# THE CRYSTALLOGRAPHY OF HERDERITE FROM TOPSHAM, MAINE 

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#### Abstract

Crystals of herderite, $\mathrm{CaBe}(\mathrm{OH}, \mathrm{F}) \mathrm{PO}_{4}$, from Topsham, Maine, a new locality, exhibit several novelties: prismatic development in the direction of the $c$-axis, twinning on (100), and the new forms $\alpha$ (I04), $\beta$ ?(115), $\gamma(121)$. Herderite from a new find at Greenwood, Maine, shows the normal columnar development of the clinodome zone and known forms with the addition of $\gamma(121)$. The crystallography of the species is revised and referred to new parameters, $a: b: c=0.6307: 1: 1.2822$; $\beta=90^{\circ} 6^{\prime}$, obtained by trebling the $c$-axis of Penfield. The revised form list contains 33 accepted forms ( 2 new) and 11 uncertain forms ( 1 new). Three described forms are rejected. For the accepted forms a suitable angle-table is given.


In the summer of 1933 a pocket in the pegmatite of Fisher Quarry, Topsham, Maine, was opened under the active direction of Professor Charles Palache, and an interesting suite of minerals was uncovered. The field relations of this material, which is preserved in the Harvard Mineralogical Museum, were described in a general paper by Palache (1934). The minerals found are more or less typical of the complex acid pegmatites of Maine: cleavelandite, quartz, lepidolite, beryl, topaz, gahnite, tourmaline, garnet, columbite, sericite, apatite, torbernite, cookeite and, last to form, the rare phosphate herderite in considerable abundance.

The herderite occurs in well developed crystals up to nearly 5 cm . long and 3 cm . wide, attached to quartz, cleavelandite, lepidolite, topaz, and sericite. They range from white or greenish-white to colourless; some are stained brown. Among the smaller crystals a considerable number are transparent and fairly brilliant, but all those over half a centimeter long are mottled and translucent. A few crystals are soiled with dried kaolin; the majority, however. are clean and suitable for measurement.

A study of these crystals revealed the fact that herderite presents peculiar goniometric difficulties because of surprising variation in habit and similarity of angles in different zones. It was decided, therefore, to study the crystallography of the species in some detail, supplementing observations on the material from Topsham by measurements on crystals from a new find at Greenwood, Maine, already known through Penfield's work (1894) as a herderite local-
ity. This study suggested a revised statement of the crystallography in which some of the described forms have been rejected and some set aside as uncertain; two new forms have been added to the list of accepted forms and an angle table has been prepared in a suitable form with reference to a new choice of parameters.
Herderite from Ehrenfriedersdorf, Saxony, was recognized as a new species by Haidinger (1828), and described as an othorhombic mineral. E. S. Dana (1884) described crystals from Stoneham, Maine, which he found to be orthorhombic, developed prismatically with the $a$-axis. Penfield (1894) first recognized the monoclinic symmetry of herderite from several localities in Maine, and the twinning, together with nearly rectangular axes, which leads to the orthorhombic appearance of the crystals. He chose an orientation and elements that agreed as closely as possible with the orthorhombic setting of Dana. Thus the clino-axis became the axis of prismatic development with the observed twinning plane as the base. In a short note, Henglein (1909) described a crystal from Epprechtstein, Bavaria, with several new forms, prismatically developed with the $c$-axis and twinned on the orthopinacoid. Dürrfeld (1909 A) discredited Henglein's description, and showed that in the conventional setting, Henglein's supposed new forms were already known on herderite. In subsequent studies, Dürrfeld ( 1909 B, 1910, 1911) described numerous crystals from Epprechtstein, on which he found several new forms; all the crystals showed the usual prismatic development in the direction of the clinoaxis, with twinning on the base. Ford (1911) added further crystallographic observations on material from Auburn, Maine, retaining Penfield's setting of the mineral.
Four crystals from Topsham were selected for measurement and description. They all proved to be prismatically developed with the vertical axis, two being monoclinic individuals, the other two twins on the orthopinacoid. Since this is the very type of development that was once announced and immediately discredited, it will be necessary to compare the measured angles with those of herderite in the conventional setting and in the position which results from the interchange of the $a$ - and $c$-axes.
Two crystals from Greenwood were also measured. They proved to be monoclinic individuals developed equally in the directions of the $a$ - and $c$-axes, and terminated in front by positive forms above and negative forms below.
Table 1. Herderite. Two-Circle Measurements on Six Crystals

| Forms | Measured |  |  |  |  |  | Calculated |  | Calculated with $a$ - and $c$-axes interchanged |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Range |  | Mean |  | No. of Faces | No. of Crystals | $\phi$ | $\rho$ | Forms | $\phi$ | ${ }^{\rho}$ |
|  | $\phi$ | $\rho$ | $\phi$ | $p$ |  |  |  |  |  |  |  |
| c 001 | $90^{\circ} 01^{\prime}-90^{\circ} 02^{\prime}$ | $0^{\circ} 17^{\prime}-0^{\circ} 27^{\prime}$ | $90^{\circ} 01^{\prime}$ | $0^{\circ} 21^{\prime}$ | 6 | 5 | $90^{\circ} 00^{\prime}$ | $0^{\circ} 06^{\prime}$ |  |  |  |
| ${ }^{b} 0010$ | 000-004 | - | 002 | 9000 | 8 | 4 | 000 | 9000 | $\begin{array}{ll}a & 100 \\ b & 010\end{array}$ | $\begin{array}{r} -90^{\circ} 00^{\prime} \\ 000 \end{array}$ | $\begin{gathered} 0^{\circ} 06^{\prime} \\ 9000 \end{gathered}$ |
| a 100 | - | - | 9001 | 9000 | 1 | 1 | 9000 | 9000 | ${ }_{\text {c }} 0001$ | 9000 | 9000 |
| $l 120$ | 38 47-38 55 | - | 3851 | 9000 | 4 | 3 | $3824 \frac{1}{2}$ | 9000 | v 011 |  |  |
| $m 110$ | 57 43-58 10 | - | 5800 | 9000 | 20 | 6 | $5745 \frac{1}{2}$ | 9000 | $t \quad 012$ | 3720 57 | $\begin{aligned} & 9000 \\ & 9000 \end{aligned}$ |
| u 013 | 013-101 | 23 07-23 11 | 045 | 2309 | 9 | 4 | 014 | $2308 \frac{1}{2}$ |  |  |  |
| $t \quad 012$ | 000-016 | 32 20-32 38 | 009 | 3232 | 13 | 6 | $009 \frac{1}{2}$ | 3240 |  | -0 091 |  |
| v 011 | 004-029 | 51 37-51 58 | 011 | 5148 | 10 | 4 | $004 \frac{1}{2}$ |  | $l \mid 120$ | -0 04 | 52 $314 \frac{1}{2}$ |
| s 021 | 004-014 | 68 40-68 46 | 005 | 6844 | 5 | 3 | $002{ }^{\frac{1}{2}}$ | 6842 | $\bigcirc 120$ | -0 04 |  |
| ${ }^{*} \alpha{ }^{1} \mathrm{I} 04$ | -89 31-90 50 | 26 58-27 07 | -90 10 | 2703 | 2 | 2 | -90 00 | 2652 |  |  |  |
| e 102 | 9001-90 02 | $4540-4606$ | 9002 | 4554 | 4 | 4 | 9000 | 4531 | $e: \overline{102}$ | 9000 |  |
| $e$ : 102 | -89 43-90 01 | 44 39-45 36 | -89 52 | 4507 | 2 | 2 | -90 00 | $4525 \frac{1}{2}$ | e: 102 | 9000 | $4428 \frac{1}{2}$ |
| p 113 | 57 26-58 11 | 38 15-39 15 | 5748 | 3847 | 4 | 2 | $5749 \frac{1}{2}$ | 3845 |  |  |  |
| q 112 | $5758-5833$ | 5015-50 18 | 5815 | 5017 | 4 | 2 | $5748 \frac{1}{2}$ | $5016 \frac{1}{2}$ |  |  |  |
| $q$ : $\overline{1} 12$ | $-5710-5740$ | $4933-5030$ | -5730 | 5001 | 3 | 2 | -5743 | 5012 |  |  |  |
| $\begin{array}{ll}n & 111\end{array}$ | 57-54-58 12 | 67 12-67 42 | 5803 | 6726 | 14 | 6 | 5747 | $6725 \frac{1}{2}$ | $z: \overline{1} 24$ |  |  |
| $n: \overline{111}$ | $-5740-5746$ | $6644-6724$ | -57 44 | 6706 | , | 2 | -57 44 ${ }^{\frac{1}{2}}$ | 6774 | z: 124 | 5720 | $6654 \frac{1}{2}$ |
| $r: \overline{123}$ | -38 $04-4031$ | $4641-4741$ | -39 01 | 4729 | 12 | 5 | -38 20 | $4727 \frac{1}{2}$ |  |  |  |
| ${ }^{*} \boldsymbol{\beta} \boldsymbol{I} 15$ | - | - | -61 12 | 2511 | 2 | 1 | -57 39 |  |  |  |  |
| ${ }^{h} \quad \overline{2} 14$ | - | - | -7240 | 5030 | 1 | 1 | -7228 | 4647 |  |  |  |
| ${ }^{*} \gamma 121$ | $3831-4042$ | 73 25-74 16 | 3941 | 7353 | 13 | 5 | - 3826 | 7301 |  |  |  |

[^0]The measurements of the six crystals are summarized in table 1, which gives the observed forms, the range of the measured twocircle angles, the resulting averages, and the calculated angles. To these are added the calculated angles of known forms which nearly coincide with different known forms when the $a$ - and $c$-axes are interchanged. Although the crystals measured are, like all herderites, only moderately good, it will be seen that the mean measured angles are consistently closer to the calculated angles in proper


Fig. 1. Herderite. Individual crystal from Topsham, Maine, with pronounced monoclinic development. Forms: $c(001), b(010), l(120), m(110), t(012), v(011)$, $s(021), \alpha(104)$ new, $n(111), r$ : (123), $\gamma(121)$ new.

Fig. 2. Herderite. Twin on (100) from Topsham, Maine. Forms: $c(001), m(110)$, $u(013), t(012), v(011), e(102), n(111), \beta$ ?(T15) new, $r:(123), \gamma(121)$ new.
position than to those resulting from misorientation. Furthermore, most of the forms found are already known in the position in which the crystals were measured, whereas in the alternative position many would give symbols corresponding to unknown forms. The proper orientation and consequently the remarkable development of the Topsham crystals is thus established geometrically. A determination of the optical orientation of one of the measured monoclinic individuals brought independent verification.

Figures 1, 2, and 3, illustrate the principal features of the new material. Figure 1 represents a monoclinic individual from Topsham, exhibiting the novel prismatic habit. The crystal is bounded mainly by $m(110)$, and the terminal forms $\alpha(\overline{1} 04)$ and $r:(\overline{1} 23)$. The prism $m(110)$ is the common prism of herderite. The negative orthodome $\alpha(\overline{1} 04)$ is a new form, and appears on this crystal and on another similar one as a large dull but plane face with measured angles agreeing well with the calculated values. The negative pyramid $r:(\overline{1} 23)$, a common form on herderite, is likewise dull and gives weak reflexions. The edges between the terminal forms and the prisms are truncated by small faces of the known forms: $c(001)$, $t(012), v(011), s(021), n(111)$, and $\gamma(121)$, which is a new form. The acute edges of the prism $m$ are truncated by narrow faces of $b(010)$ and $l(120)$. The new pyramid $\gamma(121)$ was observed on all the Topsham crystals and also on one of the crystals from Greenwood. On the Topsham crystals it occurred characteristically as two narrow faces in the zone [ $m v r$ :].

Figure 2 also illustrates a Topsham crystal developed prismatically like the one described above and twinned on the orthopinacoid. The prism zone is bounded by $m(110)$ only, while the termination is formed mainly by the faces of the clinodome v(011) in nearly parallel position on the two individuals. Indication of twinning is given by a deep re-entrant following the plane of (100) and dividing the termination symmetrically. The re-entrant is formed by badly etched and curved faces of $r:(\overline{1} 23)$ and $\beta(\overline{1} 15)$, a new form the symbol of which is regarded as doubtful since the surface gave very poor reflexions. Smaller faces of $c(001), u(013)$, $t(012), n(111)$, and the new form $\gamma(121)$ are also found on the terminations.

Penfield (1894) showed that the twinning of herderite can be referred to either $c(001)$ or $a(100)$ as the twinning plane, and figured a twin with hypothetical traces of both planes. All of the actual twins with visible re-entrants described by him indicated twinning on $c(001)$. Such twinning should give parallelism in the two clinodome zones, whereas twinning on $a$ should result in coincidence in the prism zones. Careful observations on the Topsham crystals showed that both the prism zones and the clinodome zones deviate slightly from exact parallelism. It therefore seems best to regard the composition plane (100) as the twin plane; the twinning thus becomes an example of the alternative and hitherto unobserved expression of Penfield's twin law.

Figure 3 shows a typical crystal from the new occurrence at Greenwood. As in most of the published figures of herderite, the form of the crystal is determined mainly by the clinodome zone. The forms observed on two crystals of this type are $c(001), a(100)$, $b(010), l(120), m(110), u(103), t(012), e(102), e:(\overline{1} 02), p(113)$, $q(112), q:(\overline{1} 12), n(111), n:(\overline{1} 11), r:(\overline{1} 23), h(\overline{2} 14), \gamma(121)$. The negative forms are all more or less etched and rounded, a common characteristic of herderite and further confirmation of the nonequivalence of the positive and negative forms, even though the angles are nearly alike.


Fig. 3. Herderite. Individual crystal from Greenwood, Maine, with orthorhombic appearance. Forms: $c(001), b(010), m(110), u(013), l(012), e(102), e:(\bar{T} 02)$, $p(113), q(112), q:(\overline{1} 12), n(111), n:(\overline{1} 11), r:(\overline{1} 23), \gamma(121)$ new.

The Greenwood crystals gave good angles in close agreement with the angles calculated from Penfield's elements; the angles measured on the Topsham specimens agree less closely. From the best measurements on the latter an axial ratio, which compares with earlier values as follows, was obtained:

| $a: b: c$ | $\beta$ |
| :---: | :--- |
| $0.6237: 1: 0.4255$ | $90^{\circ} 15^{\prime}$ (Yatsevitch, 1935) |
| $0.6246: 1: 0.4258$ | $\ldots \ldots$ (Dürrfeld, 1909) |
| $0.6308: 1: 0.4274$ | $90^{\circ} 06^{\prime}$ (Penfield, 1894) |
| $0.6206: 1: 0.4236$ | $90^{\circ} \quad$ (Dana, 1884) |

Since the measurements made in this study are less comprehensive than those of Penfield, the calculated angles are based on Penfield's measurements referred to new parameters as explained below.

In the monoclinic system a setting in which the clinoaxis is the axis of columnar development is ungainly and inconvenient. However, since columnar development may follow either the $a$-axis or the $c$-axis in herderite, nothing will be gained by a rotation of axes. In the adopted setting, therefore, the axial directions of the previous workers are retained, so that the figures present the same as-


Fig. 4. Herderite. Gnomonic projection of the accepted forms showing the pseudo-orthorhombic character of the species and the importance of the poles of $n(111)$, the preferred parametral plane, in the zonal network.
pect as those already published. A consideration of the symbols of the known forms of herderite in relation to the importance of the corresponding forms suggested a new choice of the unit pyramid that results in trebling the $c$-axis of Penfield. Goldschmidt (1897) already simplified the symbols of herderite by taking a $c$-axis equal to three-halves of Penfield's. Our choice of the unit pyramid, namely $n$ (111), the only pyramid found at every known herderite locality, results in further simplification as can be seen by comparing the lists of symbols for corresponding forms in the three settings in table 2. Furthermore, the gnomonic projection of the estab-
lished forms of herderite (figure 4), shows the importance of $n(111)$ as a zonal node and normal distribution of poles in radial zones.

The elements and symbols in the three settings are related by the following equations:

$$
\begin{aligned}
a: b: c(\text { G.M.Y. }) & =a: b: 2 c(\text { Goldschmidt }) & =a: b: 3 c(\text { Penfield }) \\
h k l \quad & =h k 2 l \quad & =h k 3 l \quad "
\end{aligned}
$$

A complete form list of herderite was compiled as a result of an examination of the published work, and is presented in table 2. In the list eleven forms are regarded as uncertain for the reasons given below. Three forms with highly complex symbols are omitted. The following are those considered uncertain:
$f(209)$; described as $f(203)$ by Dürrfeld (1909) with sign uncertain. Later (1910B) given as $f(\overline{2} 03)$. A minute face in poor zonal relation. Possibly the same as the new form from Topsham, $\alpha(\overline{1} 04)$.
$E(803) ; \epsilon(803)$; described without measurements as new forms $E(801)$ and $\epsilon(\overline{8} 01)$ by Dürrfeld ( 1910 A ).
$\beta$ (T15); described in this paper. "Badly etched and curved."
$g(114) ; g:(114)$; described as $g(334)$ by Dürreld (1909) with sign uncertain. Later ( 1910 B) given as $g(334)$. In poor zonal relation. Possibly the same as the new and uncertain form from Topsham, $\beta$ (T15).
$o(443)$; given as an orthorhombic form $o(441)$ by Haidinger (1828) and never observed again.
$y(133) ; y(\overline{1} 33)$; described as an orthorhombic form $y(131)$ by Dana (1884) from Stoneham, Maine, but not found again. In good zonal relation, but sign unknown.
$G(349)$; described as $g(343)$ by Ford (1911). "Striated and curved"; in poor zonal relation.
$H(135)$; described as $h(395)$ by Dürrfeld (1910 B). "Ein Produkt der Aetzung." In good zonal relation.
The following forms are neglected:
$(20.37 .0)=l(20.37 .0), \mathrm{D}$ ürrfeld (1909). "Uneben und matt." $(881)=p_{24}(24.24 .1)$, Dürrfeld (1909). Vicinal to (110).
$(11.22 .24)=(11.22 .8)$, Dürrfeld (1909). "Uneben und matt. Wahrscheinlich $x$ (362)."

The optical constants of the Topsham material were determined on the measured single crystal illustrated in figure 1, and on grains by the immersion method. The values obtained agree closely with those given by Penfield (1894), and are given below:
\(\left.\begin{array}{l}X(obtuse bisectrix)=1.591 <br>
Y(=b)=1.611 <br>

Z(acute bisectrix)=1.619\end{array}\right\} \pm 0.003\)$\quad$| $2 V=75^{\circ} \pm 5^{\circ} ; r>v$. |
| :--- |
| $Z: c$-axis $=3 \frac{1}{2}^{\circ}$. |

Table 2. Herderite. Distribution and Correlation of Forms

| Symbols <br> Dana <br> (1884) <br> Penfield <br> (1894) | Stone- ham $^{1}$ | Paris ${ }^{2}$ | $\begin{gathered} \mathrm{He}- \\ \text { bron }^{2} \end{gathered}$ | $\begin{gathered} \mathrm{Au} \\ \text { burn } \end{gathered}$ | Greenwood 4.5 | Top- sham |  | Symbols Goldschmidt (1897, 1918) | Letters \& Symbols Yatsevitch |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 001 | c | c | $c$ | $c$ | c | $c$ | $c$ | 001 | ${ }_{\text {c }} 0001$ |
| 010 | $b$ | $b$ | - | $b$ | $b$ | $b$ | - | 010 | b 010 |
| 100 | - | $a$ | - | - | $a$ | - | $a$ | 100 | a 100 |
| 130 | ${ }^{\mu}$ | - | - | - | - | - | - | 130 | - 130 |
| 120 | $l$ | - | - | - | $l$ | $l$ | $l$ | 120 | $l \mid 120$ |
| 110 | $m$ | $m$ | $m$ | $m$ | $m$ | $m$ | $m$ | 110 | $m 110$ |
| 011 | u | - | - | - | u | $u$ | - | 023 | $\begin{array}{ll}u & 013\end{array}$ |
| 032 | $t$ | $t$ | - | $t$ | $t$ | $t$ | $t$ | 011 | $t \quad 012$ |
| 031 | $v$ | $v$ | - | $v$ | - | $v$ | $v$ | 021 | ข 011 |
| 061 | $s$ | $s$ | - | - | - | $s$ | - | 041 | $s \quad 021$ |
| 203 | - | - | - | - | - | - | $f$ | 409 | $f$ 209? |
| 304 | - | - | - | - | - | $\alpha$ | - | 102 | ${ }^{*} \alpha$ I04 |
| 101 | d | - | - | - | - | - | - | 203 | d 103 |
| 101 | - | - | - | - | - | - | $\delta$ | 203 | ¢ 103 |
| 302 | $c$ | $e$ | - | $\varepsilon$ | $e$ | $e$ | $e$ | 101 | $e \quad 102$ |
| 302 | ${ }^{\prime}$ : | - | - | - | $e$ : | - | - | 101 | e: 102 |
| 301 | - | - | - | $d$ : | - | - | - | 201 | d: 101 |
| 801 | - | - | - | - | - | - | E | 16.0.3 | E 803? |
| $\overline{801}$ | - | - | - | - | - | - | $\epsilon$ | 16.0.3 | $\epsilon{ }^{\text {c }}$ 03? |
| 112 | - | ' | - | $r$ | - | - | - | 113 | $r 116$ |
| $\overline{3} 35$ | - | - | - | - | - | $\beta$ | - | 225 | ${ }^{*} \beta$ I15? |
| 334 | - | - | - | - | - | - | $g$ | 112 | $g$ 114? |
| 334 | - | - | - | - | - | - | $g$ | I12 | $g$ : I14? |
| 111 | $p$ | - | - | - | $p$ | - | $p$ | 223 | ¢ 113 |
| 111 | - | - | - | - | - | - | $p$ : | 223 | p: 113 |
| 332 | $q$ | $q$ | $q$ | $q$ | $q$ | - | $q$ | 111 | $q \quad 112$ |
| 332 | $q$ : | - | - | - | $q$ : | - | $q$ : | 111 | $q$ : I12 |
| 331 | $n$ | $n$ | $n$ | $n$ | $n$ | $n$ | $n$ | 221 | $n 111$ |
| 331 | $n$ : | $n$ : | - | $n$ : | $n$ : | - | $n$ : | 221 | $n$ : I11 |
| 441 | - | - | - | - | - | - | 。 | 883 | - 443? |

Table 2-(Continued)

| Symbols <br> Dana <br> (1884) <br> Penfield <br> (1894) | Stone ham ${ }^{1}$ | Paris ${ }^{2}$ | Hebron ${ }^{2}$ | $\begin{aligned} & \mathrm{Au}- \\ & \text { burn }^{3} \end{aligned}$ | Green wood 4,5 | Topsham ${ }^{5}$ | Ep-prechtstein ${ }^{6}$ Ehrenfrieders dorf | Symbols Goldschmidt (1897, 1918) |  <br> Symbols <br> Yatse- <br> vitch |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 122 | - | $k$ | - | - | - | - | - | 123 | k 126 |
| 392 | - | - | - | - | - | - | $h$ | 265 | H 135? |
| 3.12 .4 | - | w | - | - | - | - | - | 142 | w 144 |
| 364 | - | - | - | - | z: | - | - | 122 | s: 124 |
| 394 | - | ${ }_{3}$ | - | - | - | - | - | 132 | z 134 |
| 121 | - | - | - | $r$ : | $r$ : | $r:$ | $r$ : | 243 | $r$ : 123 |
| 343 | - | - | - | g | - | - | - | 689 | $G$ 349? |
| 131 | $y$ | - | - | - | - | - | - | 263 | $y$ 133? |
| 131 | $y$ | - | - | - | - | - | - | 263 | $y$ : 133? |
| 634 | - | - | - | $h$ | $h$ | - | - | $\overline{212}$ | h 214 |
| 362 | $x$ | - | - | - | - | - | $x$ | 121 | $x \mathrm{I} 22$ |
| $\overline{2} 41$ | - | - | - | - | - | - | $i$ | 483 | $i \quad 243$ |
| 361 | - | - | - | - | $\gamma$ | $\gamma$ | - | 241 | ${ }^{*} \gamma \quad 121$ |
| 391 | - | - | - | - | - | - | $p$ : | $\overline{2} 61$ | $P \overline{1} 31$ |

* New form. German form letters taken from the literature are consistently replaced by the corresponding English letters followed by a colon.
${ }^{1}$ Dana (1884), Penfield (1894).
${ }^{2}$ Penfield (1894).
${ }^{3}$ Penfield (1894), Ford (1911).
${ }^{4}$ Penfield (1894, Yatsevitch (1935).
${ }^{5}$ Yatsevitch.
${ }^{6}$ Haidinger (1828), Dürrfeld (1909-1910).

In conclusion, an angle table for herderite is presented in a form which combines the requirements of both single-circle and twocircle goniometry. The angles $\phi_{2}, \rho_{2}$, are two-circle angles referred to the $b$-axis as pole, while the angles A, B, C are $h k l:(100)$, $h k l:(010), h k l:(001)$ respectively. This method of presentation was described in a recent paper by Peacock (1934).

Table 3．Herderite－－ $\mathrm{CaBe}\left(\mathrm{OH}, \mathrm{F}_{\mathrm{F}} \mathrm{PO}_{4}\right.$

| $\begin{aligned} & \text { Monoclinic: } a: b: c=0.6307: 1: 1.2822 ; \beta=90^{\circ} 06^{\prime} . \\ & p_{0}: q_{0}: r_{0}=2.0330: 1.2822: 1 ; \mu=89^{\circ} 54^{\prime} . \\ & r_{2}: p_{2}: q_{2}=1.5598: 1.5855: 1 . \\ & p_{0}=2.0331, q_{0}=1.2822 ; x_{0}{ }^{\prime}=0.0017 . \end{aligned}$ |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Forms | $\phi$ | $\rho$ | $\phi_{2}$ | $\rho_{2}=B$ | C | A |
| c 001 | $90^{\circ} 00^{\prime}$ | $0^{\circ} 06^{\prime}$ | $89^{\circ} 54^{\prime}$ | $90^{\circ} 00^{\prime}$ | $0^{\circ} 00^{\prime}$ | $89^{\circ} 54^{\prime}$ |
| b 010 | 000 | 9000 | － | 000 | 9000 | 9000 |
| a 100 | 9000 | 9000 | 000 | 9000 | 8954 | 000 |
| ${ }_{\mu}^{\mu} 130$ | 27 51震 | 9000 | 000 | $2751 \frac{1}{2}$ | 8957 | $6208 \frac{1}{2}$ |
| $l 120$ | $3824 \frac{1}{2}$ | 9000 | 000 | $3824 \frac{1}{2}$ | $8956 \frac{1}{2}$ | $5135 \frac{1}{2}$ |
| $m 110$ | 57 45⿸⿻一丿工 | 9000 | 000 | $5745 \frac{1}{2}$ | 8955 | $3214 \frac{1}{2}$ |
| $u 013$ | 014 | $2308 \frac{1}{2}$ | 8954 | $6651 \frac{1}{2}$ | $2302 \frac{1}{2}$ | $8954 \frac{1}{2}$ |
| $t 012$ | $009 \frac{1}{2}$ | 3240 | 8954 | 5720 | 3240 | 8955 |
| ข 011 | $004 \frac{1}{2}$ | 5203 | 8954 | 3757 | 5203 | $8956 \frac{1}{2}$ |
| $s \quad 021$ | $002 \frac{1}{2}$ | 6842 | 8954 | 2118 | 6842 | $8958 \frac{1}{2}$ |
| ＊$\alpha 104$ | －90 00 | 2652 | 11652 | 9000 | 2658 | 11652 |
| d 103 | 9000 | $3411 \frac{1}{2}$ | $5548 \frac{1}{2}$ | 9000 | $3405 \frac{1}{2}$ | $5548 \frac{1}{2}$ |
| $\delta 103$ | －9000 | $3403 \frac{1}{2}$ | $12403 \frac{1}{2}$ | 9000 | $3409 \frac{1}{2}$ | $12403 \frac{1}{2}$ |
| e 102 | 9000 | 4531 | 4429 | 9000 | 4525 | 4429 |
| $e: \overline{1} 02$ | －9000 | $4525 \frac{1}{2}$ | $13525 \frac{1}{2}$ | 9000 | $4531 \frac{1}{2}$ | $13525 \frac{1}{2}$ |
| $d: \overline{101}$ | －90 00 | $6347 \frac{1}{2}$ | 153 471 | 9000 | $6353 \frac{1}{2}$ | $15347 \frac{1}{2}$ |
| $r 116$ | 57 531 | $2154 \frac{1}{2}$ | $7111 \frac{1}{2}$ | 7834 | $2149 \frac{1}{2}$ | $7134 \frac{1}{2}$ |
| p 113 | $5749 \frac{1}{2}$ | 3845 | $5548 \frac{1}{2}$ | 7032 | 3840 | $5800 \frac{1}{2}$ |
| $p$ ： 113 | －57 412 | 3839 | $12403 \frac{1}{2}$ | 7030 | 3844 | 12152 |
| $q \quad 112$ | $5748 \frac{1}{2}$ | $5016 \frac{1}{2}$ | 4429 | $6548 \frac{1}{2}$ | 5011 | 4924 |
| $q$ ：$\overline{1} 12$ | －57 43 | 5012 | $13525 \frac{1}{2}$ | $6546 \frac{1}{2}$ | 5017 | $13030 \frac{1}{2}$ |
| $n 111$ | 5747 | $6725 \frac{1}{2}$ | $2610 \frac{1}{2}$ | $6030 \frac{1}{2}$ | $6720 \frac{1}{2}$ | $3837 \frac{1}{2}$ |
| $n$ ：I11 | －57 44 ${ }^{\frac{1}{2}}$ | 6724 | 153 471 | $6028 \frac{1}{2}$ | 6729 | $14119 \frac{1}{2}$ |
| k 126 | 3833 | $2839 \frac{1}{2}$ | $7111 \frac{1}{2}$ | $6758 \frac{1}{2}$ | $2835 \frac{1}{2}$ | $7236 \frac{1}{2}$ |
| w 144 | $2141 \frac{1}{2}$ | 5404 | $6258 \frac{1}{2}$ | 4112 | 5402 | $7235 \frac{1}{2}$ |
| $z: \overline{1} 24$ | －38181 | 3915 | 11652 | 6014 | 3915 | $11305 \frac{1}{2}$ |
| z 134 | －27 46⿺𠃊 | 4723 | 11652 | 49 22 $\frac{1}{2}$ | 4726 | $11003 \frac{1}{2}$ |
| $r: 123$ | －38 20 | $4727 \frac{1}{2}$ | $12403 \frac{1}{2}$ | $5441 \frac{1}{2}$ | $4731 \frac{1}{2}$ | $11711 \frac{1}{2}$ |
| h ${ }^{2} 14$ | －72 28 | 4647 | $13525 \frac{1}{2}$ | 7719 | $4652 \frac{1}{2}$ | 13401 |
| $x$ 122 | －38 211 | 5833 | $13525 \frac{1}{2}$ | 4801 | 5832 | 12158 |

Table 3-(Continued)

| Forms | $\phi$ | $\rho$ | $\phi_{2}$ | $\rho_{2}=B$ | C | A |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| i 243 | $-3822 \frac{1}{2}$ | 6522 | $14332 \frac{1}{2}$ | 4433 | $6525 \frac{1}{2}$ | 12421 |
| ${ }^{*} \gamma 121$ | 3826 | 7301 | $2610 \frac{1}{2}$ | 4129 | 7257 | $5331 \frac{1}{2}$ |
| $P \mathrm{I} 31$ | $-2750 \frac{1}{2}$ | 7703 | $15347 \frac{1}{2}$ | 3029 | 7706 | $11704 \frac{1}{2}$ |

* New form.


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[^0]:    * New form.

