

The new K, Pb-bearing uranyl-oxide mineral kroupaite: Crystal-chemical implications for the structures of uranyl-oxide hydroxy-hydrates

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ABSTRACT

Kroupaite (IMA 2017-031), ideally $\text{KPb}_{0.5}[(\text{UO}_2)_8\text{O}_4(\text{OH})_{10}] \cdot 10\text{H}_2\text{O}$, is a new uranyl-oxide hydroxyl-hydrate mineral found underground in the Svornost mine, Jáchymov, Czechia. Electron-probe microanalysis (WDS) provided the empirical formula $(\text{K}_{1.28}\text{Na}_{0.07})_{\Sigma 1.35}(\text{Pb}_{0.23}\text{Cu}_{0.14}\text{Ca}_{0.05}\text{Bi}_{0.03}\text{Co}_{0.02}\text{Al}_{0.01})_{\Sigma 0.48}[(\text{UO}_2)_{7.90}(\text{SO}_4)_{0.04}\text{O}_{4.04}(\text{OH})_{10.00}] \cdot 10\text{H}_2\text{O}$, on the basis of 40 O atoms apfu. Sheets in the crystal structure of kroupaite adopt the fourmarierite anion topology, and therefore kroupaite belongs to the schoepite-family of minerals with related structures differing in the interlayer composition and arrangement, and charge of the sheets. Uptake of dangerous radionuclides (⁹⁰Sr or ¹³⁵Cs) into the structure of kroupaite and other uranyl-oxide hydroxy-hydrate is evaluated based on crystal-chemical considerations and Voronoi-Dirichlet polyhedra measures. These calculations show the importance of these phases for the safe disposal of nuclear waste.

Keywords: Kroupaite, new mineral species, uranyl-oxide hydroxy-hydrate, crystal structure, Voronoi-Dirichlet polyhedral, ¹³⁵Cs, ⁹⁰Sr; Jáchymov

INTRODUCTION

Uranium dioxide, as nuclear fuel or uraninite (Janeczek et al. 1999), UO_{2+x} , readily reacts with oxygen and water to form a fascinating family of uranyl-oxide hydroxyl-hydrates (UOHs) (Finch and Ewing 1991; Wronkiewicz et al. 1996; Plášil 2014). These occur in nature as minerals and are among the first alteration products that form during weathering of uraninite in oxidized zones of U deposits worldwide (Finch et al. 1996a, 1996b; Plášil 2018a). They are of interest in forensic studies of intercepted illicit nuclear materials as they provide insights into uranium oxide history. Several studies have focused on their structures, solubilities, and thermodynamic stabilities (Casas et al. 1997; Finch and Murakami 1999; Kubatko et al. 2006a; Klingensmith et al. 2007; Gorman-Lewis et al. 2008; Kirkegaard et al. 2019), due to their general importance in nuclear waste disposal and the environmental chemistry of uranium.

The onset of oxidation and hydration of uranium oxide often yields phases consisting of electroneutral sheets of uranyl pentagonal bipyramids with substantial H_2O in the interlayer region, and typically little, if any, additional metal cations (Burns 2005; Krivovichev and Plášil 2013; Lussier et al. 2016; Plášil 2018a). In some cases, uranium oxide hydrates containing mixtures of U(IV), U(V), or U(VI) oxidation states occur as well. Continued alteration of uranium oxide, alteration in more chemically diverse

aqueous fluids, and alteration of geologically old uranium oxide that contains substantial radiogenic lead result in formation of uranyl-oxide hydroxy-hydrates with anionic sheets of uranyl polyhedra charge-balanced by cations in the interstitial regions of the structures.

Here we describe the new mineral kroupaite that was found underground in the Svornost (formerly “Einigkeit” in German) mine in Jáchymov, Western Bohemia, Czechia. Details of the mineralogy, geology, and history of the Jáchymov ore district can be found elsewhere (Ondruš et al. 2003; Hloušek et al. 2014). The specimens studied originate from the Jan Evangelista vein at the Daniel level of the Svornost mine. Associated minerals include fourmarierite, Na-rich metaschoepite, uranopilite, liebigite, ewingite, and gypsum. The new mineral and its assemblage are of supergene origin associated with oxidation-hydration alteration of uraninite in old mine workings. The name honors mining engineer Gustav Kroupa (1857–1935), who was employed by the state mines in Jáchymov beginning in 1886, and who as head of the mining district, approved shipment of 10 tons of leachate obtained from processing pitchblende ore to Marie-Curie Skłodowska and Pierre Curie in 1898. They went on to isolate three grams of the new substance radium chloride, and subsequently the new element radium. The Commission on New Minerals, Nomenclature and Classification of the International Mineralogical Association (IMA) approved the new mineral and name (IMA 2017-031). The description is based upon the holotype specimen deposited in the mineralogical collection of the National Museum in Prague (catalog number no. PIP 16/2017).

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Crystals used in this study are deposited in the Natural History Museum of Los Angeles County (catalog number 66572).

PHYSICAL AND OPTICAL PROPERTIES

Kroupaite forms as radial aggregates of thick platy, orange-yellow crystals up to 1 mm in diameter (Fig. 1) growing in interstices of gypsum crystals. Tablets are flattened on {100}, with the prominent crystal forms {100}, {013}, and {021} (Fig. 2). Crystals are brittle with at least one cleavage, perfect on {100} and uneven fracture. Crystals are translucent with vitreous luster, have light yellow streak, and are non-fluorescent under long-wave and short-wave ultraviolet radiation. The Mohs hardness is approximately 2, estimated by scratch tests. The density was not measured due to the limited availability of material. The calculated density is 5.058 g/cm³ based on the empirical formula. Kroupaite is readily soluble in dilute HCl, with no effervescence.



FIGURE 1. Orange yellow aggregates of kroupaite on the surface of strongly altered uraninite. Horizontal field of view is 2.5 mm (photo P. Škácha). (Color online.)

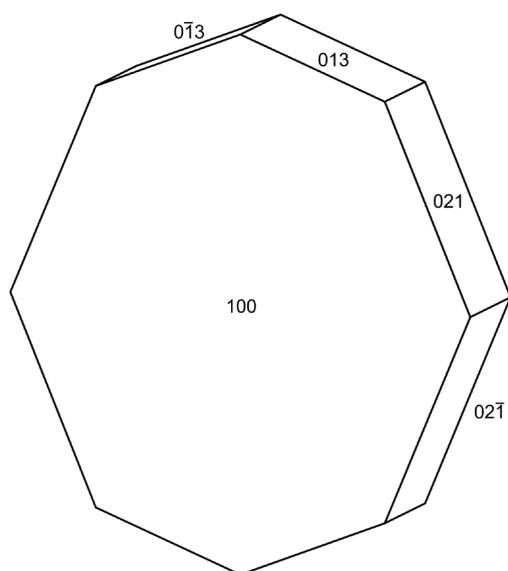


FIGURE 2. Crystal drawing of kroupaite in clinographic projection.

Kroupaite is optically biaxial (-), with $\alpha = 1.691(2)$, $\beta = 1.752(2)$, $\gamma = 1.768(2)$ (measured with white light). The $2V$ is $53(1)^\circ$, measured directly by conoscopic observation on a spindle stage; the calculated $2V$ is 52.7° . Dispersion is strong, $r > v$. The mineral is pleochroic with X colorless, Y yellow, and Z yellow; $X < Y \approx Z$. The optical orientation is $X = \mathbf{a}$, $Y = \mathbf{c}$, $Z = \mathbf{b}$. The Gladstone-Dale compatibility (Mandarino 2007), $1 - (K_p/K_c)$, is -0.018 (superior) for the empirical formula.

Raman spectroscopy

A Raman spectrum was collected in the range 4500–12 cm⁻¹ using a DXR dispersive Raman Spectrometer (Thermo-Scientific) mounted on a confocal Olympus microscope. The Raman signal was excited by a green 532 nm diode-pumped solid-state laser and was collected by a CCD detector. The experimental parameters were: 50 \times objective, 10 s exposure time, 100 exposures, 400 lines/mm grating, 50 μ m pinhole spectrograph aperture, and 1 mW laser power level. The instrument was set up by a software-controlled calibration procedure using multiple neon emission lines (wavelength calibration), multiple polystyrene Raman bands (laser frequency calibration), and standardized white-light sources (intensity calibration). Spectral manipulations as well as band-fitting were performed using the Omnic 9 software (Thermo-Scientific).

In the Raman spectrum of kroupaite (Fig. 3a) a weak broad band at 3487 cm⁻¹ is assigned to the ν O–H stretching vibrations of hydroxyl and molecular H₂O H-bonded into the structure. The approximate bond-lengths of H-bonds ($\text{H} \cdots \text{Acceptor}$) lie in the range 1.8–2.0 Å (Libowitzky 1999). The strong band centered at 833 cm⁻¹, with a shoulder at 812 cm⁻¹ (Fig. 3b), is attributed to the ν_1 symmetric stretching vibration of uranyl U–O. The splitting of the ν_1 of (UO₂)²⁺ is concomitant with four unique U sites observed in the crystal structure. Based on recent theoretical and experimental studies (Colmenero et al. 2018; Kirkegaard et al. 2019), the assignment of the vibration bands directly to ν_1 (UO₂)²⁺ is not straightforward: the component bands comprise both symmetric stretching ν_1 (UO₂)²⁺ and δ (U–OH), as well as libration vibration of (H₂O). Nevertheless, using an empirical relationship to derive the approximate U–O bond lengths from the band positions assigned to the (UO₂)²⁺ stretching vibrations gives ~ 1.78 Å (833 cm⁻¹) and ~ 1.80 Å (812 cm⁻¹) (Fig. 3b). These values are in line with U–O bond-lengths obtained from the crystal structure data (see Supplemental¹ Table S1). There is a series of weak bands in the 580–280 cm⁻¹ range (570, 542, 500, 450, 400, 328, and 298 cm⁻¹). Those at 570–500 cm⁻¹ are attributable to librations of H₂O. Those at 450–328 cm⁻¹ can be assigned to δ (O–U–O_{eq}) vibrations. According to a theoretical study of schoepite (Colmenero et al. 2018, 2020), these bands also have a significant contribution of the ν (U–O_{eq}), δ (U–OH), and libration of H₂O. The band at 298 cm⁻¹ is attributed to ν_2 (δ) (UO₂)²⁺, but there may be contributions from δ (O–U–O_{eq}), δ (U–OH), and water librations. Remaining bands located below 200 cm⁻¹ (190, 155, 116, 63, and 40 cm⁻¹) are assigned to molecular deformations and lattice modes.

Chemical analysis

Kroupaite was analyzed by electron microprobe using a Cameca SX100 electron microprobe (Masaryk University, Brno)

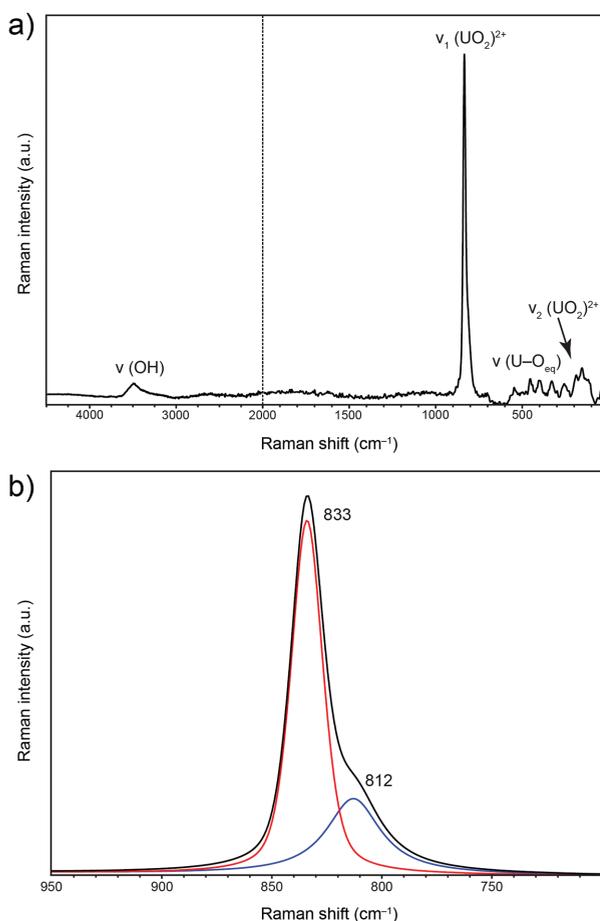


FIGURE 3. (a) Raman spectrum of kroupaite in the full range of 4500–12 cm^{-1} (split at 2000 cm^{-1}). (b) Band decomposition in the Raman spectrum of kroupaite for $\nu_1(\text{UO}_2)^{2+}$ in the region from 950–700 cm^{-1} . (Color online.)

TABLE 1. Analytical data for kroupaite (in wt%), average of six analyses

Constituent	Mean	Range	St.dev.	Probe standard	Normalized
Na_2O	0.08	0.00–0.20	0.08	albite	0.08
K_2O	2.14	1.99–2.32	0.10	sanidine	2.25
CaO	0.10	0.08–0.14	0.03	fluorapatite	0.10
PbO	1.84	1.64–2.46	0.31	vanadinite	1.93
CuO	0.41	0.00–0.72	0.28	lammerite	0.43
CoO	0.05	0.00–0.33	0.12	Co metal	0.05
Al_2O_3	0.02	0.00–0.12	0.04	sanidine	0.02
Bi_2O_3	0.25	0.00–0.51	0.19	Bi metal	0.26
UO_3	80.67	78.80–82.24	1.15	uranophane	84.64
SO_3	0.11	0.00–0.38	0.18	SrSO_4	0.12
H_2O^a	9.65				10.12
Total	95.23				100.00

^a Calculated as determined from the structure.

operating in wavelength-dispersive spectroscopy mode using an accelerating voltage of 15 kV, beam current of 4 nA, and a 10–15 μm beam diameter. Concentrations of elements other than those reported in Supplemental¹ Table S2 were below detection limits (ca. 0.03–0.10 wt%). The low analytical totals are due to an uneven surface and the porosity of the polished section; therefore, we also report normalized data (column “Norm.” in Table 1). A matrix correction was applied to the data using the

“PAP” software (Pouchou and Pichoir 1991). The H_2O content was calculated by stoichiometry (obtained from the structure); the paucity of pure material precluded a direct determination of the H_2O content. The empirical formula calculated on the basis of 40 O atoms per formula unit is: $(\text{K}_{1.28}\text{Na}_{0.07})_{\Sigma 1.35}(\text{Pb}_{0.23}\text{Cu}_{0.14}\text{Ca}_{0.05}\text{Bi}_{0.03}\text{Co}_{0.02}\text{Al}_{0.01})_{\Sigma 0.48}[(\text{UO}_2)_{7.90}(\text{SO}_4)_{0.04}\text{O}_{4.04}(\text{OH})_{10.00}] \cdot 10\text{H}_2\text{O}$. The ideal formula is $\text{K}\text{Pb}_{0.5}[(\text{UO}_2)_8\text{O}_4(\text{OH})_{10}] \cdot 10\text{H}_2\text{O}$, which requires: K_2O 1.73, PbO 4.11, UO_3 84.21, H_2O 9.95, total 100 wt%.

X-ray crystallography and structure determination

Powder X-ray diffraction data were collected using a Rigaku R-Axis Rapid II curved imaging plate microdiffractometer with monochromated $\text{MoK}\alpha$ radiation. A Gandolfi-like motion on the ϕ and ω axes was used to randomize the sample. Observed d -values and intensities were derived by profile fitting using the JADE 2010 software (Materials Data, Inc.). Data are given in Supplemental¹ Table S1. Unit-cell parameters refined from the powder data using JADE 2010 with whole pattern fitting are: $a = 14.781(7)$, $b = 14.095(6)$, $c = 16.719(7)$ \AA , $V = 3583(3)$ \AA^3 , $Z = 4$ (space group: $Pbca$).

Single-crystal X-ray diffraction data were collected at room temperature on a Rigaku SuperNova diffractometer equipped with a microfocus X-ray source ($\text{MoK}\alpha$, $\lambda = 0.71073$ \AA) and an Atlas S2 CCD detector. The crystal, $0.07 \times 0.06 \times 0.03$ mm large, was mounted on a cut microloop. The raw data reduction was done using CrysAlis software (Rigaku 2019). An absorption correction combining a Gaussian correction and an empirical scaling was applied to the data using the Jana2006 software (Petříček et al. 2014). The structure was solved with SHELXT using charge-flipping (Sheldrick 2015). Full-matrix least-squares refinement of the structure against F^2 was performed with Jana2006 (Petříček et al. 2014); the structure has been refined to $R = 0.0447$ for 2587 unique observed reflections. The crystallographic data can be found in the original CIF (as supplementary file¹); selected interatomic distances and results of the bond-valence analysis are given in Tables 2 and 3, respectively.

DESCRIPTION OF THE STRUCTURE

Kroupaite crystallizes in orthorhombic space group $Pbca$ and its structure (Fig. 4) contains 4 U sites, 1 K site, 1 Pb site, and 19 O sites. Each U site is coordinated by seven ligands (Table 2), forming pentagonal bipyramids, where the apices of each bipyramid are comprised of strongly bonded O atoms, forming the approximately linear uranyl ion, UO_2^{2+} . In the equatorial plane, each uranyl ion is bonded to five ligands, either O or OH^- (Table 3), and the polyhedra polymerize by sharing edges and equatorial vertices (Fig. 4) into the well-known fourmarierite anion sheet topology (Fig. 5) (Burns 2005; Krivovichev and Plášil 2013; Lussier et al. 2016). In the interlayer, there are two independent cation sites that are occupied by K^+ and Pb^{2+} . Both sites have occupancies lower than unity. Additionally, there are four O sites (O15, O16, O18, O19) in the interlayer corresponding to H_2O molecules (Table 3) that were identified based on the bond-valence sums incident upon the corresponding O atoms. The K atom is [7]-fold coordinated (to 3.3 \AA) and binds to five distinct O_{Ur} (Ur = uranyl) atoms. Site-scattering refinement revealed that the site is partially occupied ($\sim 0.47/0.5$). The Pb site is [9]-fold

TABLE 2. Selected interatomic distances (Å) for kroupaite

U1-O2	1.805(10)	U2-O11	1.789(11)	U3-O4	1.765(10)
U1-O7	1.799(11)	U2-O14	1.799(12)	U3-O8	1.800(10)
U1-O1 ⁱ	2.231(9)	U2-O1	2.222(8)	U3-O6	2.413(9)
U1-O6	2.693(10)	U2-O10 ⁱⁱⁱ	2.548(9)	U3-O9	2.451(9)
U1-O10 ⁱⁱⁱ	2.460(8)	U2-O12 ⁱⁱⁱ	2.428(10)	U3-O11	2.533(9)
U1-O13	2.254(8)	U2-O18 ⁱⁱ	2.312(9)	U3-O12	2.224(9)
U1-O22	2.434(9)	U2-O22	2.445(9)	U3-O16	2.313(9)
<U1-O _{Ur} >	1.80	<U2-O _{Ur} >	1.79	<U3-O _{Ur} >	1.78
<U1-O _{eq} >	2.41	<U2-O _{eq} >	2.39	<U3-O _{eq} >	2.39
U4-O3	1.791(12)	Pb1-O4 ⁱⁱⁱ	2.971(11)	K1-O4 ⁱⁱⁱ	3.201(18)
U4-O5	1.797(10)	Pb1-O5 ^v	2.804(11)	K1-O6 ⁱⁱⁱ	2.902(18)
U4-O1	2.252(8)	Pb1-O7 ^v	3.025(11)	K1-O8 ⁱⁱ	3.201(18)
U4-O6 ^{iv}	2.410(9)	Pb1-O7 ^w	3.102(11)	K1-O15	2.86(2)
U4-O11	2.471(10)	Pb1-O8 ^v	2.803(11)	K1-O16 ⁱⁱ	3.28(2)
U4-O12	2.253(9)	Pb1-O10	2.732(11)	K1-O17	2.86(2)
U4-O19	2.538(9)	Pb1-O14	2.462(14)	K1-O18	2.69(3)
<U4-O _{Ur} >	1.79	Pb1-O14 ^{vi}	3.036(14)	<K1-O>	3.00
<U4-O _{eq} >	2.39	Pb1-O18 ^{vii}	3.006(16)		
		<Pb1-O>	2.88		

Note: Symmetry codes: (i) $-x+3/2, y-1/2, z$; (ii) $-x+3/2, -y+1, z-1/2$; (iii) $x, -y+3/2, z-1/2$; (iv) $-x+3/2, y+1/2, z$; (v) $x-1/2, -y+3/2, -z+1$; (vi) $-x+1, -y+2, -z+1$; (vii) $-x+1, -y+1, -z+1$; (viii) $-x+1, y+1/2, -z+3/2$; (ix) $x, -y+3/2, z+1/2$; (x) $x+1/2, -y+3/2, -z+1$; (xi) $x+1/2, y, -z+3/2$; (xii) $-x+3/2, -y+1, z+1/2$.

coordinated (to 3.3 Å); six of the ligands are O_{Ur} atoms from adjacent structural sheets, with three from each sheet, and thus the Pb cations directly bridge between sheets. There are dimers of Pb polyhedra; one Pb-polyhedron is linked to its symmetrical equivalent through the pair of symmetrically related O16(H₂O) atoms to form Pb₂O(O_{Ur})₁₀(H₂O)₃ dimers.

According to the bond-valence analysis and site-scattering refinement, the formula, assuming full metal-cation site occupancy for K (0.94 K from the site-scattering refinement) and 0.5 Pb (0.44 from refinement) and full occupancies of the O(H₂O) sites, is K_{0.94}Pb_{0.5}[(UO₂)₈O₄(OH)₁₀]·8H₂O, Z = 4, although the H₂O content is likely somewhat lower.

RELATIONSHIP TO OTHER UOH MINERALS AND COMPOUNDS

The structural unit in kroupaite is the well-known fourmarierite-type sheet, which accommodates various combinations

TABLE 3. The bond-valence analysis for kroupaite^a

	U1	U2	U3	U4	Pb1 ^b	K1 ^b	ΣBV _{anions}	Assignment
O1	0.68	0.69		0.65		2.01		O
O2	1.66					1.66		O
O3				1.71		1.71		O
O4			1.81		0.12	0.06	1.99	O
O5				1.69	0.17		1.87	O
O6	0.25		0.46	0.46		0.12	1.29	OH
O7	1.69				0.19		1.88	O
O8			1.68		0.17	0.06	1.91	O
O9	0.42	0.35	0.42				1.19	OH
O10		1.72			0.21		1.93	O
O11		0.45	0.36	0.41			1.21	OH
O12	0.64		0.69	0.65			1.98	O
O13		1.69					1.69	O
O14					0.48		0.48	H ₂ O
O15						0.13	0.13	H ₂ O
O16		0.57	0.57			0.05	1.18	OH
O17						0.13	0.13	H ₂ O
O18					0.11	0.20	0.31	H ₂ O
O19	0.44	0.43		0.35			1.22	OH
ΣBV _{cations}	5.78	5.89	5.99	5.92	1.46	0.73		

Note: ΣBV = sum of the bond-valences; bond-valence parameters were taken from Gagné and Hawthorne (2015) and from Burns et al. (1997).

^a All values are in valence units (v.u.).

^b Site with a reduced occupancy.

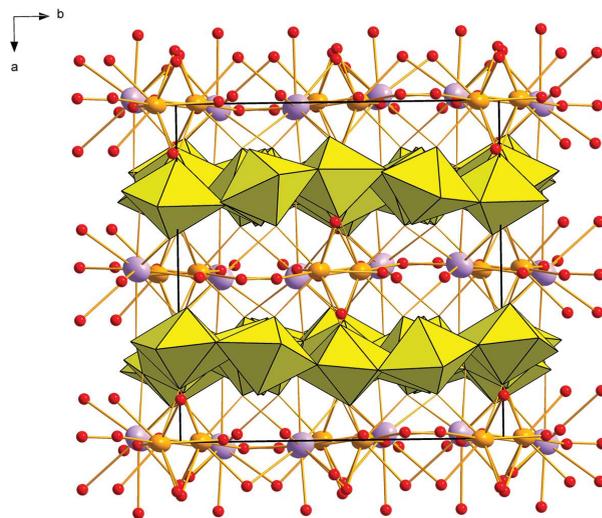


FIGURE 4. Crystal structure of kroupaite viewed down [001]. The uranyl-oxide hydroxide sheets (in yellow) alternate with the interlayer containing water oxygen (red), potassium (lavender), and lead (orange). Unit-cell edges are outlined by black-solid lines. (Color online.)

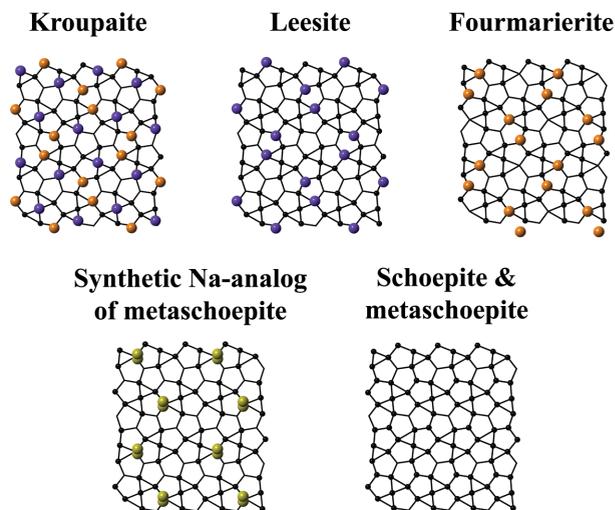


FIGURE 5. Comparative view of the anion sheet topologies and OH⁻ distributions for uranyl-oxide hydroxide-hydrate minerals with the fourmarierite topology. Black circles highlight vertices containing OH⁻, and bare vertices represent O²⁻. Orange spheres represent Pb²⁺, blue K⁺, and green Na⁺ atoms, respectively. Figure adapted from Klingensmith et al. (2007). (Color online.)

of OH⁻ and O in uranyl minerals, and thus has variable charge. Electroneutral sheets with composition [(UO₂)₄O(OH)₆] occur in schoepite and metaschoepite (Weller et al. 2000; Plášil 2018b), whereas anionic sheets with composition [(UO₂)₄O₂(OH)₅]⁻ occur in synthetic Na-bearing metaschoepite (Klingensmith et al. 2007) and leesite (Olds et al. 2018), and those with composition [(UO₂)₄O₃(OH)₄]²⁻ occur in fourmarierite (Li and Burns 2000a).

Lead cations in the structure of kroupaite occupy the same site as Pb²⁺ in fourmarierite, but surprisingly, also the same site as K⁺ in leesite (Fig. 5). In the structure of kroupaite, K atoms

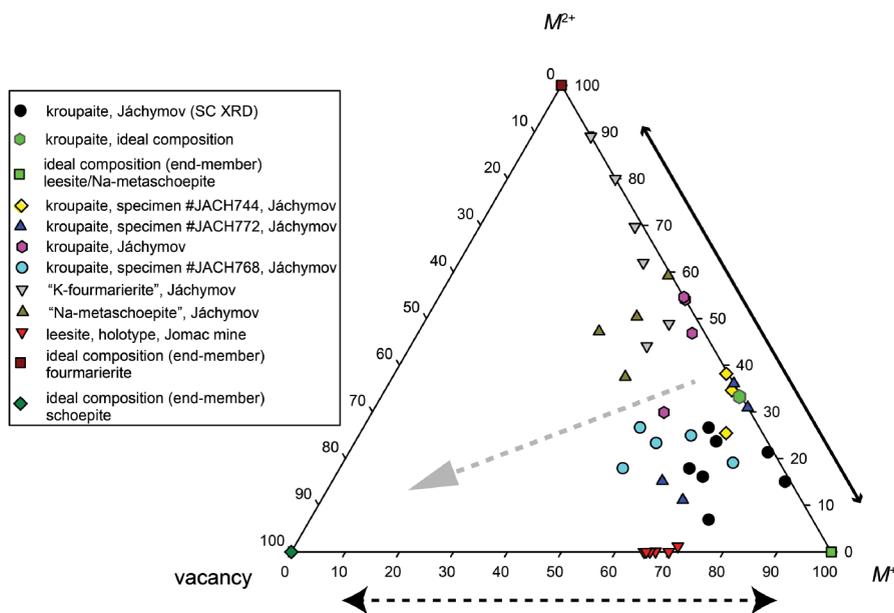


FIGURE 6. Ternary compositional plot for chemical analyses of kroupaite and related minerals. Analyses from additional set of kroupaite samples (labeled as JACH) are displayed to illustrate chemical substitutional trends. $M^+ \leftrightarrow$ vacancy (with black dashed line): variability in composition between leesite (end-member) and schoepite; $M^+ \leftrightarrow M^{2+}$ (black solid line): variability between leesite (end-member) and fourmarierite; the gray arrow points toward the substitution characteristic for intermediate series members and schoepite. (Color online.)

occupy the site adjacent to the dimeric Pb polyhedral units. The different behaviors of K and Pb in the structures of kroupaite and leesite are well documented by distinct substitution trends between kroupaite and fourmarierite (characteristic for the same Pb sites) and leesite (Fig. 6). The substitution in leesite should take place at the single cationic site for Pb^{2+} and K^+ . The main structural distinction of kroupaite from leesite is a unique K^+ site in kroupaite (Fig. 5). It appears that in the presence of Pb^{2+} with a stereoactive lone pair of electrons, K^+ is favored at a site that provides more space and, consequently, K atoms shift to a position beneath bounding O_{Ur} atoms. The corresponding Voronoi-Dirichlet polyhedral values that characterize particular coordination environments of metal cations in the interlayers of kroupaite, leesite, fourmarierite (Fig. 7) and synthetic Na-metaschoepite are given in Supplemental Table S3. Comparing Lewis acid (LA) strengths, Pb^{2+} is a much stronger acid (0.22 v.u.) than K^+ (0.11 v.u.). Both kroupaite and leesite contain similar amounts of H_2O in their interlayers (kroupaite is slightly more hydrated) and the arrangement of $(OH)^-$ in the kroupaite sheet is identical to that found both in leesite and synthetic Na-metaschoepite. The consequence is that Pb adopts a site in the kroupaite structure that is more compatible with the distribution of higher bond-valence from Lewis acids to Lewis bases; in kroupaite the average $Pb^{2+}-O$ bond-strength is 0.16 v.u. while that of K^+-O is 0.10 v.u. Acceptors of the majority of bonds from Pb^{2+} in kroupaite are apical uranyl atoms within the sheets.

Uranyl-oxide hydroxy-hydrates with various interlayer cations

The interstitial complexes of uranyl-oxide hydrates incorporate various elements with distinct stereochemistry. Uranyl

minerals form in complex multiphase chemical conditions arising from their geological settings (and geochemistry) and are also expected to form in complex environments such as underground repositories for long-term storage of nuclear (Maher et al. 2013; Ewing 2015).

The structures and compositions of uranyl-oxide hydrates have recently been reviewed (Plášil 2018a). Crystal structures of uranyl-oxide hydrates sometimes contain U(V) or U(IV), with U(V) observed in structures containing $\beta-U_3O_8$ (Burns and Finch 1999) and $\alpha-U_3O_8$ (Plášil 2017a) types of uranyl-oxide layers. In nollmotzite, $Mg[U^V(U^{VI}O_2)_2O_4F_3] \cdot 4H_2O$, the $\beta-U_3O_8$ type of sheet contains fluorine as well as oxygen (Plášil et al. 2018).

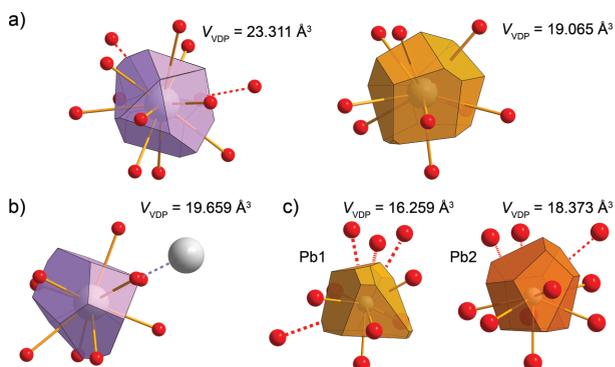


FIGURE 7. Voronoi-Dirichlet polyhedra (VDP) for interlayer cations in selected structures with corresponding VDP volumes (V_{VDP}): (a) kroupaite, K1 atom (lavender); Pb1 atom (orange); (b) leesite; K1 atom (lavender); (c) fourmarierite. (Color online.)

The interstitial complexes of uranyl oxide hydrates incorporate various alkali and alkaline earth cations as well as lanthanides (Hill and Burns 1999; Burns and Hill 2000a, 2000b; Cahill and Burns 2000; Zhang et al. 2018, 2019). The capacity of uranyl-oxide hydrates to accommodate cations of various Lewis-acid strengths arises in part from the heterogeneous distribution of different types of anions within the sheets: uranyl O atoms, which are somewhat undersaturated with respect to their bond-valence requirements, and OH⁻ groups within the uranyl-oxide layers that are bond-valence donors. These sheets readily accommodate cations of distinct charges and radii (Zhang et al. 2016), and also of different stereochemistry (Olds et al. 2017). In comparison, kamitugaite, PbAl[(UO₂)₅(PO₄)_{2.38}(AsO₄)_{0.62}O₂(OH)₂](H₂O)_{11.5} (Plášil 2017b) combines divalent and trivalent cations in its interstitial complexes, and the Pb²⁺ is electron lone-pair stereoactive. The distribution of anions appears to preclude occurrence of both Pb²⁺ and Al³⁺ in the same interlayer. Thus, there are two distinct interlayers in kamitugaite, giving a large unit cell.

Voronoi-Dirichlet polyhedra (VDP) calculations (Blatov 2004) were used to evaluate and quantify bonding environments in the interlayer regions of UOHs. The VDP calculations are summarized in Supplemental¹ Table S3 and selected aspects are displayed in Figure 8. Generally, Pb²⁺ occupies sites with VDP volume (V_{VDP}) $\sim 18 \text{ \AA}^3$. If there is an additional cation with a larger ionic radius, as K⁺ in gauthierite and kroupaite, it occupies sites with $V_{\text{VDP}} > 20 \text{ \AA}^3$. In leesite, the K⁺ occupies a site with $V_{\text{VDP}} > 19.66 \text{ \AA}^3$ that is populated by Pb²⁺ in other uranyl-oxide-hydrate structures. The structure of gauthierite is particularly interesting as it contains four symmetrically independent partially occupied K sites. Site K2 has $V_{\text{VDP}} \sim 27 \text{ \AA}^3$.

TABLE 4. Ranges in charge-densities for most common topological types of UOH structural units

Topology	Charge density range (eÅ ⁻³)	Range in Lewis basicity (v.u.)
α -U ₃ O ₈	2.23×10^{-3} to 18.23×10^{-3}	0.14–0.23
β -U ₃ O ₈	3.84×10^{-3} to 11.09×10^{-3}	0.12–0.24
Fourmarierite	2.72×10^{-3} to 6.83×10^{-3}	0.11–0.23

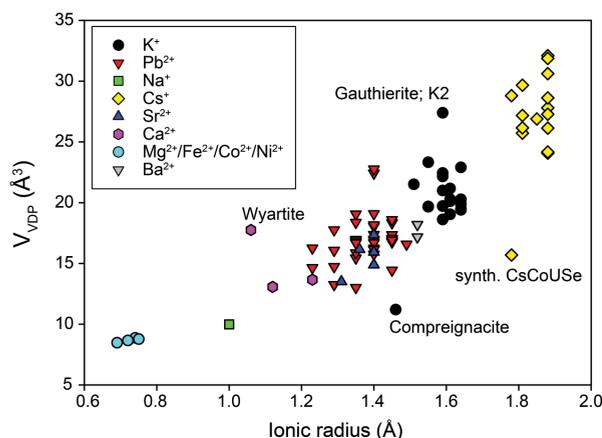


FIGURE 8. The size of cation polyhedra in the interlayers of uranyl-oxide hydroxy-hydrate structures: the volume (V_{VDP}) of Voronoi-Dirichlet polyhedra vs. the ionic radius. Outliers are labeled. (Color online.)

Potential Cs⁺ and Sr²⁺ incorporation

Voronoi-Dirichlet polyhedra calculations for uranyl-oxide-hydrate structures can help in predicting incorporation of radio-nuclides of concern for nuclear waste disposal, such as ¹³⁵Cs ($t^{1/2} = 2.3 \text{ MY}$) or ⁹⁰Sr ($t^{1/2} = 28.8 \text{ Y}$) that are important for long-term disposal and shorter-term heat generation, respectively (Maher et al. 2013; Ewing 2015). VDP calculations are sensitive to the size of the corresponding cation and can be employed to determine characteristic volumes of corresponding cation polyhedra in uranyl-oxide-hydrate structures. Results of the analysis are given in Supplemental¹ Table S3 and Figure 8, where bonding properties of interlayer cations in most uranyl-oxide-hydrate structures based on VDP volume and corresponding ionic radii (after Shannon 1976) are listed. The ionic radii of Cs⁺ and Sr²⁺ are 1.81 and 1.36 Å, respectively, and Sr²⁺ readily substitutes for Pb²⁺ and Ca²⁺, as in agrinierite (Cahill and Burns 2000). Substitutions of Sr²⁺ for Pb²⁺ and Ca²⁺ has been documented for synthetic UOHs related to curite and becquerelite (Burns and Hill 2000a; Burns and Li 2002). Cesium is less likely to be incorporated into the interlayers of UOHs structures, although a synthetic uranyl oxide hydrate containing Cs has been reported (Hill and Burns 1999) as well as uptake of Cs⁺ by a uranyl oxide hydrate during crystallization (Giammar and Hering 2004). It is plausible that Cs⁺ can be incorporated in K-bearing UOHs, as the V_{VDP} of K⁺ sites reaches $\sim 24 \text{ \AA}^3$ (with an extreme value of $\sim 27 \text{ \AA}^3$ in the case of K2 in gauthierite; Table 4).

Charge-density match in uranyl-oxide-hydrate structures

We used charge density calculations to identify mismatches in UOHs by modifying an approach used earlier for uranyl germanates and uranyl silicates (Li et al. 2018). The charge density ρ associated with the anionic structural units was calculated as $\rho = q_e \times Z/V$. Here q_e is the effective charge of the structural unit, which is the formal charge q_f of the structural units modified by the number of hydrogen bonds, $q_f + h \times 0.2$ (where h is the number of hydrogen atoms in the structural unit and 0.2 v.u. is the assumed bond-strength of the corresponding H bond). Z is the number of formula units in each unit cell, V is the unit-cell volume (\AA^3), and ρ is then the charge density associated with the structural unit. The charge density of the interlayer complex is calculated in the same way, taking into account the formal charge of the interlayer complex modified by the H-bonds emanating from it (Supplemental¹ Table S4). The majority of UOHs structures exhibit an excess of charge density associated with the interlayer complex (Fig. 9). Exceptions are the denser (polymerized) dehydrogenated structures such as for curite and spriggite. The outlying value of the synthetic PbUOH phase (Li and Burns 2000b) is due to the density of the bond-valence acceptors within the framework as compared to the relatively simple complex occupying the channels. The high charge density of the REE^{III}-containing UOHs is associated with structural units of the α -U₃O₈ topology that are highly versatile. The variation of the charge densities for the α -U₃O₈ type sheet is the largest within the most common topological types (Table 4).

IMPLICATIONS

The new K,Pb-bearing uranyl-oxide hydroxy-hydrate kroupaite is particularly interesting due to ordering of monovalent and

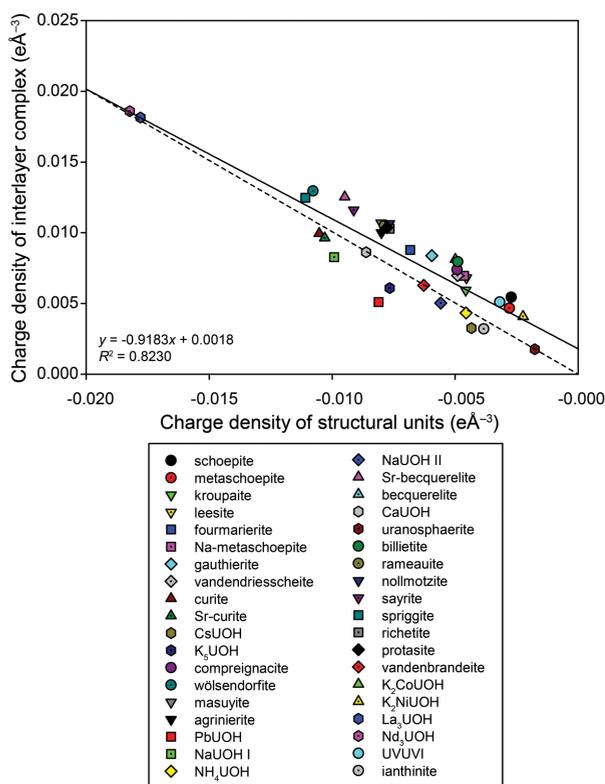


FIGURE 9. Charge-density matches in uranyl-oxide hydrate structures. The black solid line represents a linear fit to the data (equation and regression statistics given), and the dashed line represent an ideal match; $a = -1$, $b = 0$. (Color online.)

divalent cations of different stereochemistry in the interlayer region. Minerals provide unique insights into crystal chemical features that may be difficult to study via laboratory synthesis. Recent observations of natural samples, including kroupaite, leesite, and gauthierite from several localities demonstrate that uranyl-oxide-hydrate sheet anion topologies readily accommodate a range of heterovalent cations via unique configurations of their interlayers. Some uranyl-oxide-hydrate structures investigated here were found, based on analysis of their corresponding Voronoi-Dirichlet polyhedra, to be suitable for incorporation of large monovalent cations such as Cs⁺.

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Endnote:

¹Deposit item AM-20-47311, Supplemental tables and CIF. Deposit items are free to all readers and found on the MSA website, via the specific issue's Table of Contents (go to http://www.minsocam.org/MSA/AmMin/TOC/2020/Apr2020_data/Apr2020_data.html).