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## INTRODUCTION

Tarbuttite, a basic zinc phosphate, was first described by Spencer (1907, 1908). His crystals were for the most part composed of subparallel groups with individual forms usually striated and rounded, with few well-defined faces in the primary zones so that, to use his own words, "the calculations are all the more awkward . . . and the elements given below can only be considered as a first approximation." Rosický (1913) adopted Spencer's setting and measured a large number of crystals on which he found 17 new forms but did not recalculate the elements.

The stereographic projection accompanying Spencer's paper shows a large obliquity of the base, a scarcity of forms in the vertical zone and several form-rich pyramidal zones. These facts suggested a search for a possible better choice of elements. To this end a complete morphological investigation together with an x-ray determination of the lattice constants was undertaken, the results of which appear in this paper.

## MORPHOLOGY

A number of matrix specimens of tarbuttite from the type locality, Broken Hill mines, N. W. Rhodesia, now in the Harvard Mineralogical Museum, were carefully examined for suitable crystals. One superb specimen (Harvard number 92882) was found consisting of a matrix of black stalactitic limonite thickly sprinkled with a large number of colorless, transparent crystals varying in size from 0.1 to 1.0 millimeter. The faces were bright, sharp and free from striations. Their habit, short prismatic approaching pseudoisometric, presented considerable difficulty in the choice of the prismatic zone.

The crystals are usually attached to the matrix on a plane nearly parallel to the perfect cleavage. The choice of a prismatic zone was made difficult in these crystals through the absence of a pronounced direction of elongation and by the presence of large faces of what proved to be forms of highly complex indices (forms G and E of figure 2). But by setting the perfect cleavage ( $\{001\}$  of Spencer's position) vertical and by selecting the strongest zone of which it formed a part as the prism zone, a satisfactory orientation was secured. Measurements being made on the two-circle goniometer with this zone vertical, a gnomonic projection was obtained which is shown in figure 1. In this projection the choice of b[010] normal to the cleavage is obvious. For a[100] the selec-



tion of either [cf] or [cM] is indicated; they proved by calculation to give essentially equal periods. The choice leaned toward the more pronounced zone contained in [cf]; this choice was found to lead to simpler indices and was therefore taken as [100].

Figure 1 is the gnomonic projection of the accepted forms of tarbuttite on a plane normal to the chosen vertical axis. The gnomonic plane is also considered as the first layer |hk1| of the reciprocal lattice. The vertical planes (hk0) are represented by radial lines drawn from  $c\{001\}$  to (hk1), the point (hk1) being inserted as a large blank circle,  $m \ b \ k \ M \ v$ , when it does not represent a known terminal form. These radial lines are thus normal to their respective vertical planes, and their lengths are inversely proportional to the spacings and reticular densities of the corresponding planes in the direct lattice.<sup>1</sup>

The points marked by large filled circles, c f Z s t W l r h u i, are nodes of the reciprocal lattice in the first layer and their spacings define the lattice translations. These face poles may be considered as actually in the plane of the gnomonic projection. The small blank circles, G P FB N H p n q o E, represent terminal planes which lie on higher lattice layers (*hkn*) and occupy fractional positions on the gnomonic projection. The representative lattice cell, therefore, may be defined as that cell whose respective reciprocal lattice points, either present or implied, are the three non-colinear points nearest the origin. The point nearest the center c represents the axial plane (001); the first layer point nearest c, namely b, is taken as (011); the next nearest not in zone [cb], namely f, as (101).

Figure 2 is a typical crystal of tarbuttite in normal position. Figure 2a is a crystal of tarbuttite after Spencer, redrawn in normal position.

The most prominent forms in the vertical zone are  $a\{100\}$  and  $b\{010\}$ . The terminal planes are unusually well developed and give remarkably perfect signals. The largest and most frequently observed forms are  $c\{001\}$ ,  $G\{1.6.23\}$ ,  $s\{121\}$ ,  $Z\{1\overline{2}1\}$ ,  $W\{\overline{1}11\}$ ,  $l\{\overline{1}21\}$ ,  $E\{\overline{347}\}$ ,  $u\{\overline{11}1\}$ .

<sup>1</sup> The obliquity of the base is so small that the large blank circles, which would normally appear on the reciprocal lattice projection of the zero layer-line slightly offset from the net intersections, are placed on these intersections to avoid confusion.

FIG. 1. Tarbuttite: gnomonic projection of the accepted forms.

FIG. 2. Tarbuttite: typical doubly terminated crystal from Broken Hill, Northern Rhodesia.

FIG. 2a. Tarbuttite: crystal drawing in new position after Spencer.

FIG. 3. Tarbuttite: relation of Spencer's setting to that of the new position.

FIG. 4. Tarbuttite: stereographic projection of the accepted forms.

FIG. 5. Tarbuttite: stereographic projection of the optical orientation and the position of the optic axes. These appeared on nearly every crystal measured. The new form  $q\{\overline{102}\}$  was observed on three crystals as a small face in good position.

The singular development of the forms  $G\{1.6.23\}$  and  $E\{\overline{347}\}$  is a unique feature of these crystals. On the eleven crystals employed for calculation, G was observed eight times and E ten times. Their positions in the projection are good and their measured values agree well with those calculated. Added evidence of their rationality is obtained by zonal calculation. The face pole G lies at the intersection of two zones  $[1\overline{41}]$  defined by the face poles  $\{\overline{101}\}$  and  $\{212\}$ , and  $[\overline{610}]$  defined by  $\{001\}$  and  $\{163\}$ ; the indices of this zone intersection are  $\{1.6.23\}$  which is the symbol determined for G. Similarly, E lies at the intersection of the zone  $[4\overline{30}]$  passing through the face poles  $\{001\}$ ,  $\{\overline{343}\}$ , and the zone [111] containing  $\{101\}$ ,  $\{1\overline{21}\}$ ; the symbol of the intersection is  $\{\overline{347}\}$ , which is the symbol of E. The comparatively simple indices of the zones passing through G and E may be taken as confirming their rational character.

Rosický observed these two forms and gave them the indices  $G\{\overline{5}59\}$ ,  $E\{\overline{3}84\}$ , which in the new position correspond to  $\{0.13.10\}$ ,  $\{\overline{5},\overline{6},11\}$ . These are but approximately similar to indices derived from the writer's observations. Comparison of calculated angles for the two sets of symbols (table 1) shows similarity for E and an unexplained gross discrepancy for the azimuth angle of G.

# Table 1. Tarbuttite: Comparison of the Sets of Indices of G and E

	$\phi$	ρ
G {0.13.10}	7°39′	11°00′
{1.6.23}	20 35	10 47
$E \{ 5.6.11 \}$	$-139\ 21\frac{1}{2}$	31 58
$\{\overline{347}\}$	$-141 56\frac{1}{2}$	31 421

Rosický's crystals were of poor quality, which undoubtedly prevented him from determining the true indices of these two forms. Due to the remarkable perfection of development of these forms on the crystals studied here and the excellence of their position on the gnomonic projection, it was decided to adopt new indices while retaining the old letters.

Table 2 gives the measured maximum range, the best measured mean, the calculated  $\phi$  and  $\rho$  of the forms, together with the number of times each form was observed. The perfection of the crystals studied is well brought out by the close agreement of the mean measured and the calculated values of  $\phi$  and  $\rho$ .

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ated	$\begin{array}{c} 1^{\circ} 28\frac{1}{2},\\ 90\ 00\\ 90\ 00\end{array}$	9999 9999 9999	90 00 45 35 17 04	$\begin{array}{c} 25 & 18\frac{1}{2} \\ 44 & 09 \\ 71 & 19\frac{1}{2} \end{array}$	$\begin{array}{c} 10 \ 47\frac{1}{2} \\ 61 \ 26 \\ 15 \ 59\frac{1}{2} \end{array}$	$\begin{array}{c} 24 57_{\frac{1}{2}} \\ 53 41 \\ 25 31_{\frac{1}{2}} \end{array}$	$\frac{44}{52} \frac{21\frac{1}{2}}{59}$ 70 34	$31 \ 42\frac{1}{2}$	
Calcul	$\begin{array}{c} \phi \\ 87^{\circ}00' \\ 0 & 00 \\ 72 & 19 \end{array}$	$\begin{array}{c} 45 & 35_{\overline{2}} \\ 90 & 39_{\overline{2}} \\ 108 & 52 \end{array}$	$\begin{array}{c} 123 \ 54\frac{1}{2} \\ 72 \ 41 \\ -108 \ 54 \end{array}$	$-\frac{108}{-108} \frac{28_{2}}{04}$ $-\frac{107}{37}$	$\begin{array}{c} 20 & 35 \\ 32 & 02 \\ 131 & 14\frac{1}{2} \end{array}$	$\begin{array}{c} 132 \ 42\frac{1}{2} \\ 134 \ 15\frac{1}{2} \\ - \ 69 \ 58\frac{1}{2} \end{array}$	$\begin{array}{rrrr} - & 70 & 41 \\ - & 44 & 06 \\ - & 95 & 39\frac{1}{2} \end{array}$	$-14156\frac{1}{2}$	
t Mean	$\begin{array}{c} 1^{\circ}{}^{P}_{38'}\\ 90\ 00\\ 90\ 00\end{array}$	00 06 00 06	90 00 45 34 16 57	25 03 44 07 71 21	$\begin{array}{c} 11 & 00 \\ 61 & 34 \\ 15 & 50 \end{array}$	24 52 53 40 25 34	44 26 53 02 70 30	31 37	_
Bes Measured	$\begin{array}{c} \phi \\ 87^{\circ}17' \\ 0 & 00^{\frac{1}{2}} \end{array}$	$\begin{array}{c} 45 \\ 90 \\ 45 \\ 109 \\ 04 \end{array}$	$^{123}_{-108}$ 56 108 00	-108 11 -107 49 -107 44	$\begin{array}{c} 20 & 30 \\ 31 & 59 \\ 130 & 35 \end{array}$	$     \begin{array}{r}       132  40 \\       134  13 \\       -  69  15     \end{array} $	$\begin{array}{rrrr} - & 70 & 35 \\ - & 44 & 11 \\ - & 95 & 36 \end{array}$	-141 33	
wred Range	$\begin{array}{c}1^{\circ}47, \stackrel{\rho}{-}1^{\circ}30'\\90^{\circ}00'\\90&00\end{array}$	90 00 90 00 90 00	90 00 42 56 -45 20 17 18 -16 50	25 12 -24 57 44 11 -43 53 71 38 -71 18	11 08 -10 57 61 55 -61 26 15 57 -15 06	25 04 -24 34 53 44- 53 23 25 47 -25 13	$\begin{array}{c} 44 \ 41 \ -44 \ 25 \\ 53 \ 25 \ -53 \ 00 \\ 70 \ 30 \end{array}$	31 40 -31 30	
Meas	$\phi$ - 82°30' - 72 15	$\begin{array}{rrrr} - & 43 & 39 \\ - & 90 & 33 \\ - & 108 & 47 \end{array}$	$\begin{array}{rrrr} 23 & 56 \\ - & 72 & 06 \\ - & 107 & 52 \end{array}$	107 37 107 38 107 08	$\begin{array}{rrrr} - & 20 & 15 \\ - & 31 & 14 \\ - & 129 & 50 \end{array}$	$\begin{array}{rrrr} - & 132 & 03 \\ - & 134 & 07 \\ & 68 & 40 \end{array}$	$\begin{array}{c} & 69 & 47 \\ & 43 & 37 \\ 36 & 36 \end{array}$		
	90°40′ 359 45 72 28	46 00 91 10 109 15	-108 172 41	$-108 19 \\ -107 51 \\ -108 18$	$\begin{array}{c} 20 58 \\ 32 01 \\ 130 39 \end{array}$	$\begin{array}{c} 132 \ 51 \\ 134 \ 29 \\ - \ 69 \ 18 \end{array}$	-7046 -4436 -95	-141 45	
es									
Fac	222	4110	110		00 11/14	211		10	
rm.	001 010 100	110 2T0 1T0	230 101 103	102 101 301	1.6.23 121 125	$\frac{123}{121}$	$\frac{111}{321}$	347	form.
Fo	a a c	m k M	f v	*d*	PSG	RZZ	Al	E	* New

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## CORRELATION OF SETTING

The relation of Spencer's setting to the writer's is shown in figure 3. From the figure, the form-to-form transformation formula can be directly derived when it is recognized that Spencer's c is one-half Richmond's b, so that [010] must be multiplied by 2.

Spencer	Richmond
a'100(100)	$1\overline{2}1(\overline{1}2\overline{1})$
b 010	<u>1</u> 11
c 001	020

The transformation formula is, therefore,  $\overline{110}/212/\overline{110}$ .

Table 3 shows the forms of tarbuttite observed by Spencer, Rosický and'Richmond. The forms represented by a letter in the column *Richmond* are the forms observed by him and accepted as established. Certain additional forms observed by Spencer or Rosický but not by

Form	Richmond	Spencer-Rosický	Form	Richmond	Spencer-Rosický
001	С	g 221 g	141	t†	t 103 t
010	b	c 001 c	412	$B^{\dagger}$	— 314 B
100	a	$d$ $\overline{2}\overline{2}3$ $d$	125	P	- 321 P
110	m	$-\overline{225}$ v	123	F	— 421 F
430	2	$- \overline{449} L$	543	2	— 825 M
210	2	- 112 x	$1\overline{2}1$	Z	a 100 a
210	b	k TT1 $k$	9.10.15	2	
110	M	$e \frac{111}{221} e$	T12	N	261 N
10 11 0	2	$-\frac{552}{552}$ z	8.13.10	$H^{\dagger}$	— <b>T</b> 93 <i>H</i>
10.11.0		001			
$2\overline{3}0$	v	m 110 —	Ī11	W	b 010 $b$
074	2	— 445 C	595	pt	— 052 <i>p</i>
031	?		T21	l	l 021 l
0 11 2	2	$-1\overline{1}5$ D	311	r	$r = \overline{243}$ r
101	f	$f = \overline{101} f$	321	2	
101	n	$- \overline{201} n$	123	01	0 121 -
100					
102	$q^*$		5.6.11	2	— 384 E
101	ĥ	h  021  h	347	E	
301	ĩ	$i$ $\overline{12}2$ $i$	111	и†	u 011
1.6.23	G				
0.13.10	2	<u>5</u> 59 G			
121	S	s 102 s			

TABLE 3. TARBUTTITE: CORRELATION OF FORM LETTERS

\* New form.

			Triclinic; pin	acoidal-T		
		a:b:c=0.6296:	1:0.5971; $\alpha = 8$	$9^{\circ}37\frac{1}{2}', \beta = 91^{\circ}2$	$28\frac{1}{2}', \gamma = 107^{\circ}41$	,
	po	$q_0:r_0=0.9954:0$	$0.6265:1; \lambda = 8$	$9^{\circ}55\frac{1}{2}', \mu = 88^{\circ}$	$34\frac{1}{2}', \nu = 72^{\circ}19'$	
		$p_0' = 0.9957$	$q_0' = 0.6267; a$	$x_0' = 0.0258, y_0$	'=0.0014	
	Form	ф	0	4	В	С
		*	P			
C	001	87°00′	$1^{\circ}28\frac{1}{2}'$	88°34½′	89°55½′	
b	010	0 00	90 00	72 19	_	89°55½′
a	100	72 19	90 00		72 19	$88\ 34\frac{1}{2}$
m	110	45 351	90 00	26 43 <sup>1</sup> / <sub>2</sub>	45 35 <del>1</del>	88 531
k	210	90 391	90.00	18 201	90 39 <del>1</del>	88 311
M	110	108 52	90 00	36 33	108 52	88 37 <sup>1</sup> / <sub>2</sub>
	220	102 541	00.00	54 251	102 541	00 10
v F	200	123 342	90 00 4E 2E	31 33 <sup>2</sup>	123 342	00 49 11 16
J	101	12 41	45 55	44 25	11 43 <del>2</del> 05 271	10 201
n	103	-108 54	17 04	107 04	95 212	18 29 2
*q	<b>T</b> 02	$-108\ 28\frac{1}{2}$	25 181	115 18 <del>1</del>	97 47	26 44
h	101	-10804	44 09	134 09	$102\ 28\frac{1}{2}$	$45 \ 34\frac{1}{2}$
i	301	-107 37	$71 \ 19\frac{1}{2}$	$161 \ 19\frac{1}{2}$	106 40	$72 \ 45\frac{1}{2}$
G	1 6 23	20.35	10 471	83 201	70 541	10 17
S	121	32.02	61 27	47 56	41 53	60 35±
t	141	$19\ 07\frac{1}{2}$	71 25	55 24	26 25	70 52
D	110					(A. 66.1
B	412	$64\ 26\frac{1}{2}$	64 52	$26\ 15\frac{1}{2}$	$67 \ 00\frac{1}{2}$	63 30 1/2
P	125	131 14 ±	15 59 1	81 49 1	100 49 ±	14 57 =
F	123	$132 \ 42\frac{1}{2}$	$24\ 57\frac{1}{2}$	77 58	106 37 ½	23 561
Ζ	$1\overline{2}1$	$134\ 15\frac{1}{2}$	53 41	67 44	124 13	$52 \ 41\frac{1}{2}$
N	<b>1</b> 12	$-6958\frac{1}{2}$	25 311	109 56	81 31	26 53
H	8.13.10	$-5156\frac{1}{2}$	42 $57\frac{1}{2}$	112 $33\frac{1}{2}$	$65 \ 09\frac{1}{2}$	44 05
W	T11	- 70 41	44 211	124 27	76 371	45 44
b	505	- 48 081	51 06	124 27	58 43	51 56
P 1	T21	-40.002	52 50	110 102	55 011	53 571
v	161	TIUU	34 37	110 402	55 012	00 012
r	311	- 95 39 <del>1</del>	70 34	157 16	95 20	72 021
0	123	-150 41	30 40 1	111 541	116 25	30 42 1
E	347	$-141 56\frac{1}{2}$	$31 \ 42\frac{1}{2}$	$115 \ 44\frac{1}{2}$	$114\ 26\frac{1}{2}$	32 42
11	111	135 00	50.27	124 40	124 17	52 121
ev	TTT	100 09	34 31	134 47	144 1/	JJ TJ 2

# TABLE 4. TARBUTTITE: Zn<sub>2</sub>PO<sub>4</sub>(OH)

\* New form.

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Richmond are indicated by a dagger after the letter. Forms not observed by Spencer or Rosický are followed by a dash. Forms represented by a ? in column *Richmond* were discredited by him for one or more of the following reasons: (1) observed but once and in poor position, (2) calculated values not in agreement with actual measurements, (3) complexity of symbols and poor position.

Using the method outlined by Wolfe (1937), we transform Spencer's elements to those in the writer's setting and obtain: a:b:c=0.6332:1: 0.6047;  $\alpha = 89^{\circ}14\frac{1}{2}'$ ,  $\beta = 92^{\circ}26\frac{1}{2}'$ ,  $\gamma = 108^{\circ}00'$ .

The elements from the new measurements are: a:b:c=0.6296:1:0.5971;  $\alpha = 89^{\circ}37\frac{1}{2}'$ ,  $\beta = 91^{\circ}28\frac{1}{2}'$ ,  $\gamma = 107^{\circ}41'$ .

The two sets of elements are not in close agreement. Spencer states that his elements are only "a first approximation," being derived from crystals unsuitable for accurate measurements. The crystals here studied are of such exceptional quality that measured and calculated values agree closely. The new elements are therefore adopted and employed to derive the formal angle table for the accepted forms of tarbuttite in the new setting (table 4).

Figure 4 is a stereographic projection of the accepted forms of tarbuttite.

#### Optics

The optical properties of tarbuttite were determined on a small crystal mounted on the universal stage, and by the immersion of crystal fragments. The optical data are summarized in table 5.

TABLE 5 TARRITTE OFFICAT DATA

	LADDE V.	TARDOTTID.	Of HOLD DIRE	
	φ	ρ	n(Na)	
X	7°	58°	1.660	negative
Y	159	25	$1.705 \pm 0.003$	$2V = 50^{\circ}$
Z	-86	80	1.713	no pleochroism

The optical orientation and the positions of the optic axes in relation to the principal planes of the crystal are represented stereographically in figure 5.

#### PSEUDOSYMMETRY

The new setting of tarbuttite brings out certain pseudosymmetrical elements which are graphically illustrated in figures 1 and 6. In figure 1 the dotted lines outline one pseudoisometric cell. The direction of the unit prism m is approximately in the 45° position and k at 90°; c is close to the center of the projection. Figure 6 is a clinographic drawing of the direct lattice cell of tarbuttite (small) and shows the relation of the unit cell to that of the pseudoisometric (heavy dashes).

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# STRUCTURAL LATTICE

X-ray measurements were made on a single carefully selected crystal 0.5 millimeter in the longest direction. The six lattice elements were



FIG. 6. Tarbuttite: relation of the several direct lattice cells.



FIG. 7. Tarbuttite: rotation photograph about the c-axis; unfiltered copper radiation.

determined by rotation and Weissenberg photographs of the zero and first layer-lines rotating the crystal successively about the three chosen crystallographic axes. Excellent photographs were obtained with copper radiation. The films were practically unfogged by scattered radiation due to the shortness



FIG. 8. Tarbuttite; zero layer-line photograph about c-axis; unfiltered copper radiation.

of the exposure time. The diffraction spots were exceptionally sharp so that it was possible to measure and calculate the lattice elements with considerable accuracy.



FIG. 9. Tarbuttite: first layer-line photograph about c-axis; copper radiation; nickel filter.

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The exceptional quality of the photographs is shown in figures 7, 8, and 9. The rotation and zero layer-lines were taken without a filter (figures 7, 8), while a nickel filter was used for the first layer-line (figure 9). The zone lines have been drawn in on the zero and first layer line photographs and the intersection of the zone lines with the axial directions indexed. These photographs were all taken about the *c*-axis.

The zero layer-line photographs taken about the three zone axes gave three pairs of values for the spacings of the axial planes. The reciprocal axial angles were determined by lattice spacing measurements along lattice cell diagonals and by triangulation calculations. The lattice constants measured and computed are shown in table 6.

From rotation photographs	From Weissenberg photographs			
$     \begin{array}{r} \hat{A} \\     a_0 = 8.062 \\     b_0 = 12.86 \\     c_0 = 7.687   \end{array} $	$d_{100} = 7.706$ $d_{010} = 12.29$ $d_{001} = 7.685$	$\alpha^* = 89^{\circ}51'$ $\beta^* = 88\ 27$ $\gamma^* = 72\ 14$	$ \overset{\text{A}}{a_0} = 8.097 \\     b_0 = 12.91 \\     c_0 = 7.688 $	$\begin{array}{l} \alpha = 89^{\circ}34\frac{1}{2}' \\ \beta = 91 \ 35\frac{1}{2} \\ \gamma = 107 \ 47 \end{array}$

TABLE 6. TARBUTTITE: STRUCTURAL LATTICE CONSTANTS

A study of the lattice parameters shows that the three chosen axes of rotation, which were previously taken as the three crystallographic axes, are also the three shortest noncoplanar lattice periods.

The direct lattice elements calculated from the Weissenberg photographs give the following ratio, which agrees well with that computed from the geometrical elements.

$$\begin{array}{l} a_0:b_0:c_0 = 0.6271:1:0.5957; \quad \alpha = 89^\circ 34\frac{2}{2}', \quad \beta = 91^\circ 37\frac{1}{2}', \quad \gamma = 107^\circ 47' \\ a:b:c = 0.6296:1:0.5971; \quad \alpha = 89^\circ 37\frac{1}{2}', \quad \beta = 91^\circ 28\frac{1}{2}', \quad \gamma = 107^\circ 41' \end{array}$$

The relation of Spencer's lattice cell (large cell with solid and dotted lines) to that in the new position is shown in figure 6.

The method outlined by Wolfe and used to transform Spencer's elements to those in the new position may also be employed to calculate the edge lengths of the Spencer cell in the new position as well as the volume of that cell. This method makes use of the transformation formula Spencer to Richmond ( $\overline{110}/212/\overline{110}$ ) and the absolute lengths of the chosen unit cell. Matrix calculation of the Spencer to Richmond transformation together with translation formulae give the following relationship:

a'	$[100] = [\overline{2}0\overline{2}] = 22.03$ Å	$a_0 =$	8.097Å
b'	$[010] = [\overline{2}02] = 22.58$	$b_0 =$	12.91
c'	[001] = [321] = 30.46	$c_0 =$	7.69
α′	$[010] \land [001] = [\overline{2}02] \land [321] =$	100°0	$6\frac{1}{2}'$
$\beta'$	$[001] \land [100] = [321] \land [\overline{2}0\overline{2}] =$	123 5	$4\frac{1}{2}$
$\gamma'$	$[100] \land [010] = [\overline{2}0\overline{2}] \land [\overline{2}02] =$	89 4	2

From the volumetric formula the volume of the Spencer cell is 12,297.45 cu. Å. The volume of the new unit cell is 765; therefore the volume of Spencer's cell is 16.06 cu. Å (ca. 16.00) times that of the unit cell, which is also a reflection of the accuracy of the preceding calculations.

## CONTENTS OF THE UNIT CELL

The chemical analysis of tarbuttite by Spencer gives the formula  $Zn_2PO_4(OH)$ . The determined elements of the structural lattice give the volume of the unit cell,  $V_0 = 764.9$ , which, with the given density 4.15, makes the cell molecular weight,  $M_0 = 1924$ . The analysis then gives the number of molecules in the unit cell as shown in table 7.

## TABLE 7. TARBUTTITE: MOLECULAR CONTENT OF THE UNIT CELL

	1	2	3	4
ZnO	66.6	0.822	15.81	16
$P_2O_5$	29.2	0.205	3.94	4
$H_{2}O$	3.8	0.212	4.08	4

1. Tarbuttite, Broken Hill mines, N.W. Rhodesia; Spencer, analyst.

2. Molecular proportions from analysis reduced to 100%.

3. Number of molecules in the unit cell.

4. Number of molecules in the unit cell reduced to the nearest whole number.

The molecular content of the unit cell is, therefore, 16ZnO,  $4P_2O_5$ ,  $4H_2O$ , giving the cell formula  $8[Zn_2PO_4(OH)]$ .

## Acknowledgments

This work was undertaken during the investigation of minerals of the chemical type  $R_2XO_4(Z)$  under the direction of Professor Charles Palache, whose critical observations have aided materially in its preparation. I also wish to thank Drs. M. A. Peacock and Harry Berman for many helpful suggestions.

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