# Bi-Sb energetics in sulfosalts and sulfides

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### ABSTRACT

Experimental brackets (300–450°C) on Sb-Bi partitioning between stibnite-bismuthinites (Sb,Bi)<sub>2</sub>S<sub>3</sub> and sulfosalts in the AgSbS<sub>2</sub>–AgBiS<sub>2</sub> binary subsystem ( $\alpha$ -Ag(Sb,Bi)S<sub>2</sub>,  $\beta$ -Ag<sub>5</sub>(Sb,Bi)<sup>4</sup><sub>4</sub>(Sb,Bi)<sup>II</sup>S<sub>10</sub>) and extant constraints are used to define mixing properties and standard state Gibbs energies of Sb-Bi exchange reactions. They are also used to construct a phase diagram for Ag(Sb,Bi)S<sub>2</sub> sulfosalts. We infer that the non-ideality associated with Sb-Bi mixing is largest in minerals of the  $\beta$ -Ag<sub>5</sub>(Sb,Bi)<sup>4</sup><sub>4</sub>(Sb,Bi)<sup>II</sup>S<sub>10</sub> series, and is sufficient to produce miscibility gaps between an ordered intermediate species Ag<sub>5</sub>(Sb)<sup>4</sup><sub>4</sub>(Bi)<sup>II</sup>S<sub>10</sub> and Sb- and Bi-end-members at  $T < 240^{\circ}$ C (measured in terms of symmetric regular-solution-type parameters  $\frac{1}{4}W_{BI-Sb}^{II} = W_{BI-Sb}^{II} \sim 8.5 \text{ kJ/gfw}$ ). The non-ideality associated with the Sb-Bi substitution in stibnite-bismuthinite and  $\alpha$ -Ag(Sb,Bi)S<sub>2</sub> is  $\approx$  70% that in the Ag<sub>5</sub>(Sb,Bi)<sup>4</sup><sub>4</sub>(Sb,Bi)<sup>II</sup>S<sub>10</sub> series (W\_{BI-Sb}^{BS} \approx 12.0 \text{ kJ/gfw}; W\_{BI-Sb}^{\alpha} \approx 6.0 \text{ kJ/gfw}). It is insufficient to produce exsolution at temperatures of ore deposition ( $T > T_c \approx 88^{\circ}$ C), but most likely is responsible for a preponderance in molar Sb/Bi ratios towards end-member compositions. Finally, positive Gibbs energies of the Sb-Bi exchange reactions

 $\begin{array}{l} \frac{1}{2}Bi_2S_3 + AgSbS_2 = AgBiS_2 + \frac{1}{2}Sb_2S_3 \ (\Delta\bar{G}^{BS-\alpha}_{Bi-Sb} \approx 2.70 \ kJ/gfw) \\ \text{and} \qquad \frac{1}{2}Bi_2S_3 + \frac{1}{5}Ag_5Sb_5S_{10} = \frac{1}{5}Ag_5Bi_5S_{10} + \frac{1}{2}Sb_2S_3 \ (\Delta\bar{G}^{BB-\beta}_{Bi-Sb} \approx 4.89 \ kJ/gfw) \\ \text{indicate that Bi is more compatible in stibuite-bismuthinite sulfides than in } Ag(Sb,Bi)S_2 \ sulfosalts. \end{array}$ 

**Keywords:** bismuthinite-stibnites,  $Ag(Sb,Bi)S_2$  sulfosalts, Sb-Bi energetics, ordering and exchange reactions.

#### Introduction

ANTIMONY- and Bi-rich sulfides and sulfosalts with compositions approximating those in the Ag<sub>2</sub>S– Sb<sub>2</sub>S<sub>3</sub>–Bi<sub>2</sub>S<sub>3</sub> system (stibnite-bismuthinites, (Sb,Bi)<sub>2</sub>S<sub>3</sub>; miargyrite, Ag(Sb,Bi)S<sub>2</sub>,  $X_{Bi} \approx 0.0$ ; aramayoite, Ag(Sb,Bi)S<sub>2</sub>,  $0.17 \leq X_{Bi} \leq 0.35$ ; matildite, Ag(Bi,Sb)S<sub>2</sub>,  $X_{Bi} \approx 1.0$ ) are common constituents in polymetallic hydrothermal sulfide ore deposits of epithermal-mesothermal vein type (e.g. Bartos, 1990; Boldyreva, 1970; Borodayev *et al.*, 1986; Brooker and Jaireth, 1995; Bussell *et al.*, 1990; Ruvalcaba-Ruiz and Thompson, 1988; Czamanske and Hall, 1975; Gibson *et al.*, 1990; Gilmer *et al.*, 1988; Goodell, 1974; Goodell and Petersen, 1974; Gröpper *et al.*, 1991; Hayase, 1955; Jeppson, 1987; Johnson and Meinert, 1994; Kelly and Turneaure, 1970; Lueth, 1988; Lueth et al., 1990; Petersen et al., 1977; Petruk, 1968; Sillitoe et al., 1975; Springer, 1969; Stone, 1959; Turneaure, 1971). Among these minerals, bismuthinite-stibnites exhibit distinct compositional variations along flow paths of mineralizing fluids in ore deposits that are characterized by preponderances of molar Bi/(Bi+Sb) ratios near the end-members, with a conspicuous paucity of intermediate compositions (Fig. 1). Such a pattern of molar semi-metal ratios is suggestive of significant non-ideality of Sb-Bi mixing in bismuthinite-stibnites (e.g. Ghosal and Sack, 1995). Previous workers (e.g. Lueth et al., 1990) have attributed such variations in molar Bi/(Bi+Sb) ratios to a process referred to as 'semi-metal boiling', whereby preferential volatilization of antimony from the ore fluid at a point along the flow path is held responsible for the sudden change

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FIG. 1. Histogram of number of analyses (# Analyses) vs molar Bi/(Bi + Sb) ratios  $(X_{Bi}^{BS})$  of bismuthinite-stibnites taken from compilations of Springer (1969) and Lueth (1988).

in bismuthinite-stibnite Bi/Sb ratios. However, a similar pattern of semi-metal abundance ratios is observed in the argentian sulfosalt pyrargyrite-proustite ( $Ag_3(As,Sb)S_3$ ), and is due to non-ideality of As-Sb mixing (Ghosal and Sack, 1995).

In this study, we conducted experiments to characterize Sb-Bi partitioning between bismuthinite-stibnites and solid solutions near the AgSbS<sub>2</sub>-AgBiS<sub>2</sub> binary at 300, 350, 400 and 450°C. We have used these brackets, as well as available constraints on phase equilibria in the AgSbS<sub>2</sub>-AgBiS<sub>2</sub> subsystem (Keighin and Honea, 1969; Chang *et al.*, 1977; Van Hook, 1960), to determine the non-idealities of Sb-Bi mixing in sulfides and sulfosalts in the AgSbS<sub>2</sub>-AgBiS<sub>2</sub>-Sb<sub>2</sub>S<sub>3</sub>-Bi<sub>2</sub>S<sub>3</sub> quadrilateral subsystem. We also construct a *T-X* diagram for the AgSbS<sub>2</sub>-AgBiS<sub>2</sub> binary (Fig. 3) consistent with extant constraints on miscibility gaps and two-phase regions.

# **Systematics**

Stibnite-bismuthinites (*Pbnm*; Klein and Hurlbut Jr., 1971) exhibit complete solid solubility in Sb-Bi at temperatures  $\ge 200^{\circ}$ C (Springer and LaFlamme, 1971). The minerals approximating the AgSbS<sub>2</sub>-AgBiS<sub>2</sub> binary subsystem, miargyrite, aramayoite, and matildite, exhibit limited solid solution at temperatures of ore deposition

(~200-300°C). However, at higher temperatures (~380°C, AgSbS<sub>2</sub>, Keighin and Honea (1969); 195°C, AgBiS<sub>2</sub>, Van Hook, (1960)) they undergo polymorphic transitions to a galena-like facecentred cubic structure which forms an isomorphous series across the AgSbS2-AgBiS2 binary join (e.g. Graham, 1951). The structures of all three low-temperature polymorphs are similar, being based on a galena-like layering of alternate S and Ag-Sb-Bi layers of atoms, and can be described in terms of pseudo-cubic sublattices with near-identical cell-edge lengths (Graham, 1951). More recent structure refinements of the low-temperature forms (Knowles, 1964; Mullen and Nowacki, 1974) describe statistical superstructures based on rock-salt-type substructures that differ from earlier structural estimations in their finer details, but these details are suspect because of the high R values in their calculations (12-13%) and because of the difficulty in distinguishing between Ag and Sb atoms by X-ray analysis deriving from their similar scattering properties (Knowles, 1964). The Ag and semi-metal atoms in the low-temperature structures are ordered into separate sites, resulting in a lowering of symmetry with respect to the high-temperature cubic structure (Graham, 1951). Additionally, the semi-metals atoms in the aramayoite (~Ag<sub>5</sub>Sb<sub>4</sub>BiS<sub>10</sub>, Chang et al., 1977) structure appear to exhibit long-range ordering into two types of semi-metal sites. Based on arguments derived from analysis of the phase equilibria (e.g. Fig. 3), we have assumed that endmember 'aramayoite' has the formula  $Ag_5Sb_4BiS_{10}$  rather than the formula Ag<sub>6</sub>Sb<sub>5</sub>BiS<sub>12</sub> suggested by Graham (1951). In contrast, the high-temperature cubic polymorph has a completely disordered arrangement of the Ag, Sb and Bi atoms within the metal-semi-metal layer (Graham, 1951). The close similarity between the low-temperature structures is consistent with their treatment as a continuous solid solution (referred to as  $\beta$ -Ag<sub>5</sub>(Sb,Bi)<sub>5</sub>S<sub>10</sub> in this study), with immiscibility and the existence of a strongly ordered compound on the AgSbS<sub>2</sub>-AgBiS<sub>2</sub> binary join (i.e. aramayoite; Ag<sub>5</sub>Sb<sub>4</sub>BiS<sub>10</sub>) narrowing the ranges of Sb-Bi solubility at the temperatures of deposition. This low-temperature (non-cubic) solid solution inverts to the high-temperature (cubic) solid solution (referred to as α-Ag(Sb,Bi)S<sub>2</sub>) at temperatures of 195–380°C, with the inversion involving a complete disordering of the Ag, Sb and Bi atoms (Graham, 1951).

#### Experimental

The Sb-Bi exchange experiments (evacuated silica tubes;  $300-450^{\circ}$ C) were conducted between bismuthinite-stibnites and solid solutions in the AgSbS<sub>2</sub>-AgBiS<sub>2</sub> subsystem. The starting materials were synthesized from stoichiometric proportions of the pure elements (99,999% Ag shot, 99.999% Sb ingot, 99.9995% S pieces, 99.999% Bi ingot) which were heated in evacuated silica tubes to temperatures above the liquidus. The melts were then quenched and annealed at a temperature (500°C) below the solidus (519-801°C) for 1-2 weeks. Quenched products were characterized with a CAMECA SX-50 electron microprobe and a SIEMENS D500 X-ray diffractometer. Phases in the AgSbS<sub>2</sub>-AgBiS<sub>2</sub> subsystem homogenized after one such run. However, the bismuthinite-stibnites used in this study had to be re-ground and reannealed three times (1-2 weeks for each run) to attain homogeneity in these products, contrary to the claims of earlier workers (Springer and Laflamme, 1971) that homogeneity could be achieved at 500°C in a few days. The exchange experiments were conducted as described in Ghosal and Sack (1995), with tiny grains of solid solutions in the AgSbS<sub>2</sub>-AgBiS<sub>2</sub> system immersed in substantially larger volumes of finely ground bismuthinite-stibnite in each experiment (Table 1). The experiments were annealed at 300-450°C for 2-4 months and then quenched. The quenched products were mounted in coldsetting epoxy and then polished using 3  $\mu$  alumina powder and 1 µ diamond paste. The final composition of the Ag(Sb,Bi)S<sub>2</sub> grain was analysed using a CAMECA SX-50 electron microprobe (20 kV, 10 na,  $1-10 \mu$  beam-size). The standards used were synthetic AgSbS<sub>2</sub> (Ag, Sb, S) and AgBiS<sub>2</sub> (Bi). The analytical precision of the analyses  $(\sqrt{N}/N; N = \text{counts})$ , determined from Poisson statistics of counts on standards, was <0.5% for all elements. Based on microprobe analyses of internal standards, we believe that analyses are accurate to better than +2% for elements present in concentrations >3 wt%.

# **Experimental results**

The results of the Sb-Bi exchange experiments between bismuthinite-stibnites and solid solutions in the AgSbS<sub>2</sub>-AgBiS<sub>2</sub> subsystem (i.e.  $\alpha$ - and  $\beta$ -Ag(Sb,Bi)S<sub>2</sub>) at 300 and 450°C (Table 1) are plotted as brackets on the apparent configurational

energy of the exchange reaction  $RTlnK_D$ 

(where 
$$\operatorname{RTln} K_D = \frac{(1 - X_{\text{Bi}}^{\Phi})}{X_{\text{Bi}}^{\Phi}} \frac{X_{\text{Bi}}^{\text{BS}}}{(1 - X_{\text{Bi}}^{\text{BS}})};$$

where  $\Phi \equiv \alpha$ - or  $\beta$ -Ag(Sb,Bi)S<sub>2</sub>; BS  $\equiv$ bismuthinite-stibnite) against molar Bi/(Bi + Sb) ratios in bismuthinite-stibnite (Fig. 2). The reversal brackets on RTlnK<sub>D</sub> for the  $\alpha$ -Ag(Sb,Bi)S<sub>2</sub> solution indicate limited partitioning of Sb and Bi between  $\alpha$ -Ag(Sb,Bi)S<sub>2</sub> and bismuthinite-stibnites for  $X_{Bi}^{BS} \leq 0.5$  at 450°C, and  $\geq 0.6$  at 300°C. In contrast, the



FIG. 2. Apparent configurational Gibbs energies

(RTln
$$K_D$$
;  $K_D = \frac{(1 - X_{\text{Bi}}^{\Phi})}{X_{\text{Bi}}^{\Phi}} \frac{X_{\text{Bi}}^{\text{BS}}}{(1 - X_{\text{Bi}}^{\text{BS}})};$ )

of Sb-Bi exchange reactions between bismutinitestibnites (BS) and  $\alpha$ - and  $\beta$ -Ag(Sb,Bi)S<sub>2</sub> solid solutions ( $\Phi$ ) as functions of the molar Bi/(Bi+Sb) ratios of bismutinite-stibnites  $(X_{Bi}^{BS})$ . Empty and filled squares, ellipses with vertical major axes and rhombi represent 450, 400 and 300°C brackets on Sb-Bi partitioning between bismutinite-stibuites and  $\alpha$ -Ag(Sb,Bi)S<sub>2</sub> solid solutions (empty symbols represent brackets for which  $RTlnK_D$  decreased during experiment). Circles and ellipses with horizontal major axes represent 300 and 350°C brackets on Sb-Bi partitioning between bismutinite-stibnites and  $\beta$ -Ag(Sb,Bi)S<sub>2</sub> solid solutions. Labelled curves give values of  $RTlnK_D$  calculated using equations 7 and 13 for the parameters given in Table 2. Arrows indicate direction of change in  $RTlnK_D$  during the experiments.



FIG. 3. Temperature-composition (T-X) diagram for the AgSbS<sub>2</sub>-AgBiS<sub>2</sub> subsystem. Filled *rhombi* represent mixtures that homogenized on annealing (Chang *et al.*, 1977). Empty *circle* represents an initial homogeneous composition that unmixed on annealing (this study); filled *circles* represent compositions that remained homogeneous during annealing. *Arrows* represent brackets on the two-phase region between  $\alpha$ - and  $\beta$ -Ag(Sb,Bi)S<sub>2</sub>. Upright and inverted triangles represent natural aramayoite compositions reported by Borodayev *et al.* (1986;  $X_{\text{Bi}} \approx 0.35$ ,  $T \approx 250^{\circ}$ C) and Graham (1951;  $X_{\text{bi}} \approx 0.17$ ,  $T > 150^{\circ}$ C as required by the phase diagram) respectively.

partitioning between bismuthinite-stibnites and the  $\beta$ -Ag(Sb,Bi)S<sub>2</sub> solution is strongly dependent on the composition of bismuthinite-stibnite, with  $0.2 \leq X_{Bi}^{Bi} \leq 0.5$  at 300°C. The experiments also demonstrate that the  $\alpha$ -Ag(Sb,Bi)S<sub>2</sub> solution does not coexist stably with bismuthinite-stibnites with  $X_{Bi}^{BS} \geq 0.6$  at 450°C and  $\geq 0.9$  at 300°C, as the  $\alpha$ -Ag(Sb,Bi)S<sub>2</sub> compositions in these experiments undergo partial breakdown to pavonite (AgBi<sub>3</sub>S<sub>5</sub>). In addition, our experiments indicate that a single  $\alpha$ - or  $\beta$ -Ag(Sb,Bi)S<sub>2</sub> solution with  $X_{Bi} = 0.4$  is not stable at 300°C, as homogeneous grains with that initial composition unmixed into  $\alpha$ - and  $\beta$ -Ag(Sb,Bi)S<sub>2</sub> solutions with  $X_{Bi}^{BS} \geq 0.5$  and  $X_{Bi}^{BS} \leq 0.3$  respectively (Fig. 3).

#### Thermodynamic formulation

The molar Gibbs energy of a solid solution  $\Phi$  can be described in terms of its configurational  $(-T\bar{S}^{IC} \Phi)$  and non-configurational (or vibrational;  $\bar{G}^{*\Phi}$ ) components,

$$\bar{\mathbf{G}}^{\Phi} = \bar{\mathbf{G}}^{*\Phi} - \mathbf{T}\bar{\mathbf{S}}^{\mathrm{IC}\ \Phi} \tag{1}$$

For bismuthinite-stibnite (BS;  $(Sb,Bi)_2S_3$ ), the Gibbs energy can be adequately described with a symmetric regular solution model. In this model, the vibrational Gibbs energy is given by the expression

$$\bar{G}^{*BS} = \bar{G}^{0 BS}_{5b_2S_3}(1 - X^{BS}_{Bi}) + \bar{G}^{0 BS}_{Bi_2S_3}X^{BS}_{Bi} + W^{BS}_{Bi-Sb}X^{BS}_{Bi}(1 - X^{BS}_{Bi})$$
(2)

and the configurational component is formulated based on an assumption of random mixing of Sb and Bi on the semi-metal site with a multiplicity of two in the (Sb,Bi)<sub>2</sub>S<sub>3</sub> formula unit,

$$\bar{S}^{IC BS} = -2R[X_{Bi}^{BS} \ln X_{Bi}^{BS} + (1 - X_{Bi}^{BS}) \ln(1 - X_{Bi}^{BS})$$
(3)

A symmetric regular solution model may also be used to describe the Gibbs energy of the  $\alpha$ -Ag(Sb,Bi)S<sub>2</sub> solid solution, with a vibrational component

$$\bar{\mathbf{G}}^{\ast \alpha} = \bar{\mathbf{G}}^{\ast \alpha}_{\mathsf{AgSbS}_{2}}(1 - X^{\alpha}_{\mathsf{Bi}}) + \bar{\mathbf{G}}^{\ast \alpha}_{\mathsf{AgBiS}_{2}}X^{\alpha}_{\mathsf{Bi}} + W^{\alpha}_{\mathsf{Bi-Sb}}X^{\alpha}_{\mathsf{Bi}}(1 - X^{\alpha}_{\mathsf{Bi}})$$
(4)

and a configurational component that assumes random mixing of Ag, Sb and Bi on the two cation sites with exactly 50% of the sites being occupied by Ag atoms,

$$\bar{S}^{IC \alpha} = -2R[\frac{1}{2}ln_2^1 + \frac{1}{2}X_{Bi}^{\alpha} ln_2^1X_{Bi}^{\alpha} + \frac{1}{2}(1 - X_{Bi}^{\alpha}) ln_2^1(1 - X_{Bi}^{\alpha})]$$
(5)

The exchange reaction between bismuthinitestibnite and the  $\alpha$ -Ag(Sb,Bi)S<sub>2</sub> solid solution

$$\frac{1}{2}Bi_{2}S_{3} + AgSbS_{2} = AgBiS_{2} + \frac{1}{2}Sb_{2}S_{3}$$
(6)

can be formulated as

$$\text{RT} \ln \left[ \frac{(1 - X_{\text{Bi}}^{\alpha}) X_{\text{Bi}}^{\text{HS}}}{X_{\text{Bi}}^{\alpha} (1 - X_{\text{Bi}}^{\text{HS}})} + \frac{1}{2} W_{\text{Bi-Sb}}^{\text{BS}} (1 - 2X_{\text{Bi}}^{\text{BS}}) = \Delta \tilde{G}_{\text{BiSb}}^{0} {}^{\text{BS}-\alpha} + W_{\text{Bi-Sb}}^{\alpha} (1 - 2X_{\text{Bi}}^{\alpha})$$
(7)

where

$$\Delta \bar{\mathbf{G}}_{\text{BiSb}}^{0 \text{ BS}-\alpha} = (\Delta \bar{\mathbf{G}}_{\text{AgBiS}_2}^* - \bar{\mathbf{G}}_{\text{AgSbS}_2}^*) - \frac{1}{2} (\bar{\mathbf{G}}_{\text{Bi}_2\text{S}_3}^0 - \bar{\mathbf{G}}_{\text{Sb}_5\text{S}_3}^0) \quad (8)$$

In formulating the Gibbs energy of the  $\beta$ -Ag(Sb,Bi)S<sub>2</sub> phases (i.e. miargyrite, Ag<sub>5</sub>Sb<sub>5</sub>S<sub>10</sub>; aramayoite, Ag<sub>5</sub>Sb<sub>4</sub>BiS<sub>10</sub>; matildite, Ag<sub>5</sub>Bi<sub>5</sub>S<sub>10</sub>), we assume that these phases display pronounced long-range ordering of Sb and Bi atoms between two non-equivalent

			Initia	Y	l			Final co	mosition	of miarc	write-ma	tilditec			
				1517			(wei	ight percei	ntages, st	andard de	viations(	$\sigma$ ) and $\lambda$	(iBi)		
Label	Temp (°C)	Time (h)	BS	MM	# pts	Ag	б	, Sb	, b	Bi	б	S	ь	Total	$X_{\mathrm{Bi}}$
04971-11	450	1584	0.1	0.0	5	33.42	0.30	39.04	0.11	6.08	0.21	21.73	0.21	100.3	0.083
04971-12	450	1584	0.1	0.1	S	33.13	0.35	38.56	0.69	6.39	0.20	21.56	0.16	99.64	0.088
04971-21	450	1584	0.2	0.0	S	32.65	0.53	33.76	0.26	11.96	0.30	21.58	0.19	99.94	0.171
04971-31	450	1584	0.3	0.1	5	31.30	0.47	30.26	0.28	15.77	0.26	20.28	0.29	97.61	0.233
04971-33	450	1584	0.3	0.3	5	31.91	0.27	29.88	0.34	16.56	0.46	20.66	0.20	10.66	0.244
04971-42	450	1584	0.4	0.3	5	30.97	0.37	26.27	0.33	23.02	0.30	20.59	0.58	100.9	0.338
04971-43	450	1584	0.4	0.4	5	30.85	0.40	24.91	0.24	24.55	0.33	20.54	0.14	100.9	0.365
04971-51	450	1584	0.5	0.3	7	28.00	1.39	21.68	0.24	28.61	0.23	20.20	0.10	98.49	0.435
04971-53	450	1584	0.5	0.5	1	29.48	ł	20.14	1	30.08	i	19.57	ł	99.27	0.465
02982-11	400	1512	0.1	0.0	-	36.11	١	38.82	1	4.70	I	21.38	I	101.1	0.066
02982-12	400	1512	0.1	0.1	1	35.38	١	36.97	ł	6.70	1	21.37	1	100.4	0.095
02982-21	400	1512	0.2	0.1	1	35.11	ł	33.37	1	13.12	I	21.08	Ţ	102.7	0.186
02982-23	400	1512	0.2	0.3	1	35.35	١	31.63	1	15.13	I	21.06	T	103.2	0.218
02983-11	350	1176	0.1	0.0		36.14	ł	39.31	1	1.99	I	21.90	ł	99.34	0.029
02983-13	350	1176	0.1	0.2	1	35.76	١	34.74	ł	6.81	ł	20.78	I	98.09	0.103
02983-21	350	1176	0.2	0.1	Ι	34.27	ł	31.97	1	12.72	I	20.71	ł	99.68	0.188
02983-23	350	1176	0.2	0.3	-	33.51	١	31.11	1	13.63	I	20.95	I	99.2	0.203
04974-23	300	3720	0.2	0.2	-	33.84	١	30.56	1	14.02	i	19.83	I	98.24	0.211
04974-24	300	3720	0.2	0.3	1	38.76	١	26.62	1	15.68	I	20.12	I	101.2	0.255
04974-32	300	3720	0.3	0.2	-	33.85	١	31.07	1	14.57	I	20.70	I	100.2	0.215
04974-33	300	3720	0.3	0.3	Ι	33.35	ł	26.70	1	19.43	I	20.42	I	<u>99.89</u>	0.249
04974-41	300	3720	0,4	0.2	1	33.90	١	30.61	1	14.19	I	20.76	I	99.46	0.213
04974-42	300	3720	0.4	0.3	-	35.16	١	29.42	1	16.02	1	20.86	1	101.5	0.241
04974-51	300	3720	0.5	0.3	1	33.80	١	26.30	١	21.65	Ι	20.24	I	102.0	0.324
04974-52	300	3720	0.5	0.4	-1	33.35	١	25.73	1	19.44	I	20.43	I	98.95	0.306
04974-62	300	3720	0.6	0.5		31.21	١	16.19	1	35.00	I	19.06	ł	101.5	0.558
04974-63	300	3720	0.6	0.6	1	30.49	١	15.06	)	33.87	I	19.72	1	99.14	0.567
04974-72	300	3720	0.7	0.6	-	30.95	١	12.62	1	39.73	ł	18.79	I	102.1	0.647
04974-73	300	3720	0.7	0.7	1	30.08	ł	11.05	1	39.51	I	18.47	T	99.11	0.676
04974-82	300	3720	0.8	0.7		28.19	ł	8.61	1	41.71	T	17.45	I	95.96	0.738
04974-83	300	3720	0.8	0.8		29.81	}	7.64	1	43.32	I	17.60	1	98.36	0.768

TABLE 1. Results of exchange experiments between bismuthinite-stibnite and miargyrite-matildite at 300–450°C (Key: BS = bismuthinite-stibnite; MM = miargyrite-matildite)

# BI-SB ENERGETICS IN SULFOSALTS AND SULFIDES

IABLE 2. I hermodynamic mixin $(Key: BS = bismuthinite-stibu)$	g parameters and energies of transitions and e nite; $\beta = \beta$ -Ag(Sb, Bi)S <sub>2</sub> ; $\alpha = \alpha$ -Ag(Sb, Bi)S	xchange reactions in bismuthinite-stibuite and $\alpha$	· and þ-Ag(Sb,Bi)S <sub>2</sub> .
Name of solid solution	Parameter	Description	kJ/gfw
(Bi,Sb) <sub>2</sub> S <sub>3</sub> (bismuthinite-stibnite)	W <sup>BS</sup> W <sup>BS</sup>	Margules-type parameter describing non-ideality of Bi-Sb mixing	12.0±2.0
$lpha-Ag(Sb,Bi)S_2$	$W^{\alpha}_{B^{i},Sb}$	Margules-type parameter describing non-ideality of Bi-Sb mixing	$6.0 \pm 1.0$
β-Ag(Sb,Bi)S <sub>2</sub> Ordering reaction	$\Delta \hat{H}_s^0 \ ^\beta = \hat{H}_{a_s}^0 \ ^\beta S_{a_s} S_{b_s} B_{iS_{10}} + \frac{3}{5} \hat{H}_{a_s}^0 \ ^\beta S_{1s_s} S_{10}$ $\tilde{\pi}_0 \ B \qquad \tilde{\pi}_0 \ B$	Enthalpy of ordering reaction	$-11.0\pm1.0$
<u>5</u> AgsBi <sub>5</sub> S <sub>10</sub> + AgsBi420510 = <u>5</u> AgsBi <sub>5</sub> S <sub>10</sub> + AgsSb4BiS <sub>10</sub>	$\begin{array}{l} -\Pi_{A\hat{g},B\hat{s}}_{i\hat{g},B\hat{s}}_{i\hat{s}}_{i\hat{s}}_{i\hat{s}}_{i\hat{s}} - \tilde{\xi}\Pi_{A\hat{g},S\hat{s},S\hat{s}_{i\hat{s}}}_{i\hat{s}}\\ \Delta \tilde{\xi}_{s}^{0} \ \beta = \tilde{\xi}_{A\hat{g},S\hat{s},B\hat{s},S\hat{s}_{i\hat{s}}} + \frac{3\tilde{\xi}_{0}}{\tilde{\xi}}\tilde{\xi}_{B\hat{s},S\hat{s}_{i\hat{s}}}_{i\hat{s},S\hat{s}_{i\hat{s}}}\\ = \tilde{\xi}_{0,B} \end{array}$	Entropy of ordering reaction	0.0
	$\begin{split} & - \overset{\rm C}{S}\overset{\rm Agg}{}_{\rm gg}{}_{\rm Bi,s}{}_{\rm So} \stackrel{\rm Z}{=} \overset{\rm Z}{}_{\rm S}\overset{\rm C}{}_{\rm So}{}_{\rm So$	Gibbs energy of ordering reaction	$-11.0\pm 1.0$
Reciprocal reaction AgsSb <sub>5</sub> S <sub>10</sub> + AgsBi <sub>5</sub> S <sub>10</sub> = AgsSh <sub>2</sub> Si <sub>5</sub> , + AgsBi <sub>5</sub> Sh <sub>50</sub>	$\Delta \hat{\mathrm{H}}_{\mathrm{x}}^{0}$ $^{eta} = \hat{\mathrm{H}}_{\mathrm{A}_{\mathrm{S}}^{0}\mathrm{S}\mathrm{b}_{\mathrm{z}}}^{\ B}\mathrm{is}_{\mathrm{s}_{\mathrm{u}}} + \hat{\mathrm{H}}_{\mathrm{A}_{\mathrm{S}}^{0}\mathrm{S}\mathrm{B}\mathrm{i}_{\mathrm{z}}\mathrm{S}\mathrm{b}_{\mathrm{l}0}}^{\ D}$ $- \hat{\mathrm{H}}_{\mathrm{u}}^{0} \hat{\mathrm{B}}_{\mathrm{u}},  - \hat{\mathrm{H}}_{\mathrm{u}}^{0} \hat{\mathrm{B}}_{\mathrm{u}},  -$	Enthalpy of reciprocal reaction	0.0
	$\Delta \tilde{\mathbf{S}}_{\mathbf{X}}^{0} \ \boldsymbol{\beta} = \tilde{\mathbf{S}}_{\mathbf{A}}^{0} \begin{array}{c} \boldsymbol{\beta} \\ \boldsymbol{\beta} = \tilde{\mathbf{S}}_{\mathbf{A}}^{0} \begin{array}{c} \boldsymbol{\beta} \\ \boldsymbol{\beta} \\ \boldsymbol{\beta} \\ \boldsymbol{\beta} \end{array} \right) + \tilde{\mathbf{S}}_{\mathbf{A}}^{0} \begin{array}{c} \boldsymbol{\beta} \\ \boldsymbol{\beta} $	Entropy of reciprocal reaction	0.0
	$\begin{split} &-S^{4}_{\text{B}\text{S}} S_{\text{B}\text{S}} S_{\text{I}0} - S^{V}_{\text{B}\text{S}} B_{\text{I}} S_{\text{I}0} \\ &\Delta \tilde{G}^{0}_{\text{S}} \ \beta = \Delta \tilde{H}^{0}_{\text{S}} \ \beta - T \Delta \tilde{S}^{0}_{\text{S}} \ \beta \end{split}$	Gibbs energy of reciprocal reaction	0.0

S. GHOSAL AND R. O. SACK

	$W_{Bl-Sb}^{I\beta}$	Margules-type parameter describing non-ideality of Bi-Sb mixing on site I	$34.0 \pm 4.0$
	W <sup>II</sup> B Bi:Sb	Margules-type parameter describing non-ideality of Bi-Sb mixing on site II	$8.5 \pm 1.0$
β→α	$\Delta {ar H}_{AgSuS_2}^{0\ eta - arkappa}$	Enthalpy of transition for Sb-end-member	7.53
	$\Delta ar{S}^0 egin{array}{c} eta \to lpha \ Aggs b S_2 \end{array}$	Entropy of transition for Sb-end-member	0.0115
	$\Delta { ilde H}^0_{AgBiS_2}$	Enthalpy of transition for Bi-end-member	5.34
	$\Delta \bar{S}^{0}_{A\bar{g}BIS_2}^{p\to \alpha}$	Entropy of transition for Bi-end-member	0.0115
Energies of exchange reaction	$\Delta \tilde{G}_{BiSb}^{0~BS-\alpha}$	Energy of exchange reaction between bismuthinite-stibuite and $\alpha$ -AgSbS <sub>2</sub> (Equation 8)	$2.70 \pm 0.10$
	$\Delta \bar{G}_{Bi-Sb}^0  B_{S-\beta}$	Energy of exchange reaction between bismuthinite-stibnite and β-AgSbS <sub>2</sub> (Equation 14)	$4.89 \pm 0.10$

TABLE 2. (contd.)

**BI-SB ENERGETICS IN SULFOSALTS AND SULFIDES** 

semi-metal sites (I and II) which occur in a ratio of multiplicities of 4:1. A formula unit based on 10 S atoms is chosen for the  $\beta$ -Ag(Sb,Bi)S<sub>2</sub> solid solution to simplify the formulation of the model for the Gibbs energy, and, the species Ag<sub>5</sub>(Sb)<sup>I</sup><sub>4</sub>(Bi)<sup>II</sup>S<sub>10</sub> represents a fully ordered 'aramayoite' component that is stable at low temperatures. Molar compositional and ordering variables may be defined as

 $X_{Bi}^{\beta} = Bi/(Bi + Sb)$ 

and

$$s^{\beta} = \chi^{II}_{\mathrm{Pi}}{}^{\beta} - \chi^{I}_{\mathrm{Pi}}{}^{\beta} \tag{9}$$

The vibrational component of the Gibbs energy of  $\beta$ -Ag(Sb,Bi)S<sub>2</sub> solid solutions can be adequately expressed as a second-order Taylor's expansion in these compositional and ordering variables:

$$\bar{\mathbf{G}}^{*\beta} = g_o + g_x(X^{\beta}_{\mathrm{Bi}}) + g_s(s^{\beta}) + g_{xx}(X^{\beta}_{\mathrm{Bi}})^2 + g_{ss}(s^{\beta})^2 + g_{xs}(X^{\beta}_{\mathrm{Bi}})(s^{\beta}), \quad (10)$$

Following procedures outlined elsewhere (e.g. Sack, 1992) the coefficients in equation 10 may be ready related to end-member energies  $(\bar{G}^{0}_{Ag,Sb_{S}b_{S}}, \bar{G}^{0}_{Ag,Bi_{S}b_{S}}, \bar{G}^{0}_{Ag,Bi_{S}$ 

$$\begin{split} \bar{\mathbf{G}}^{*\beta} &= \bar{\mathbf{G}}_{Ag_{s}Sb_{5}S_{10}}^{0}(1-X_{Bi}^{\beta}) + \bar{\mathbf{G}}_{Ag_{s}Bi_{5}S_{10}}^{0}X_{Bi}^{\beta} + \\ & (\Delta \bar{\mathbf{G}}_{x}^{0\ \beta} + \mathbf{W}_{Bi-Sb}^{1\ \beta} + \mathbf{W}_{Bi-Sb}^{1\ \beta})(X_{Bi}^{\beta})(1-X_{Bi}^{\beta}) + \\ & (\frac{3}{10}\Delta \bar{\mathbf{G}}_{x}^{0\ \beta} + \frac{1}{2}\Delta \bar{\mathbf{G}}_{s}^{0\ \beta} - \frac{1}{5}\mathbf{W}_{Bi-Sb}^{1\ \beta} + \frac{4}{5}\mathbf{W}_{Bi-Sb}^{1\ \beta})(s^{\beta}) + \\ & (\frac{4}{25}\Delta \bar{\mathbf{G}}_{x}^{0\ \beta} - \frac{1}{25}\mathbf{W}_{Bi-Sb}^{1\ \beta} - \frac{16}{25}\mathbf{W}_{Bi-Sb}^{1\ \beta})(s^{\beta})^{2} + \\ & (-\frac{3}{2}\Delta \bar{\mathbf{G}}_{x}^{0\ \beta} + \frac{2}{5}\mathbf{W}_{Bi-Sb}^{1\ \beta} - \frac{8}{5}\mathbf{W}_{Bi-Sb}^{1\ \beta})(X_{Bi}^{\beta})(s^{\beta}) \quad (11) \end{split}$$

For the molar configurational entropy of the  $\beta$ -Ag(Sb,Bi)S<sub>2</sub> solid solution we may write the following formulation based on the assumption that Sb and Bi display long-range nonconvergent ordering between sites I and II (e.g. Harlov and Sack, 1994).

$$\begin{split} \bar{\mathbf{S}}^{\text{IC}\ \beta} &= -\mathbf{R}[4(1 - X_{\text{B}i}^{\beta} + \frac{1}{5}s^{\beta})\ln(1 - X_{\text{B}i}^{\beta} + \frac{1}{5}s^{\beta}) + \\ &\quad 4(X_{\text{B}i}^{\beta} - \frac{1}{5}s^{\beta})\ln(X_{\text{B}i}^{\beta} - \frac{1}{5}s^{\beta}) + \\ &\quad (1 - X_{\text{B}i}^{\beta} - \frac{4}{5}s^{\beta})\ln(1 - X_{\text{B}i}^{\beta} - \frac{4}{5}s^{\beta}) + \\ &\quad (X_{\text{B}i}^{\beta} + \frac{4}{5}s^{\beta})\ln(X_{\text{B}i}^{\beta} + \frac{4}{5}s^{\beta}) \end{split}$$
(12)

The Sb-Bi exchange reaction between bismuthinite-stibnite and the  $\beta$ -Ag(Sb,Bi)S<sub>2</sub> solid solution

$$Bi_{2}S_{3} + \frac{1}{5}Ag_{5}Sb_{5}S_{10} = \frac{1}{5}Ag_{5}Bi_{5}S_{10} + \frac{1}{2}Sb_{2}S_{3}$$
(13)

can thus be described as

$$\operatorname{RT} \ln \left[ \left\{ \frac{(1 - X_{\text{Bi}}^{\beta} + \frac{1}{3} s^{\beta})^{4} (1 - X_{\text{Bi}}^{\beta} - \frac{4}{3} s^{\beta})}{(X_{\text{Bi}}^{\beta} - \frac{1}{3} s^{\beta})^{4} (X_{\text{Bi}}^{\beta} + \frac{4}{3} s^{\beta})} \right\}^{1/5} \frac{X_{\text{Bi}}^{\text{BS}}}{(1 - X_{\text{Bi}}^{\text{BS}})} \right] - \Delta \bar{G}_{\text{BiSb}}^{0} \stackrel{\text{BS}-\beta}{1} + \frac{1}{2} W_{\text{Bi-Sb}}^{\text{BS}} (1 - 2X_{\text{Bi}}^{\text{BS}}) = \frac{1}{5} (\Delta \bar{G}_{x}^{0} \stackrel{\beta}{} + W_{\text{Bi-Sb}}^{1} + W_{\text{Bi-Sb}}^{1} (1 - 2X_{\text{Bi}}^{\beta}) + \frac{1}{25} (-3\Delta \bar{G}_{x}^{0} \stackrel{\beta}{} + 2W_{\text{Bi-Sb}}^{1} - 8W_{\text{Bi-Sb}}^{11}) (1 - 2X_{\text{Bi}}^{\beta}) + \frac{1}{25} (-3\Delta \bar{G}_{x}^{0} \stackrel{\beta}{} + 2W_{\text{Bi-Sb}}^{1} - 8W_{\text{Bi-Sb}}^{11}) (s^{\beta})$$
(14)

where

$$\begin{split} \Delta \tilde{\mathbf{G}}_{\text{BiSb}}^{0 \text{ BS-}\beta} &= \frac{1}{5} (\tilde{\mathbf{G}}_{\text{Ag}_{s}\text{Bi}_{s}\text{S}_{10}}^{0} - \tilde{\mathbf{G}}_{\text{Ag}_{s}\text{S}\text{B}_{s}\text{S}_{10}}^{0}) - \\ & \frac{1}{2} (\tilde{\mathbf{G}}_{\text{Ag}_{s}\text{S}\text{b}_{s}\text{S}_{10}}^{0} - \tilde{\mathbf{G}}_{\text{Sb}_{2}\text{S}_{3}}^{0}) = \\ & \Delta \tilde{\mathbf{G}}_{\text{BiSb}}^{0 \text{ BS-}\alpha} + \Delta \tilde{\mathbf{G}}_{\text{Ag}\text{Sb}_{2}}^{0 \beta \rightarrow \alpha} - \Delta \tilde{\mathbf{G}}_{\text{Ag}\text{BiS}_{2}}^{0 \beta \rightarrow \alpha} \quad (15) \end{split}$$

The value of  $s^{\beta}$  for a given  $X_{Bi}^{\beta}$  and T can be determined by applying the condition of homogeneous equilibrium to the Gibbs energy of the solid solution

$$(\partial \bar{\mathbf{G}}/\partial s^{\beta}) = 0 \tag{16}$$

which gives us the equation

$$\operatorname{RT} \ln \left[ \frac{(X_{\mathrm{Bi}}^{\beta} - \frac{1}{5}g^{\beta})(1 - X_{\mathrm{Bi}}^{\beta} - \frac{4}{5}g^{\beta})}{(1 - X_{\mathrm{Bi}}^{\beta} + \frac{1}{5}g^{\beta})(X_{\mathrm{Bi}}^{\beta} + \frac{4}{5}g^{\beta})} \right] = \\ \left( \frac{3}{5} \Delta \bar{G}_{x}^{0} \beta + \frac{5}{5} \Delta \bar{G}_{x}^{0} \beta - \frac{1}{4} W_{\mathrm{Bi-Sb}}^{I} + W_{\mathrm{Bi-Sb}}^{\mathrm{II}} + W_{\mathrm{Bi-Sb}}^{\mathrm{II}} \right) + \\ \left( \frac{3}{5} \Delta \bar{G}_{x}^{0} \beta - \frac{1}{10} W_{\mathrm{Bi-Sb}}^{I} - \frac{5}{5} W_{\mathrm{Bi-Sb}}^{\mathrm{II}} \right) (s^{\beta}) + \\ \left( -\frac{3}{4} \Delta \bar{G}_{x}^{0} \beta + \frac{1}{2} W_{\mathrm{Bi-Sb}}^{I} - 2 W_{\mathrm{Bi-Sb}}^{\mathrm{II}} \right) (X_{\mathrm{Bi}}^{\beta})$$
(17)

Finally, the condition of equilibrium for the Sb-Bi exchange reaction between the  $\alpha$ - and  $\beta$ -Ag(Sb,Bi)S<sub>2</sub> solid solutions,

$$AgBiS_{2} + \frac{1}{5}Ag_{5}Sb_{5}S_{10} = \frac{1}{5}Ag_{5}Bi_{5}S_{10} + AgSbS_{2}$$
(18)

may be derived by subtracting equation 7 from 14.

$$\operatorname{RT} \operatorname{In} \left[ \left\{ \frac{(1 - X_{B_{i}}^{\beta} + \frac{1}{3} s^{\beta})^{4} (1 - X_{B_{i}}^{\beta} - \frac{4}{3} s^{\beta})}{(X_{B_{i}}^{\beta} + \frac{1}{3} s^{\beta})^{4} (X_{B_{i}}^{\beta} + \frac{4}{3} s^{\beta})} \right\}^{1/5} \frac{X_{B_{i}}^{\alpha}}{(1 - X_{B_{i}}^{\alpha})} \right] + \Delta \tilde{G}_{AgBiS_{2}}^{0} - \Delta \tilde{G}_{AgBiS_{2}}^{0} + W_{Bi-Sb}^{\alpha} (1 - 2X_{B_{i}}^{\alpha}) = \frac{1}{5} (\Delta \tilde{G}_{x}^{0} \ ^{\beta} + W_{Bi-Sb}^{1} + W_{Bi-Sb}^{B}) (1 - 2X_{B_{i}}^{\beta}) + \frac{1}{25} (-3\Delta \tilde{G}_{x}^{0} \ ^{\beta} + 2W_{Bi-Sb}^{1} - 8W_{Bi-Sb}^{II,\beta}) (s^{\beta})$$
(19)

#### Calibration of thermodynamic models

In conjunction with constraints on the transition temperatures between the  $\alpha$ - and  $\beta$ -Ag(Sb,Bi)S<sub>2</sub> solutions, and bounds on the width of their two-

phase loop, we may develop a calibration for the parameters describing Sb-Bi mixing in bismuthinite-stibuite and  $\alpha$ - and  $\beta$ -Ag(Sb,Bi)S<sub>2</sub> based on analysis of our brackets on Sb-Bi partitioning. The parameters are tightly bound, if it is assumed that the standard state Gibbs energies of the Sb-Bi exchange reactions (Eqns 8, 15) are independent of temperature (e.g. Sack and Ghiorso, 1989; Harlov and Sack, 1994). As a first approximation, we may also assume that the entropy of the ordering reaction  $(\Delta \bar{S}_s^0 \beta)$ , and the enthalpy and entropy of the reciprocal reaction  $(\Delta \bar{H}_x^{0\beta}, \Delta \bar{S}_x^{0\beta})$ , for the  $\beta$ -Ag(Sb,Bi)S<sub>2</sub> solid solution are zero (Table 2). Finally, we may assume that the entropy changes of the  $\beta \rightarrow \alpha$  transitions are entirely due to the configurational effect of the complete disordering of Ag, Sb and Bi between the metal and semi-metal sites that are distinct in the lowtemperature ordered ( $\beta$ ) structure (e.g. Graham, 1951). For this assumption, the entropies of the  $\beta \rightarrow \alpha$  transitions in the AgSbS<sub>2</sub> and AgBiS<sub>2</sub> endmembers  $(\Delta \bar{S}^{0}_{AgSbS_{2}}, \Delta \bar{S}^{0}_{AgBiS_{2}})$  are 2Rln2 per formula unit, and values of  $\Delta \bar{H}^{0} \xrightarrow{\beta \to \alpha}$  for these transitions (determined from the relation  $\Delta \bar{H}^{0 \beta \rightarrow \alpha} =$  $T \Delta \bar{S}^{0 \beta \to \alpha}$ ;  $T \approx 380^{\circ}$ C for AgSbS<sub>2</sub>; 190°C for  $AgBiS_2$ ) are consistent with the calorimetric determinations of Bryndzia and Kleppa (1989). With these assumptions and the requirement that  $W_{Bi-Sb}^{BS} \leq 14.0 \text{ kJ/gfw}$  (bismuthinite-stibnites exhibit continuous solid solubility at temperatures  $\geq 200^{\circ}$ C; Springer and Laflamme, 1971), we may readily develop a calibration for the condition of equilibrium of the Sb-Bi exchange reaction between bismuthinite-stibuite and the  $\alpha$ -Ag(Sb,Bi)S<sub>2</sub> solid solution (Equation 7) that satisfies our brackets on Sb-Bi partitioning between these phases at  $300-450^{\circ}$ C (Fig. 2), provided  $W_{Bi-Sb}^{BS} \approx W_{Bi-Sb}^{\alpha}$  $\Delta \bar{G}_{Bi-Sb}^{0 BS-\alpha} \approx 2.6-3.2$  kJ/gfw.

Examination of the conditions of Bi-Sb exchange equilibrium between bismuthinite-stibnite and  $\beta$ -Ag(Sb,Bi)S<sub>2</sub> (Equation 14), and between coexisting  $\alpha$ - and  $\beta$ -Ag(Sb,Bi)S<sub>2</sub> (Equation 18), allows the value of  $W_{Bi-Sb}^{Bi}$  to be refined, and values of  $W_{Bi-Sb}^{Bi}$  (assumed to be equal to 4W) and  $\Delta \bar{H}_{s}^{0\ \beta}$  to be determined (Table 2). The strong composition dependence on the apparent Gibbs energy of the Sb-Bi exchange reaction between bismuthinite-stibuite and  $\beta$ -Ag(Sb,Bi)S<sub>2</sub> can only be satisfied if  $\frac{1}{4}W_{Bi-Sb}^{1\ \beta}$  (=  $W_{Bi-Sb}^{II\ \beta}$ ) is greater than  $\frac{1}{2}W_{Bi-Sb}^{Bi}$  by at least 2 kJ/gfw, and if the standard state Gibbs energy of the reaction

$$\frac{\frac{3}{5}Ag_5Sb_5S_{10} + Ag_5(Bi)_4^{I}(Sb)^{II}S_{10} = \\ \frac{\frac{3}{5}Ag_5Bi_5S_{10} + Ag_5(Sb)_4^{I}(Bi)^{II}S_{10}}{2}$$

is strongly negative (i.e.  $\Delta \bar{H}_s^{0~\beta} < -10 \text{ kJ/gfw}$ ). Values of  $W_{Bi,Sb}^{BS} > 14.0 \text{ kJ/gfw}$  require values of  ${}_{4}^{1}W_{Bi-Sb}^{I\beta}$  and  $W_{Bi-Sb}^{II\beta}$  (>9.5 kJ/gfw) that are also unrealistically large, predicting miscibility gaps between miargyrite and aramayoite, and between aramayoite and matildite too extensive to satisfy experimental and natural constraints, respectively. For example, values of  $W_{Bi-Sb}^{II} > 9.5 \text{ kJ/gfw}$ require miscibility gaps to appear at  $T > 300^{\circ}$ C  $(X_{\rm Bi} \approx 0.10)$ , but in our experiments, Ag(Sb,Bi)S<sub>2</sub> grains of this composition were stable to annealing for 4 months at 300°C. Equivalent values for  $\frac{1}{4}W_{Bi-Sb}^{I\beta}$  require miscibility gaps between aramayoite and matildite too extensive to accommodate the natural aramayoite composition reported by Borodayev et al. (1986;  $X_{\rm Bi} \approx 0.35$ ; Fig. 3).

At the opposite extreme, the assumption of ideal mixing in bismuthinite-stibnite  $(W_{Bi-Sb}^{BS} = 0.0)$ , values of  $\frac{1}{4}W_{Bi-Sb}^{I\beta}$  and  $W_{Bi-Sb}^{II\beta}$  of at least 6.0 kJ/gfw are required. Calibrations predicted on this assumption may be considered problematic because of the large implied difference in non-ideality of Sb-Bi substitution in solutions with similar structures. We therefore adopt the calibration for parameters given in Table 2 for a value of  $W_{Bi-Sb}^{BS}$  of 12.0 + 2.0 kJ/gfw, to achieve maximal correspondence between the models and experimental data, as well as be consistent with the premise that the energetic consequences of Sb-Bi substitution should not be grossly different in materials with similar structures. The calibrated parameters are used in constructing a phase diagram for the AgSbS<sub>2</sub>-AgBiS<sub>2</sub> binary subsystem (Fig. 3), and the resulting calculated miscibility gaps between the  $\beta$ -Ag(Sb,Bi)S<sub>2</sub> sulfosalts, miargyrite, aramayoite and matildite, are consistent with phase assemblages and compositions observed in nature.

# Conclusions

Antimony-bismuth mixing in sulfides and argentian sulfosalts is significantly non-ideal, in accordance with similar non-idealities exhibited by their As-Sb counterparts (Ghosal and Sack, 1995). Bismuthinite-stibnites ( $W_{Bi-Sb}^{BS} \approx 12.0 \text{ kJ/}$ gfw) are predicted to exsolve at temperatures  $\leq 88^{\circ}$ C, consistent with their exhibiting continuous solid solution in hydrothermal ore deposits ( $T \approx 150-350^{\circ}$ C), but exhibiting preponderances in molar ratios towards the end-members (Lueth, 1988; Fig. 1). The non-idealities in disordered Sb-Bi sulfides and sulfosalts are found to be less than that of their As-Sb counterparts, with the exception of ordered compounds (Table 2; Ghosal and Sack, 1995), and this can be attributed to the lesser relative size difference between Sb and Bi atoms, causing smaller strain effects.

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#### References

- Bartos, P.J. (1990) Metal ratios of the Quirivilca mining district, northern Peru. Econ. Geol., 85, 1629–44.
- Boldyreva, M.M. (1970) Matildite, β-AgBiS<sub>2</sub>, from the Tary Ekan deposit, Eastern Karamazar. *Dok. Akad. Nauk SSSR*, **194**, 122–4.
- Borodayev, Y.S., Nenasheva, S.N., Gamyanin, G.N. and Mozgova, N.N. (1986) First find of aramayoitegalena-matildite exsolution textures. *Dokl. Akad. Nauk SSSR*, 290, 192–5.
- Brooker, M. and Jaireth, S. (1995) Mount Rawdon, southeast Queensland, Australia - A diatreme-hosted gold-silver deposit. *Econ. Geol.*, **90**, 1799–817.
- Bryndzia, L.T. and Kleppa, O.J. (1989) Standard molar enthalpies of formation of sulfosalts in the Ag-As-S system and thermochemistry of the sulfosalts of Ag with As, Sb, and Bi. *Amer. Mineral.*, 74, 243–9.
- Bussell, M.A., Alpers, C.N., Petersen, U., Shepherd, T.J., Bermudez, C. and Baxter, A.N. (1990) The Ag-Mn-Pb-Zn vein, replacement, and skarn deposits of Uchucchacua, Peru: Studies of structure, mineralogy, metal zoning, Sr isotopes, and fluid inclusions. *Econ. Geol.*, **85**, 1348–83.
- Chang, L.L.Y., Knowles, C.R. and Chen, T.T. (1977) Phase relations in the systems Ag<sub>2</sub>S-Sb<sub>2</sub>S<sub>3</sub>-Bi<sub>2</sub>S<sub>3</sub>, Ag<sub>2</sub>S-As<sub>2</sub>S<sub>3</sub>-Sb<sub>2</sub>S<sub>3</sub> and Ag<sub>2</sub>S-As<sub>2</sub>S<sub>3</sub>-Bi<sub>2</sub>S<sub>3</sub>. *Mem. Geol. Soc. China*, **2**, 229–37.
- Czamanske, G.K. and Hall, W.E. (1975) The Ag-Bi-Pb-Sb-S-Se-Te mineralogy of the Darwin lead-silverzinc deposit, southern California. *Econ. Geol.*, 70, 1092–110.
- Ghosal, S. and Sack, R.O. (1995) As-Sb energetics in argentian sulfosalts. *Geochim. Cosmochim. Acta*, 59, 3573-9.
- Gibson, P.C., Noble, D.C. and Larson, L.T. (1990) Multistage evolution of the caldera epithermal Ag-Au vein system, Orcopampa district, southern Peru: first results. *Econ. Geol.*, **85**, 1504–19.
- Gilmer, A.L., Clark, K.F., Conde, C.J., Hernandez, I.C.,

Figueroa, J.I.S. and Porter, E.W. (1988) Sierra de Santa Maria, Velardeña mining dirtrcit, Durango, Mexico. *Econ. Geol.*, **83**, 1802–29.

- Goodell, P.C. (1974) A typical sulfosalt environment: The mineralogy of the Julcani district, Peru. *Mineral. Mag.*, 38, 215–21.
- Goodell, P.C. and Petersen, U. (1974) Julcani mining district, Peru: A study of metal ratios. *Econ. Geol.*, 69, 347–61.
- Graham, A.R. (1951) Matildite, aramayoite, miargyrite. Amer. Mineral., **36**, 436–49.
- Gröpper, H., Calvo, M., Crespo, H., Bisso, C.R., Cuadra, W.A., Dunkerley, P.M. and Aguirre, E. (1991) The epithermal gold-silver deposit of Choquelimpie, northern Chile. *Econ. Geol.*, **86**, 1206–21.
- Harlov, D.E. and Sack, R.O. (1994) Thermochemistry of polybasite-pearceite solid solutions. *Geochim. Cosmochim. Acta*, 58, 4363–75.
- Hayase, K. (1955) Minerals of bismuthinite-stibnite series with special reference to horobetsuite from the horobetsu mine, Hokkaido, Japan. *Mineral. J.*, 1, 189–97.
- Jeppson, M. (1987) Mineral chemistry of silver in antimony and bismuth rich sulfide ores in Bergslagen, central Sweden. *Neues Jahrb. Mineral. Mon.*, 5, 205-6.
- Johnson, T.W. and Meinert, L.D. (1994) Au-Cu-Ag skarn and replacement mineralization in the McLaren deposit, New World district, Park County, Montana. *Econ. Geol.*, **89**, 969–93.
- Keighin, C.W. and Honea, R.M. (1969) The system Ag-Sb-S from 600°C to 200°C. *Mineral. Deposita*, 4, 153–71.
- Kelly, W.C. and Turneaure, F.S. (1970) Mineralogy, paragenesis and geothermometry of the tin and tungsten deposits of the Eastern Andes, Bolivia. *Econ. Geol.*, **65**, 609–80.
- Klein, C. and Hurlburt, Jr., C.S. (1971) Manual of Mineralogy (after James D. Dana). 20th Edition, John Wiley & Sons, New York.
- Knowles, C.R. (1964) A redetermination of the structure of miargyrite, AgSbS<sub>2</sub>. Acta Crystallogr., 17, 847-51.
- Lueth, V.W. (1988) Studies of the geochemistry of the semimetal elements: arsenic, antimony, and bismuth. Unpublished Ph.D. thesis, University of Texas at El Paso.
- Lueth, V.W., Goodell, P.C. and Pingitore, N.E., Jr. (1990) Encoding the evolution of an ore system in bismuthinite-stibnite compositions: Julcani, Peru. *Econ. Geol.*, 85, 1462–72.
- Mullen, D.J.E. and Nowacki, W. (1974) The crystal structure of aramayoite Ag(Sb,Bi)S<sub>2</sub>. Zeits. Krist., 139, 54–69.
- Petersen, U., Noble, D.C., Arenas, M.J. and Goodell, P.C. (1977) Geology of the Julcani mining district,

Peru. Econ. Geol., 72, 931-49.

- Petruk, W. (1968) Mineralogy and origin of the Silversfield silver deposit in the Cobalt area, Ontario. *Econ. Geol.*, 63, 512-31.
- Ruvalcaba-Ruiz, D.C. and Thompson, T.B. (1988) Ore deposits at the Fresnillo mine, Zacatecas, Mexico. *Econ. Geol.*, 83, 1583–96.
- Sack, R.O. (1992) Thermochemistry of tetrahedritetennantite fahlores. In *The Stability of Minerals* (N.L. Ross and G.D. Price, eds), Chapman & Hall, London, pp. 243–66.
- Sack, R.O. and Ghiorso, M.S. (1989) Importance of considerations of mixing properties in establishing an internally consistent thermodynamic database: thermochemistry of minerals in the system Mg<sub>2</sub>SiO<sub>4</sub>-Fe<sub>2</sub>SiO<sub>4</sub>-SiO<sub>2</sub>. *Contrib. Mineral. Petrol.*, **102**, 41–68.

- Sillitoe, R.H., Halls, C. and Grant, J.N. (1975) Porphyry tin deposits in Bolivia. *Econ. Geol.*, **70**, 913–27.
- Springer, G. (1969) Naturally occurring compositions in the solid-solution series Bi<sub>2</sub>S<sub>3</sub>-Sb<sub>2</sub>S<sub>3</sub>. *Mineral. Mag.*, 37, 294-6.
- Springer, G. and Laflamme, J.H.G. (1971) The system Bi<sub>2</sub>S<sub>3</sub>-Sb<sub>2</sub>S<sub>3</sub>. *Canad. Mineral.*, **10**, 847–53.
- Van Hook, H.J. (1960) The ternary system Ag<sub>2</sub>S-Bi<sub>2</sub>S<sub>3</sub>-PbS. *Econ. Geol.*, **55**, 759–88.
- Stone, J.G. (1959) Ore genesis in the Naica district, Chihuahua, Mexico. *Econ. Geol.*, 54, 1002–34.
- Turneaure, F.S. (1971) The Bolivian tin-silver province. Econ. Geol., 66, 215-25.

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