X-ray intensity data were collected from a thin tabular crystal of pararobertsite of dimensions $0.14 \times 0.11 \times 0.01 \mathrm{~mm}^{3}$ using a Bruker PLATFORM 3-circle goniometer equipped with a 1 K SMART CCD detector. The operating conditions were: room temperature, $50 \mathrm{kV}, 45 \mathrm{~mA}$, graphite-monochromatized $\mathrm{Mo} K \alpha$ radiation ( $\lambda=0.71069 \AA$ ). Frame widths of $0.3^{\circ}$ in $\omega$ were used to acquire each frame for 120 s . A total of 1271 frames of data was collected, providing a half sphere of three-dimensional data. Data were collected for $4.7^{\circ} \leq 2 \theta \leq 56.6^{\circ}$. Fifty duplicate frames acquired at the end of the data collection indicated that no significant decay had taken place. The 7946 measured intensities ( $\overline{1} 1 \leq h \leq 11, \overline{1} 3 \leq k \leq 17, \overline{1} 4 \leq l \leq 14)$ were corrected for Lorentz and polarization effects using the program SAINT and an empirical absorption correction was applied using the

[^0]program SADABS. The final data set reduced to 3014 unique reflections. The absorption correction lowered $R_{\mathrm{INT}}$ from 3.8 to $3.1 \%$.

The SHELXL97 software (Sheldrick 1997) was used for the determination and refinement of the structure. The metal atoms $(\mathrm{Ca}, \mathrm{Mn}$, and P$)$ and several of the O atoms were readily located by direct methods. The positions of the remaining O atoms were obtained from subsequent difference-Fourier syntheses. In subsequent refinement cycles, anisotropic displacement parameters for all non-hydrogen atoms were refined to a conventional $R$ index of 0.043 and $w R_{2}=0.105$ [weighted $R$ factor on $F^{2}$, as defined by Sheldrick (1997)] for 1319 measured reflections with $F_{\mathrm{o}}>4 \sigma\left(F_{\mathrm{o}}\right), R=0.137$ and $w R_{2}=0.153$ for all 3014 data, and goodness of fit $=0.619$. At this point examination of the highest peaks in the difference-Fourier synthesis coupled with valence-bond and geometrical considerations allowed the location of all H atoms. With H atom positions and isotropic displacement parameters $(=0.05)$ held invariant, the final refinement cycles yielded $R=0.042$ and $w R_{2}=0.099$ for 1319 measured reflections with $F_{\mathrm{o}}>4 \sigma\left(F_{\mathrm{o}}\right), R$ $=0.136$ and $w R_{2}=0.149$ for all 3014 reflections, and goodness of fit $=0.601$. Maximum and minimum heights in the final difference Fourier synthsis were +1.15 and $-0.76 e / \AA^{3}$.

Table 1 includes the final fractional coordinates and displacement parameters, Table $2^{1}$ the observed and calculated structure factors, Table 3 interatomic distances and angles, and Table 4 the bond valences.

## DESCRIPTION OF THE STRUCTURE AND COMPARISON TO MITRIDATITE

In the structure of pararobertsite, Z -shaped edge-sharing chains of $\mathrm{Mn}^{3+} \mathrm{O}_{6}$ octahedra link to one another via shared O vertices and $\mathrm{PO}_{4}$ tetrahedra to form a compact sheet of composition ${ }_{\infty}^{2}\left[\mathrm{Mn}_{3}^{3+} \mathrm{O}_{2}\left(\mathrm{PO}_{4}\right)_{3}\right]^{4}$ oriented parallel to $\{100\}$ (Fig. 1a). (The notation ${ }_{\infty}^{2}$ indicates a structural unit that extends infinitely in two dimensions, i.e., a sheet.) The space between the compact sheets is filled with a thick open assemblage of $\mathrm{CaO}_{5}\left(\mathrm{H}_{2} \mathrm{O}\right)_{2}$


|  | $x$ | $y$ | $z$ | $U_{11}$ | $U_{22}$ | $U_{33}$ | $U_{23}$ | $U_{13}$ | $U_{12}$ | $U_{\text {eq }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Mn1 | 0 | 0 | 0 | 74(10) | 112(10) | 55(10) | 12(9) | 19(8) | -28(9) | 79(4) |
| Mn2 | 0 | 0 | 1/2 | 108(10) | 62(9) | 49(10) | 3(8) | 28(8) | 13(9) | 72(4) |
| Mn3 | 0.0130(2) | 0.1311(1) | 0.2380(1) | 86(6) | 81(7) | 54(6) | 12(6) | 16(5) | 3(6) | 73(3) |
| Mn4 | 0.0140(2) | 0.2319(1) | 0.4932(1) | 69(7) | 82(7) | 54(8) | -7(6) | 8(6) | -13(6) | 69(3) |
| Ca1 | 0.3384(2) | 0.3707(2) | 0.5725(2) | 84(8) | 137(10) | 214(10) | -08(9) | 31(7) | -3(9) | 145(4) |
| Ca 2 | 0.6674(2) | 0.1232(2) | 0.3595(2) | 106(8) | 130(10) | 123(9) | 0(9) | 2(7) | -15(9) | 122(4) |
| P1 | 0.2968(3) | 0.1104(2) | 0.4457(2) | 103(11) | 71(12) | 77(11) | 15(9) | 24(9) | -9(10) | 83(5) |
| P2 | 0.0845(3) | 0.1189(2) | 0.7757(2) | 112(11) | 85(12) | 100(11) | -15(10) | 23(9) | -2(11) | 99(5) |
| P3 | 0.7281(3) | 0.1407(2) | 0.0292(2) | 63(10) | 90(12) | 67(11) | -7(9) | 18(8) | -10(9) | 73(5) |
| O1 | 0.4696(7) | 0.1112(5) | 0.4660(5) | 128(32) | 183(38) | 92(31) | 35(29) | 7(25) | 5(30) | 136(14) |
| O2 | 0.2361(7) | 0.2038(5) | 0.5065(6) | 62(32) | 101(32) | 79(33) | -17(26) | 15(27) | 22(26) | 81(14) |
| O3 | 0.2344(8) | 0.0125(5) | 0.4985(6) | 150(35) | 41(32) | 141(35) | 6(27) | 41(29) | -38(27) | 109(14) |
| O4 | 0.2280(7) | 0.1135(5) | 0.3039(5) | 109(30) | 173(35) | 58(29) | 22(29) | 0(24) | -12(30) | 115(13) |
| O5 | 0.2558(7) | 0.1180(5) | 0.8283(6) | 104(30) | 143(35) | 240(37) | -18(33) | 30(27) | 10(31) | 163(14) |
| 06 | 0.0089(7) | 0.2162(5) | 0.8103(6) | 136(34) | 114(34) | 130(35) | 4(28) | 77(28) | 38(28) | 120(14) |
| O7 | 0.0349(7) | 0.1083(5) | 0.6354(5) | 146(32) | 118(34) | 74(30) | 12(26) | 27(26) | -25(28) | 112(14) |
| O8 | 0.0021(7) | 0.0302(5) | 0.8293(6) | 124(34) | 70(32) | 124(35) | 16(26) | 31(28) | 2(27) | 105(14) |
| 09 | 0.5574(7) | 0.1429(5) | 0.0003(6) | 91(30) | 196(39) | 106(31) | -8(29) | 43(25) | -41(29) | 128(14) |
| O10 | 0.7949(7) | 0.2359(5) | 0.9754(6) | 76(33) | 92(32) | 105(35) | 29(26) | 37(27) | -13(26) | 88(14) |
| 011 | 0.7912(7) | 0.1399(5) | 0.1709(5) | 96(29) | 134(35) | 44(29) | -17(26) | -2(24) | 24(28) | 93(13) |
| 012 | 0.7866 (7) | 0.0429(5) | 0.9729(6) | 66(33) | 158(35) | 86(35) | -71(27) | 4(28) | -38(27) | 105(15) |
| O13 | 0.9532(6) | 0.1111(5) | 0.3952(5) | 87(29) | 56(30) | 72(29) | -14(26) | 26(24) | 32(27) | 70(12) |
| O14 | 0.0678(7) | 0.1490(5) | 0.0797(5) | 60(29) | 148(36) | 78(31) | 24(26) | -4(24) | 31(27) | 98(14) |
| 015 | 0.5175(8) | 0.0124(5) | 0.2143(7) | 220(41) | 102(36) | 198(38) | 49(30) | 29(32) | -2(30) | 175(16) |
| 016 | 0.4783(8) | 0.2372(5) | 0.2383(6) | 134(36) | 172(39) | 208(42) | -16(30) | 13(31) | 10(30) | 174(17) |
| O17 | 0.6702(9) | $0.3843(6)$ | 0.1964(6) | 462(48) | 143(38) | 217(38) | 37(34) | 172(35) | -27(39) | 260(17) |
| H1 | 0.4311 | 0.9791 | 0.2406 |  |  |  |  |  |  | 5 |
| H2 | 0.6035 | 0.9367 | 0.1929 |  |  |  |  |  |  | 5 |
| H3 | 0.5446 | 0.2719 | 0.2463 |  |  |  |  |  |  | 5 |
| H4 | 0.4150 | 0.2680 | 0.2482 |  |  |  |  |  |  | 5 |
| H5 | 0.7146 | 0.3309 | 0.1885 |  |  |  |  |  |  | 5 |
| H6 | 0.6275 | 0.4330 | 0.1204 |  |  |  |  |  |  | 5 |

polyhedra and isolated water molecules. The structure bears strong similarities to the mitridatite (robertsite) structure type.

The compact sheet of octahedra and tetrahedra in mitridatite (Fig. 1b) is based upon nine-membered trigonal rings of edgesharing octahedra. While the ring motif in mitridatite represents a distinctly different topology from the Z-chain motif in pararobertsite, the local geometries of the octahedral linkages are similar in the two sheets. Furthermore, the loci of the trivalent cations in both of the sheets define the vertices of the Kagomé net (Figs. 1c and 1d). This latter structural similarity accounts for the similar pseudohexagonal symmetries noted by Roberts et al. (1989) in the 0 kl planes of precession films for these minerals. The linkings of $\mathrm{PO}_{4}$ tetrahedra to the octahedra in the two sheets are topologically and geometrically quite similar as well, leading to identical sheet compositions in the two structures. One interesting contrast between the sheets is that the geometry of the ring motif of mitridatite requires linkages of octahedra and tetrahedra that yield non-centric (polar) symmetry, while the Z-chain geometry of pararobertsite is consistent with a centric arrangement of octahedra and tetrahedra.

The two nonequivalent Ca atoms nestle into pockets in the sheets, each forming bonds to four phosphate O atoms and one oxo atom (also shared by three $\mathrm{Mn}^{3+}$ atoms in the sheet). The sevenfold coordination of each Ca is completed by bonds to

[^1]two water molecules. The water molecules define a shared edge between two Ca polyhedra nestled into adjacent sheets, thereby creating $\mathrm{Ca}_{2} \mathrm{O}_{10}\left(\mathrm{H}_{2} \mathrm{O}\right)_{2}$ dimers, which provide the glue that binds the sheets to one another. Contributing to a lesser extent to the adhesion between the sheets is a network of hydrogen bonds involving the water molecules bonded to the Ca atoms and an additional free water molecule also nestled into pockets in the sheets. The ${ }_{\infty}^{2}\left[\mathrm{Ca}_{2} \mathrm{O}_{10}\left(\mathrm{H}_{2} \mathrm{O}\right)_{2} \cdot \mathrm{H}_{2} \mathrm{O}\right]$ layer described above and shown in (Fig. 2) matches the corresponding layer in mitridatite very closely. Figure 3 shows the assembly of ${ }_{\infty}^{2}\left[\mathrm{Mn}_{3}^{3+} \mathrm{O}_{2}\left(\mathrm{PO}_{4}\right)_{3}\right]$ sheets and the ${ }_{\infty}^{2}\left[\mathrm{Ca}_{2} \mathrm{O}_{10}\left(\mathrm{H}_{2} \mathrm{O}\right)_{2} \cdot \mathrm{H}_{2} \mathrm{O}\right]$ layer on edge.

The structural formula for pararobertsite is $\mathrm{Ca}_{2}\left(\mathrm{H}_{2} \mathrm{O}\right)_{2}$ $\left[\mathrm{Mn}_{3}^{3+} \mathrm{O}_{2}\left(\mathrm{PO}_{4}\right)_{3}\right] \cdot \mathrm{H}_{2} \mathrm{O}, \mathrm{Z}=4$. This is consistent with the formula proposed by Roberts et al. (1989) and is exactly one third the cell content of robertsite, $\mathrm{Ca}_{6}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\left[\mathrm{Mn}_{9}^{3+} \mathrm{O}_{6}\left(\mathrm{PO}_{4}\right)_{9}\right] \cdot 3 \mathrm{H}_{2} \mathrm{O}, \mathrm{Z}=$ 4. Not surprising from the structural similarities noted above is the fact that the cell volume of pararobertsite $\left(1265.1 \AA^{3}\right)$ is almost exactly one third that of robertsite $\left(3810.2 \AA^{3}\right)$.

## $\mathbf{M n}^{3+} \mathrm{O}_{6}$ octahedra

Moore and Araki (1977) commented on the distortions of octahedra inherent in the edge-sharing nonamers and octahedral sheet as a whole in the mitridatite structure type. The cis edge-sharing octahedra ( $\mathrm{Fe} 1, \mathrm{Fe} 2$, and Fe 3 ) at the corners of the trigonal rings in mitridatite must be severely strained in order to achieve a $\mathrm{Fe}-\mathrm{Fe}-\mathrm{Fe}$ angle approaching $60^{\circ}$. It is intriguing that a virtually identically distorted cis edge-sharing octahedron (Mn4) is incorporated at the bends in the Z-chains of pararobertsite.

Cation-cation repulsions across the shared edges play a significant role in the geometries of the octahedra, effectively

TABLE 3. Bond lengths ( $(\AA)$ and selected polyhedral edge lengths ( $(\AA)$ and bond angles $\left({ }^{\circ}\right)$ in pararobertsite

| Mn1-O12 $\times 2$ | 1.932 |  | Mn2-O13×2 | 1.867 |  | Ca1-O9 | 2.234 | H1-O15-H2 | $103^{\circ}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Mn1-O8 $\times 2$ | 1.933 |  | Mn2-O7 $\times 2$ | 2.052 |  | Ca1-O14 | 2.417 | O15-H1 | 0.97 |
| Mn1-O14 $\times 2$ | 2.195 |  | Mn2-O3 $\times 2$ | 2.076 |  | Ca1-O2 | 2.443 | H1-O17 | 1.76 |
| Mean | 2.020 |  | Mean | 1.998 |  | Ca1-O16 | 2.459 | O15-H2 | 1.30 |
| O8-014 $\times 2$ * | 2.693 | 81.2 | 07-013 $\times 2$ * | 2.613 | 83.5 | Ca1-015 | 2.527 | H2-O5 | 1.49 |
| 08-012 $\times 2$ | 2.707 | 88.9 | O3-013 $\times 2$ | 2.746 | 88.1 | Ca1-O12 | 2.538 |  |  |
| 08-012 $\times 2$ | 2.758 | 91.1 | O3-07 $\times 2$ | 2.832 | 86.6 | Ca1-O5 | 2.660 | H3-O16-H4 | $105^{\circ}$ |
| O12-014 $\times 2$ | 2.894 | 88.8 | O3-013 $\times 2$ | 2.837 | 91.9 | Mean 2.468 |  | O16-H3 | 0.73 |
| O12-014 $\times 2$ | 2.954 | 91.2 | 07-013 $\times 2$ | 2.926 | 96.5 |  |  | H3-017 | 1.99 |
| O8-O14 $\times 2$ | 3.139 | 98.8 | O3-07 $\times 2$ | 3.003 | 93.4 | Ca2-O1 | 2.291 | O16-H4 | 0.72 |
| Mean | 2.858 | 90.0 | Mean | 2.826 | 90.0 | Ca2-015 | 2.377 | H4-O5 | 2.35 |
|  |  |  |  |  |  | Ca2-010 | 2.414 |  |  |
| Mn3-O4 | 1.908 |  | Mn4-O14 | 1.857 |  | Ca2-O3 | 2.431 | H5-O17-H6 | $123^{\circ}$ |
| Mn3-O14 | 1.918 |  | Mn4-O13 | 1.948 |  | Ca2-016 | 2.447 | O17-H5 | 0.82 |
| Mn3-O13 | 1.931 |  | Mn4-O10 | 1.950 |  | Ca2-013 | 2.478 | H5-O11 | 2.63 |
| Mn3-011 | 1.955 |  | Mn4-O2 | 1.970 |  | Ca2-011 | 2.544 | H5-O6 | 2.75 |
| Mn3-O6 | 2.176 |  | Mn4-O6 | 2.128 |  | Mean 2.426 |  | H5-O10 | 2.88 |
| Mn3-08 | 2.255 |  | Mn4-O7 | 2.252 |  |  |  | O17-H6 | 1.07 |
| Mean | 2.024 |  | Mean | 2.018 |  | P1-O1 1.496 |  | H6-O1 | 2.07 |
| 06-013* | 2.556 | 76.7 | 06-013* | 2.556 | 77.5 | P1-O2 1.552 |  |  |  |
| O11-O13 | 2.639 | 85.5 | 07-O13* | 2.613 | 76.6 | P1-O3 1.564 |  |  |  |
| O4-014 | 2.646 | 87.5 | O2-014 | 2.667 | 88.3 | P1-O4 1.568 |  |  |  |
| 08-014* | 2.693 | 79.9 | O10-013 | 2.704 | 87.9 | Mean 1.545 |  |  |  |
| 04-013 | 2.799 | 93.7 | O10-014 | 2.713 | 90.9 |  |  |  |  |
| O11-O14 | 2.815 | 93.2 | O2-07 | 2.785 | 82.3 | P2-O5 1.509 |  |  |  |
| 08-011 | 2.896 | 86.6 | O2-013 | 2.837 | 92.8 | P2-O6 1.531 |  |  |  |
| 06-011 | 2.922 | 89.8 | O2-06 | 2.855 | 88.3 | P2-O7 1.534 |  |  |  |
| 04-08 | 2.955 | 90.1 | 06-010 | 2.880 | 89.7 | P2-O8 1.558 |  |  |  |
| O4-06 | 2.978 | 93.4 | 06-014 | 3.056 | 99.9 | Mean 1.533 |  |  |  |
| 08-013 | 3.192 | 99.1 | 07-010 | 3.226 | 100.1 |  |  |  |  |
| O6-014 | 3.234 | 104.2 | O7-014 | 3.293 | 106.2 | P3-09 1.476 |  |  |  |
| Mean | 2.860 | 90.0 | Mean | 2.849 | 90.0 | P3-O10 | 1.556 |  |  |
|  |  |  |  |  |  | P3-011 | 1.558 |  |  |
|  |  |  |  |  |  | P3-O12 | 1.566 |  |  |
|  |  |  |  |  |  | Mean 1.539 |  |  |  |

Notes: Standard deviations for bond distances are 0.006 to 0.007 for $\mathrm{Ca}, \mathrm{Mn}, \mathrm{P}-\mathrm{O}$ and 0.008 to 0.009 for O-O. Standard deviations for bond angles are 0.2 to 0.4. Asterisks ( ${ }^{*}$ ) indicate shared octahedral edges. The number following each O-O distance denotes the corresponding $\mathrm{O}-\mathrm{M}-\mathrm{O}$ angle.

TABLE 4. Bond valences for pararobertsite

|  | O1 | O2 | O3 | O4 | O5 | 06 | O7 | O8 | O9 | O 10 | 011 | O12 | 013 | O14 | 015 | O16 | O17 | $\Sigma_{\text {c }}$ V |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Ca1 |  | 0.276 |  |  | 0.154 |  |  |  | 0.486 |  |  | 0.214 |  | 0.296 | 0.220 | 0.265 |  | 1.911 |
| Ca2 | 0.417 |  | 0.285 |  |  |  |  |  |  | 0.299 | 0.210 |  | 0.251 |  | 0.330 | 0.273 |  | 2.066 |
| Mn1 |  |  |  |  |  |  |  | $0.627 \times 2$ |  |  | $0.628 \times 2$ | $0.309 \times 2$ |  |  | 3.127 |  |  |  |
| Mn2 |  |  | $0.426 \times 2$ |  |  | $0.454 \times 2$ |  |  |  |  |  | $0.749 \times 2$ |  |  |  | 3.258 |  |  |
| Mn3 |  |  |  | 0.670 |  | 0.325 |  | 0.262 |  |  | 0.590 |  | 0.630 | 0.652 |  |  |  | 3.130 |
| Mn4 |  | 0.567 |  |  |  | 0.370 | 0.265 |  |  | 0.598 |  |  | 0.602 | 0.769 |  |  |  | 3.171 |
| P1 | 1.387 | 1.192 | 1.154 | 1.142 |  |  |  |  |  |  |  |  |  |  |  |  |  | 4.875 |
| P2 |  |  |  |  | 1.339 | 1.262 | 1.251 | 1.173 |  |  |  |  |  |  |  |  |  | 5.025 |
| P3 |  |  |  |  |  |  |  |  | 1.464 | 1.179 | 1.173 | 1.148 |  |  |  |  |  | 4.964 |
| H1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 0.790 |  | 0.210 | 1.000 |
| H2 |  |  |  |  | 0.330 |  |  |  |  |  |  |  |  |  | 0.670 |  |  | 1.000 |
| H3 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 0.870 | 0.130 | 1.000 |
| H4 |  |  |  |  | 0.070 |  |  |  |  |  |  |  |  |  |  | 0.930 |  | 1.000 |
| H5 |  |  |  |  |  | 0.030 |  |  |  | 0.020 | 0.040 |  |  |  |  |  | 0.910 | 1.000 |
| H6 | 0.110 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 0.890 | 1.000 |
| $\Sigma_{\text {a }} v$ | 1.913 | 2.035 | 1.865 | 1.812 | 1.893 | 1.986 | 1.970 | 2.062 | 1.950 | 2.096 | 2.013 | 1.990 | 2.232 | 2.027 | 2.010 | 2.338 | 2.140 |  |

Notes: Multiplicities are indicated for equivalent bonds for each cation. Constants from Brese and O'Keeffe (1991). Hydrogen bond valence based upon Brown and Altermatt (1985).
shortening the polyhedral shared O-O edges and diminishing the corresponding polyhedral angles (see Table 3). Again the distortions are most dramatically manifest in the Mn4 octahedron because its two shortest edges are adjacent. An interesting conjecture is that the Kagomé net arrangements of the $\mathrm{M}^{3+}$ cations within the planes of octahedra in the mitridatite and pararobertsite sheets (Figs. 1c and 1d) developed in response to $\mathrm{M}^{3+}$ cation-cation repulsions. This arrangement can be viewed as a planar cation close-packing with vacancies. In both structures $\mathrm{P}^{5+}$ cations ( P 2 in pararobertsite) are located at sites slightly above or below the vacancies in the cation close-packed planes.

Note that the $\mathrm{M}^{3+}-\mathrm{M}^{3+}$ distances are shortest across the shared edges (thicker lines in Figs. 1c and 1d).

The Mn1, Mn3, and Mn4 octahedra exhibit classic JahnTeller distortion, each having two long apical bonds, whereas the Mn2 octahedron shows a "reverse" Jahn-Teller distortion with two shortened apical bonds. Based upon bond valence considerations, Moore and Araki (1977) predicted the JahnTeller distortions that would be manifest in the structure of robertsite, the $\mathrm{Mn}^{3+}$ analog of mitridatite. Their predictions were borne out with the solution of the långbanite structure (Moore et al. 1991), which includes, among four discrete sheets, a
a


## C


b

d


Figure 1. (a) Pararobertsite sheet of composition ${ }_{\infty}^{2}\left[\mathrm{Mn}_{3}^{3+} \mathrm{O}_{2}\left(\mathrm{PO}_{4}\right)_{3}\right]^{4-}$ oriented parallel to $\{100\}$. The O atoms are numbered; Mn atoms can be identified from Figure 1c. P1, P2, and P3 can be identified by their bonded O atoms. (b) Mitridatite sheet of composition ${ }_{\infty}^{2}\left[\mathrm{Fe}_{9}^{3+} \mathrm{O}_{6}\left(\mathrm{PO}_{4}\right)_{9}\right]^{12-}$ oriented parallel to $\{100\}$. (c) Kagomé net of $\mathrm{Mn}^{3+}$ atoms in pararobertsite. $\mathrm{Mn}^{3+}-\mathrm{Mn}^{3+}$ distances are shown; distances corresponding to shared edges are indicated by thick lines. (d) Kagomé net of $\mathrm{Fe}^{3+}$ atoms in mitridatite. For 1 c and $1 \mathrm{~d}, \mathrm{M}^{3+}-\mathrm{M}^{3+}$ distances are shown; distances corresponding to shared edges are indicated by thick lines.
mitridatite-type sheet of $\mathrm{Mn}^{3+}$ octahedra. The Jahn-Teller distortions in the Mn3 and Mn4 octahedra in pararobertsite correspond to the distortions observed in similarly positioned octahedra in the mitridatite-type sheet of långbanite. All of the elongated apical bonds in these octahedra and in the Mn1 octahedron are in the plane of the sheet. The shortened apical bond pair of the Mn2 octahedron is also in this plane. This suggests a complimentary relationship between the Jahn-Teller distortions and the distortions required by the geometry of the octahedral linkages within the sheets. Of course, the bond valence balance is an essential component of this relationship.

A final consideration in assessing the distortions of the octahedra is the canting of the octahedral vertices that are not in
the plane of the sheet. This canting is necessary to accommodate the linkages to the $\mathrm{PO}_{4}$ tetrahedra ( P 1 and P 3 ).

Besides exhibiting a reverse Jahn-Teller effect, the Mn2 octahedron shows the least $\mathrm{O}-\mathrm{Mn}-\mathrm{O}$ angular distortions and has the shortest Mn-O average bond distance, $1.998 \AA$. This is also shorter than any octahedral $\mathrm{Fe}-\mathrm{O}$ average noted in mitridatite. It is likely that the small quantity of $\mathrm{Fe}^{3+}$ in pararobertsite reported by Roberts et al. (1989) is accommodated in this site.

## $\mathrm{PO}_{4}$ tetrahedra

Each of the three nonequivalent $\mathrm{PO}_{4}$ tetrahedra possesses one P-O bond that is significantly shorter than the rest. The


Figure 2. $\mathrm{A}^{2}\left[\mathrm{Ca}_{2} \mathrm{O}_{10}\left(\mathrm{H}_{2} \mathrm{O}\right)_{2} \cdot \mathrm{H}_{2} \mathrm{O}\right]$ layer in pararobertsite oriented parallel to $\{100\}$. The O and H atoms are numbered.
same is observed in the mitridatite structure. In every case in both structures, the short P-O bond points away from the plane of the octahedral sheet and is not involved in any $\mathrm{M}^{3+}$ bonds. Each of these O atoms bonds only to one P and one Ca atom (sometimes with H bonding as well), and the short $\mathrm{P}-\mathrm{O}$ bonds compensate for the otherwise relatively low bond strength sums received by these O atoms.

## $\mathrm{CaO}_{5}\left(\mathrm{H}_{2} \mathrm{O}\right)_{2}$ polyhedra

Both of the two nonequivalent Ca atoms in pararobertsite are coordinated to seven O atoms: four from phosphate groups, one in the plane of the octahedral sheet, and two of $\mathrm{H}_{2} \mathrm{O}$ molecules. The coordination geometry about Ca 1 is irregular, while that about Ca 2 can be described as an octahedron with an additional oxygen above one octahedral face (e.g., a monocapped octahedron). The latter geometry is comparable to that noted for all of the Ca polyhedra in mitridatite.

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Figure 3. Atomic structure of pararobertsite viewed down the $b$ axis. Octahedra have a medium stipple. Tetrahedra are lightly stippled. $\mathrm{H}_{2} \mathrm{O}$ molecules are shown in perspective.
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