

## The Crystal Structure of Omphacite

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### Abstract

The crystal structure of  $P2/n$  omphacite has been determined by the least squares method using the intensity data collected by a counter method. This  $P2/n$  clinopyroxene has a different space group, but is very similar in structure to the  $P2$  omphacite described earlier (Clark and Papike, 1968; Clark, Appleman, and Papike, 1969). The true space group of the Californian omphacite studied by Clark and Papike (1968) and Clark *et al* (1969) has been found to have  $P2/n$ , not  $P2$ , space group symmetry. In the structure of  $P2/n$  omphacite, only one kind of  $\text{SiO}_3$  chain exists in which two crystallographically different Si atoms alternate. This chain is, therefore, different from the chain of  $C2$  spodumene,  $P2_1/c$  enstatite, and  $C2/c$  diopside. Mg and Al atoms are ordered in the  $M1$  and  $M1(2)$  sites, respectively. Na and Ca atoms are partially ordered in the  $M2$  and  $M2(1)$  sites.

### Introduction

Since the first determination of the diopside structure (Warren and Bragg, 1928), five space groups have been reported for the clinopyroxenes. They are  $C2/c$ ,  $P2_1/c$ ,  $P2_1/n$ ,  $C2$ , and  $P2$ . Clark and Papike (1966, 1968) and Clark *et al* (1969) have published detailed data on  $C2/c$  and  $P2$  omphacites. It seemed to us unusual that the rare space group  $P2$  should appear in the fairly common mineral omphacite. This idea led to the finding of a new type of omphacite with the space group  $P2/n$  (Matsumoto and Banno, 1970a, b).

In this study, the structure of this new  $P2/n$  omphacite has been precisely determined and is compared with that of omphacites with different space groups. Omphacite from California determined to be of space group  $P2$  by Clark and Papike (1968) has been reexamined and found to possess  $P2/n$  space group symmetry.

### Experimental

The structure determination was made on omphacite from a hornblende-bearing eclogite of the Iratsu mass, Bessi area, Japan. The Iratsu mass belongs to the epidote amphibolite facies of the Sam-

bagawa metamorphic terrain. The atomic ratios of the pyroxenes were calculated from the results of the wet chemical analysis by Ōki (Matsumoto and Banno, 1970b; Table 1). For comparison, the atomic ratios of omphacite from other localities are also given in Table 1. The similarity in chemical composition between the omphacite from Bessi and from California is remarkable. It is important, however, to record that the omphacite crystals from Bessi possess small differences in chemical composition when examined by the EPMA ( $\pm 1$  wt percent CaO). Omphacite from California was also studied by X-ray diffraction to compare with the Bessi specimens.

The cell dimensions of the Bessi omphacite were determined by a four-circle single crystal diffractometer (Table 1). They are in good agreement with those obtained by Clark and Papike (1966, 1968) and Clark *et al* (1969) for the California omphacite (Table 1).

In order to confirm the space group symmetry of the Bessi material, especially the existence of glide planes,  $h0l$  Weissenberg photographs were taken with an exposure of more than 200 hours. The  $h0l$  reflections are absent when  $h+l$  is odd. Therefore, this omphacite has  $n$ -glide planes perpendicular to  $[010]$ , and the diffraction symbol is  $2/m P/n$ . The possible

TABLE 1. Crystallographic and Chemical Data for Omphacite

Locality of Minerals	Bessi, Japan	California	Norway
References	This Study	Clark and Papike (1968) Clark <i>et al.</i> (1969)	Warner (1964), Clark <i>et al.</i> (1969)
$\underline{a}$ (Å)	9.585 (3)	9.596 (5)	9.646 (6)
$\underline{b}$ (Å)	8.776 (3)	8.771 (4)	8.824 (5)
$\underline{c}$ (Å)	5.260 (3)	5.265 (6)	5.270 (6)
$\beta$ (°)	106.85 (3)	106.93 (8)	106.59 (8)
Cell volume (Å <sup>3</sup> )	423.5 (3)	423.9 (4)	429.9 (5)
Space group	$P2/n$	$P2/n$ <sup>a)</sup>	$C2/c$
Cations per 6 oxygen atoms			
Tetrahedral Si	1.918	1.96	1.995
Al	0.082	0.04	0.005
$\Sigma$	2.000	2.00	2.000
<u>M</u> cations			
Ca	0.516	0.51	0.583
Na	0.484	0.48	0.325
Mg	0.392	0.44	0.582
Fe <sup>2+</sup>	0.077	0.10	0.116
Fe <sup>3+</sup>	0.137	0.10	0.123
Al	0.398	0.39	0.233
Ti	0.005	0.01	0.002
$\Sigma$	2.011	2.03	1.964
Z	4	4	4
Cal. density, g·cm <sup>-3</sup>	3.39	3.37	3.36
Reference for chemical analysis	Matsumoto and Banno (1970, <i>analyst.</i> Ōki)	Coleman <i>et al.</i> (1965)	Schmitt (1963) (from Clark <i>et al.</i> 1969)

a) Space group determination by present authors; other data from Clark and Papike (1968, 1968). The standard deviations are in parentheses.

space group symmetry is thus  $P2/n$  or  $Pn$ . Existence of the glide plane was further confirmed by careful examination of the  $h0l$  reflections using the four-circle diffractometer.

The three-dimensional intensity data were collected with the four-circle automatic diffractometer from a fragment with the dimensions of 0.10×0.16×0.20 mm. The diffractometer was operated by the  $\omega/2\theta$  scan technique with the filtered  $MoK\alpha$  radiation ( $\lambda=0.7101$  Å). The calculated  $\mu r$  of the specimen is 0.21 for the  $MoK\alpha$  radiation.

All 1090 non-equivalent reflections with  $\sin\theta < 0.65$  were measured, and the number of non-zero reflections is 955. These intensity data were converted into observed structure factors by applying the Lorentz and polarization factors. Absorption corrections

were made assuming the crystal to be spherical in shape. The estimated standard deviation of each reflection was computed from counting statistics.

### Structure Refinement

The starting atomic parameters for the least squares refinements were the average values of the corresponding parameters reported for  $P2$  Californian omphacite by Clark and Papike (1968). In the earlier stage of the refinement, disordered arrangements of  $Al_{0.4}Mg_{0.4}Fe_{0.2}$  in the  $M1$  and  $M1(1)$  sites and  $Na_{0.5}Ca_{0.5}$  in the  $M2$  and  $M2(1)$  were assumed. The atomic coordinates and isotropic temperature factors were varied utilizing the ORFLS (Busing, Martin, and Levy, 1962) program modified by Iitaka.

At the later stage of the refinement, the site oc-

TABLE 2. Atomic Parameters, Isotropic Temperature Factors, and Site Occupancies of Atoms in P2/n Omphacite\*

ATOM	X	Y	Z	B	SITE OCCUPANCY
O1(1)	0.3634 (4)	0.3382 (5)	0.1232 (7)	0.73 (7)	1.0 for all O
O1(2)	0.3621 (4)	0.1767 (5)	0.6475 (8)	0.74 (6)	
O2(1)	0.6138 (4)	0.5090 (5)	0.3091 (8)	0.76 (7)	
O2(2)	0.6063 (4)	0.9974 (5)	0.8054 (8)	0.80 (7)	
O3(1)	0.6057 (4)	0.2663 (4)	0.0037 (8)	0.65 (6)	
O3(2)	0.5981 (4)	0.2398 (4)	0.4984 (8)	0.70 (7)	
Si 1	0.5393 (2)	0.3465 (2)	0.2273 (3)	0.37 (3)	1.0 for all Si
Si 2	0.5376 (2)	0.1621 (2)	0.7310 (3)	0.36 (3)	
M1(1)	0.2500	0.3480 (2)	0.7500	0.32 (5)	Al 0.868 (9), Fe 0.132
M1	0.2500	0.1580 (3)	0.2500	0.43 (5)	Mg 0.815 (9), Fe 0.185
M2	0.2500	0.5521 (3)	0.2500	0.86 (6)	Ca 0.314 (13), Na 0.686
M2(1)	0.2500	0.9502 (2)	0.7500	0.82 (5)	Ca 0.716, Na 0.284

\* If the origin of coordinate is displaced by (.75, .75, 0) and (.75, .75, .75), the values can be directly compared with the coordinate of the C2/c clinopyroxene by Burnahm's (1967) notation, and the P2 omphacite by Clark et al (1969), respectively. Standard deviations in parentheses.

TABLE 3. Observed and Calculated Structure Factors for Omphacite

h	k	l	F <sub>obs</sub>	F <sub>calc</sub>	h	k	l	F <sub>obs</sub>	F <sub>calc</sub>	h	k	l	F <sub>obs</sub>	F <sub>calc</sub>	h	k	l	F <sub>obs</sub>	F <sub>calc</sub>	h	k	l	F <sub>obs</sub>	F <sub>calc</sub>						
2	0	0	4.518	-1.702	3	6	2	26.874	24.424	3	2	10.119	-9.700	8	8	26.522	-27.059	-9	4	3.204	-3.304	10	1	2.980	-2.303	2	9	0.828	1.500	
4	0	0	8.096	13.114	4	6	2	5.233	2.595	4	2	27.441	-24.412	9	8	6.453 <sup>1</sup>	6.038	-10	4	26.620	27.063	11	1	29.621	-28.209	3	9	4.208	-4.608	
6	0	0	83.945	-83.975	5	6	2	12.898	22.357	5	2	6.455	6.615	0	9	9.977	-10.233	-11	4	2.910	-2.208	0	2	60.712	-57.579	4	9	8.911	7.911	
8	0	0	70.072	72.125	8	6	2	12.291	12.722	6	2	74.590	73.976	1	9	16.274	-14.807	-1	5	29.850	29.410	1	2	4.843	-4.399	6	9	1.040	0.143	
10	0	0	58.852	-56.949	7	6	2	7.709	7.830	7	2	4.363	4.151	2	9	5.111	-4.886	-2	5	9.745	9.492	2	2	34.164	32.632	5	9	9.156	-9.061	
12	0	0	11.917	-10.866	10	6	2	45.454	-43.258	8	2	47.897	-45.935	3	9	12.776	11.613	-3	5	13.021	13.432	3	2	4.461	4.724	0	0	48.669	48.119	
1	1	4	14.427	-11.751	10	6	2	2.260	1.120	10	2	7.735	-5.919	4	9	3.452	-1.799	-4	5	10.707	-11.370	4	2	53.937	53.501	1	10	10.351	-9.995	
2	1	4	3.795	-3.944	11	7	3	13.733	-12.769	11	2	2.521	-2.673	5	9	36.197	36.326	-5	5	15.787	16.089	5	2	0.578	-1.283	2	10	2.874	-2.850	
3	1	4	92.079	89.425	12	7	3	15.408	-14.913	12	2	46.099	-45.340	6	9	6.176	-6.770	-6	5	3.604	-3.417	6	2	39.579	38.501	3	10	6.643	6.607	
4	1	4	7.735	7.590	13	7	3	14.706	-14.674	13	2	8.602	-8.835	7	9	32.905	32.076	-7	5	1.945	-3.446	7	2	2.415	2.979	4	10	70.193	67.618	
5	1	4	62.438	59.358	14	7	3	2.812	-2.579	14	2	18.070	-13.264	8	10	23.558	-23.553	-9	5	5.361	5.439	8	2	1.582	-1.408	5	10	10.444	-11.145	
6	1	4	5.157	-5.305	15	7	3	47.613	47.651	15	2	0.578	-0.828	10	10	3.380	-1.441	-10	5	5.537	5.799	10	2	20.431	-19.757	1	11	14.892	-15.625	
7	1	4	48.661	45.922	16	7	3	38.940	38.645	16	2	39.149	-34.619	11	10	5.826	-5.171	-11	5	7.755	8.239	0	3	5.743	5.755	2	11	6.335	-4.938	
8	1	4	5.730	-5.533	17	7	3	15.660	15.806	17	2	139.223	145.736	12	10	1.868	-0.773	-2	6	14.058	-14.065	1	3	40.877	-40.336	3	11	24.022	23.722	
9	1	4	35.444	33.825	18	7	3	8.235	-2.702	18	2	6.460	-6.434	13	10	4.878	8.577	-3	6	1.298	1.485	7	3	6.561	6.168	4	10	100.209	103.639	
10	1	4	4.450	-5.903	19	7	3	10.547	10.859	19	2	17.699	18.569	14	10	21.019	-21.737	-5	6	24.879	-25.260	3	3	9.089	-9.000	-2	0	38.596	-33.818	
11	1	4	10.823	8.334	1	8	4	9.445	9.138	1	8	0.900	2.490	15	10	6.819	6.507	-8	6	6.922	7.819	4	3	5.552	-5.483	-4	0	103.021	-101.434	
0	2	4	42.575	-42.667	2	8	4	23.142	22.934	2	8	49.554	49.452	11	11	3.341	3.574	-6	6	19.358	20.068	5	3	22.745	-22.154	-8	0	29.665	-30.806	
0	2	4	4.590	4.484	3	8	4	1.534	2.009	3	8	7.835	7.579	11	11	20.756	-18.256	-7	6	5.677	4.201	6	3	18.119	17.458	-10	0	72.167	73.181	
0	2	4	54.027	-53.130	4	8	4	2.773	-3.529	4	8	8.615	-9.568	12	11	6.174	-6.111	-9	6	2.157	0.896	9	3	9.345	-8.783	-12	0	15.627	11.684	
0	2	4	2.748	-2.988	5	8	4	18.465	-17.158	5	8	87.229	-93.208	13	11	6.819	6.507	-10	6	11.891	13.305	10	3	1.293	-0.070	-1	1	3.181	4.824	
0	2	4	18.465	-16.451	6	8	4	8.160	-7.781	6	8	8.202	8.057	14	11	2.152	-0.620	-1	7	51.329	52.790	4	4	65.547	65.122	-2	1	6.143	6.214	
0	2	4	3.821	-3.537	7	8	4	5.551	-5.161	7	8	24.255	-22.294	15	11	6.169	-5.709	-10	6	11.891	13.305	10	3	1.293	-0.070	-1	1	3.181	4.824	
0	2	4	15.516	14.541	8	8	4	7.211	6.376	8	4	4.835	-4.756	12	12	6.311	-5.386	-2	7	15.464	15.785	1	4	9.092	-9.379	-2	1	6.143	6.214	
0	2	4	4.207	-3.397	9	8	4	11.958	-9.600	9	4	27.043	-25.399	-1	0	12.797	-12.675	-3	7	6.015	7.135	2	4	34.982	34.556	-3	1	6.928	-6.504	
0	2	4	8.204	7.655	10	8	4	1.370	1.713	10	4	10.635	-10.653	-3	0	7.552	7.705	-5	7	79.554	84.505	4	4	47.113	46.219	-6	1	1.370	-0.336	
0	2	4	1.762	-0.683	11	8	4	27.611	28.739	11	4	3.588	3.347	-9	0	7.441	-7.906	-6	7	6.411	6.118	5	4	4.767	2.564	-8	1	87.469	104.824	
0	2	4	15.537	15.560	12	8	4	6.298	-6.078	12	4	4.752	2.800	-11	0	6.582	7.364	-7	7	4.000	-4.303	6	4	7.957	-7.377	-9	1	1.980	2.193	
0	2	4	3.117	-3.203	13	8	4	8.535	-8.161	13	4	1.331	0.331	-1	1	17.023	15.079	-9	7	32.446	33.324	8	4	3.596	-3.645	-11	1	1.545	-1.742	
0	2	4	5.687	5.178	14	8	4	19.069	18.038	14	4	30.212	28.777	-2	1	1.734	2.369	-1	8	3.207	-3.055	10	4	15.642	-15.871	-1	2	4.915	-4.856	
0	2	4	1.950	-2.821	15	8	4	4.701	-4.712	15	4	1.589	2.129	-3	1	75.565	77.269	-2	8	85.862	91.415	10	4	15.642	-15.871	-1	2	4.915	-4.856	
0	2	4	1.011	-1.390	16	8	4	70.186	-72.372	16	0	5	1.589	2.129	-3	1	75.565	77.269	-2	8	85.862	91.415	10	4	15.642	-15.871	-1	2	4.915	-4.856
0	2	4	58.000	-55.805	17	8	4	3.994	4.312	17	2	2.454	-1.761	-5	10	30.557	27.111	-3	8	0.361	-0.007	0	5	17.237	-17.697	-2	2	2.820	-2.643	
0	2	4	1.842	-0.843	18	8	4	7.265	6.131	18	3	25.165	-24.432	-6	1	2.128	2.562	-4	8	17.530	-16.282	1	5	59.265	-58.799	-4	2	30.807	28.861	
0	2	4	31.749	31.214	19	8	4	8.666	-8.609	19	3	3.604	-3.471	-7	1	27.322	26.882	-6	8	24.796	24.962	4	5	5.046	-4.510	-5	2	5.052	5.045	
0	2	4	7.931	-7.962	20	8	4	53.367	-51.071	4	5	23.557	-22.873	-8	1	3.749	3.383	-7	8	12.567	-13.590	3	5	5.046	-4.510	-5	2	5.052	5.045	
0	2	4	17.157	15.473	5	10	6	4.665	-5.655	5	5	23.557	-22.873	-8	1	3.749	3.383	-7	8	12.567	-13.590	3	5	5.046	-4.510	-5	2	5.052	5.045	
0	2	4	1.840	0.007	6	10	6	26.164	25.657	6	5	7.461	7.496	-9	2	2.884	0.949	-8	8	41.246	-43.302	6	9	2.090	-0.950	-8	2			

TABLE 3, Continued

h	k	F <sub>obs</sub>	F <sub>calc</sub>	h	k	F <sub>obs</sub>	F <sub>calc</sub>	h	k	F <sub>obs</sub>	F <sub>calc</sub>	h	k	F <sub>obs</sub>	F <sub>calc</sub>	h	k	F <sub>obs</sub>	F <sub>calc</sub>	h	k	F <sub>obs</sub>	F <sub>calc</sub>	h	k	F <sub>obs</sub>	F <sub>calc</sub>	h	k	F <sub>obs</sub>	F <sub>calc</sub>					
0	3	2.812	3.659	-4	1	3.393	3.140	-8	7	2.877	2.596	1	7	5.359	-6.407	-8	5	3.524	-3.536	3	6	7.250	-6.845	-5	7	61.342	66.155	0	0	0	0					
1	3	18.493	-17.098	-5	1	32.309	-31.216	-9	7	37.492	-38.154	2	7	2.049	-2.896	-9	5	3.558	-6.312	4	6	12.588	-11.988	-6	7	5.411	-2.257	0	0	0	0					
3	3	3.568	3.066	-6	1	2.345	-3.804	-4	8	10.547	-11.577	4	7	2.012	0.611	-10	5	4.557	-5.792	0	7	1.579	-1.515	0	0	0	0	0	0	0	0	0	0			
3	3	4.909	6.913	-7	1	28.367	-29.240	-2	8	53.279	-55.606	7	7	13.176	-12.747	-1	6	6.950	-7.328	0	7	1.579	-1.515	0	0	0	0	0	0	0	0	0	0	0		
4	3	4.577	4.111	-8	1	5.191	-4.559	-9	8	21.917	23.238	0	7	13.310	11.811	-2	6	23.955	25.209	1	7	5.165	-4.874	0	0	40.949	-39.115	0	0	0	0	0	0	0	0	
4	3	80.477	-78.801	-10	1	3.132	2.061	-4	8	21.917	23.238	0	7	2.407	2.363	-3	6	6.053	-7.061	3	7	31.086	28.821	2	0	3.447	1.973	0	0	0	0	0	0	0	0	0
6	3	2.915	-0.332	-11	1	1.042	-4.188	-4	8	6.081	5.756	1	8	4.275	3.569	-4	6	4.427	-4.498	1	7	27.996	-27.445	0	0	40.949	-39.115	0	0	0	0	0	0	0	0	
6	3	2.229	-0.278	-12	1	4.381	4.299	-5	8	17.727	-18.057	2	8	5.519	2.879	-5	6	37.319	-38.387	0	8	5.596	-3.922	4	0	76.011	-71.001	0	0	0	0	0	0	0	0	
7	3	57.268	-54.694	-1	2	6.569	6.876	-7	8	6.218	6.992	8	8	3.016	-1.799	-6	6	3.529	-3.529	-1	0	0	0	0	0	2.012	-0.736	0	0	0	0	0	0	0	0	
0	4	37.020	35.531	-2	2	97.657	-116.371	-8	8	40.609	42.156	4	8	31.633	-29.342	-7	6	5.359	-5.243	-3	0	0	0	0	0	2.012	-0.736	0	0	0	0	0	0	0	0	
1	4	1.623	1.988	-3	2	5.377	-6.527	-1	9	36.716	40.765	0	9	9.154	-9.604	-8	6	32.745	-33.671	-5	0	0	0	0	0	1.910	6.992	0	0	0	0	0	0	0	0	
2	4	10.599	10.233	-4	2	29.071	29.206	-2	9	5.789	7.323	1	9	8.181	-8.558	-9	6	2.190	-3.177	-7	0	0	0	0	0	1.910	6.992	0	0	0	0	0	0	0	0	
3	4	7.281	7.491	-5	2	5.119	5.697	-2	9	12.799	13.818	2	9	2.405	2.046	-1	7	27.314	-27.313	-9	0	0	0	0	0	1.865	-0.850	0	0	0	0	0	0	0	0	
4	4	42.589	41.043	-6	2	10.777	-11.252	-3	9	5.353	5.702	3	9	13.981	14.845	-2	7	2.988	-2.866	-1	1	2.343	2.263	0	2	5.284	-3.698	0	0	0	0	0	0	0	0	
5	4	1.692	0.742	-7	2	2.668	2.931	-5	9	5.353	5.702	3	9	13.981	14.845	-2	7	2.988	-2.866	-1	1	2.343	2.263	0	2	5.284	-3.698	0	0	0	0	0	0	0	0	
6	4	21.342	22.276	-8	2	69.930	70.781	-9	9	2.371	+4.131	0	10	35.031	-52.642	-3	7	8.674	-9.203	-2	1	8.867	8.770	1	2	6.502	-6.493	0	0	0	0	0	0	0	0	
7	4	3.811	-5.923	-10	2	5.764	6.855	-2	10	12.603	-13.437	-2	0	10.635	11.410	-4	7	5.397	-6.024	-3	1	43.976	43.942	2	2	33.532	31.036	0	0	0	0	0	0	0	0	0
0	5	5.624	5.837	-11	2	1.870	-1.727	-2	10	19.894	20.604	-6	0	107.562	-118.652	-5	7	6.148	7.246	-5	1	28.612	27.808	0	3	5.893	-4.822	0	0	0	0	0	0	0	0	
1	5	26.277	27.060	-12	2	4.391	-5.177	-2	10	19.894	20.604	-6	0	107.562	-118.652	-5	7	6.148	7.246	-5	1	28.612	27.808	0	3	5.893	-4.822	0	0	0	0	0	0	0	0	
2	5	4.632	-4.137	-12	2	57.766	57.312	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0			
3	5	6.494	6.046	-1	3	106.548	117.892	0	0	110.949	109.810	-10	0	41.367	-44.066	-8	7	4.812	4.850	-7	1	17.642	19.570	2	3	1.651	2.253	0	0	0	0	0	0	0	0	
4	5	1.981	1.881	-2	3	4.149	4.568	2	0	17.121	-15.396	-1	1	47.291	-47.918	-3	8	4.889	4.883	-9	1	1.078	1.935	0	4	41.656	40.901	0	0	0	0	0	0	0	0	
5	5	9.899	-9.050	-3	3	27.301	-28.673	4	0	82.500	79.794	-2	1	1.370	1.035	-4	8	23.581	-23.334	-10	1	5.101	5.994	1	4	2.154	0.972	0	0	0	0	0	0	0	0	
6	5	2.229	-2.794	-4	3	2.868	3.131	6	0	88.736	-15.653	-3	1	88.313	-87.787	-4	8	4.814	-5.767	-1	2	6.919	-6.623	2	4	30.023	29.017	0	0	0	0	0	0	0	0	
7	5	5.557	-5.638	-5	3	78.653	72.394	8	0	40.397	38.151	-4	1	1.551	3.023	-5	8	0.753	5.0149	-3	2	2.018	1.622	0	5	3.480	-3.744	0	0	0	0	0	0	0	0	
8	5	3.853	3.320	-6	3	1.514	-2.417	0	1	4.110	4.156	-5	1	11.952	-10.028	-6	8	0.753	5.0149	-3	2	2.018	1.622	0	5	3.480	-3.744	0	0	0	0	0	0	0	0	
0	6	28.044	28.252	-7	3	27.503	27.997	1	1	6.236	-5.380	-6	1	1.117	-0.347	-1	9	9.515	-10.424	-2	2	25.441	-26.863	1	5	34.471	-32.799	0	0	0	0	0	0	0	0	
1	6	3.029	-5.017	-9	3	74.760	76.304	2	1	5.119	-5.071	-8	1	3.963	4.544	-3	9	29.445	-28.881	-5	2	1.729	-2.152	0	6	29.476	30.860	0	0	0	0	0	0	0	0	
2	6	11.785	12.028	-10	3	5.000	-5.354	3	1	49.492	49.197	-9	1	8.173	-8.215	-4	9	1.615	-1.242	-6	2	14.930	-14.930	0	6	32.482	30.965	0	0	0	0	0	0	0	0	
3	6	23.184	21.326	-11	3	1.509	-1.509	-7	1	20.725	21.455	-11	1	14.515	-13.656	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0		
4	6	5.828	5.771	-11	3	37.374	-38.597	7	1	20.725	21.455	-11	1	14.515	-13.656	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0		
5	6	6.254	-4.995	-1	4	8.184	-8.699	8	1	3.947	2.351	-2	2	13.194	-12.889	1	0	2.701	2.651	-10	2	6.502	-5.050	-6	0	46.925	47.527	0	0	0	0	0	0	0	0	
6	6	5.057	4.625	-2	4	48.697	51.292	-2	2	15.787	-16.259	-3	2	9.479	10.556	1	0	9.355	-9.189	-3	3	89.474	-91.476	-8	0	26.042	23.251	0	0	0	0	0	0	0	0	
7	6	3.135	-5.500	-4	4	22.276	24.146	2	2	50.898	-50.222	-5	2	6.232	-2.800	5	0	3.341	3.246	-2	3	2.665	0.937	-1	1	7.371	7.306	0	0	0	0	0	0	0	0	
8	6	36.527	35.204	-5	4	2.812	-2.082	3	2	2.018	0.217	-6	2	3.532	2.638	0	1	2.918	-2.597	-2	3	15.384	-16.260	-2	1	1.690	-1.933	0	0	0	0	0	0	0	0	
9	6	7.201	-6.849	-5	4	2.812	-2.082	4	2	9.185	-10.470	-7	2	10.193	11.704	-2	1	2.918	-2.597	-3	3	47.933	-47.550	-3	1	38.669	42.039	0	0	0	0	0	0	0	0	
0	7	12.776	-10.966	-6	4	36.767	-38.905	5	2	4.174	4.878	-7	2	3.965	-4.282	1	1	3.313	1.182	-6	3	2.485	2.977	-4	1	6.233	-5.575	0	0	0	0	0	0	0	0	
1	7	42.554	41.066	-8	4	24.533	-23.233	6	2	3.021	3.899	-9	2	2.988	5.283	2	1	2.771	-3.222	-7	3	10.436	12.997	-5	1	18.630	18.950	0	0</							

TABLE 4. Bond Distances and Bond Angles of the Tetrahedra in  $P2/n$  Omphacite\*

About Si 1		About Si 2	
Si 1 - O1 (1)	1.616 (4) Å	Si 2 - O1 (2)	1.616 (4) Å
- O2 (1)	1.597 (5)	- O2 (2)	1.590 (5)
- O3 (1)	1.649 (4)	- O3 (1)	1.666 (5)
- O3 (2)	1.662 (4)	O3 (2)	1.646 (4)
Mean	1.631	Mean	1.630
O1 (1) - O2 (1)	2.757 (5) Å	O1 (2) - O2 (2)	2.742 (6) Å
- O3 (1)	2.652 (6)	- O3 (1)	2.654 (6)
- O3 (2)	2.670 (5)	- O3 (2)	2.658 (5)
O2 (1) - O3 (1)	2.655 (6)	O2 (2) - O3 (1)	2.581 (6)
- O3 (2)	2.585 (6)	- O3 (2)	2.658 (6)
O3 (1) - O3 (2)	2.634 (6)	O3 (1) - O3 (2)	2.648 (6)
Mean	2.659	Mean	2.657
O1 (1) - Si1 - O2 (1)	118.2 (2)*	O1 (2) - Si2 - O2 (2)	117.6 (2)*
O1 (1) - Si1 - O3 (1)	108.6 (2)	O1 (2) - Si2 - O3 (2)	109.2 (2)
O1 (1) - Si1 - O3 (2)	109.0 (2)	O1 (2) - Si2 - O3 (1)	107.9 (2)
O2 (1) - Si1 - O3 (1)	109.8 (2)	O2 (2) - Si2 - O3 (2)	110.5 (2)
O2 (1) - Si1 - O3 (2)	105.0 (2)	O2 (2) - Si2 - O3 (1)	104.8 (2)
O3 (1) - Si1 - O3 (2)	105.5 (2)	O3 (2) - Si2 - O3 (1)	106.1 (2)

\* The standard deviations in parentheses are expressed in the unit of the last digit stated.

for Si1 and Si2 tetrahedra are shown in Table 4 and in Figure 1. The difference between the two tetrahedra is slight. The Si-O bonds of the bridging oxygens (O3(1) and O3(2)) are significantly longer than those to other nonbridging oxygens, as in other clinopyroxenes. The angle O1-Si-O2 is  $118^\circ$  for each tetrahedron, compared with  $105^\circ$  for O2-Si-O3, reflecting the long O1(1)-O2(1) and O1(2)-O2(2) distances of 2.757 and 2.742 Å, respectively.

The metal-oxygen bond distances for the four octahedral and eight-fold cation sites are summarized in Table 5.

The Mg and Al atoms are ordered in the M1 and M1(1) sites, respectively. The Fe atoms are distributed to fill each of these two sites as a minor component. The Na and Ca atoms are partially ordered in the M2 and M2(1) sites with an isotropic temperature factor of about  $0.8 \text{ \AA}^2$ , and with the ratio of Na/Ca=2/1 and Na/Ca=1/2, respectively. These results are very similar to those found by Clark and Papike (1968) for the  $P2$ -omphacite.

### Discussion

Among the 16 different symmetry types proposed for clinopyroxenes (Matsumoto and Banno, 1970b; Matsumoto, Tokonami, and Morimoto, 1972; Brown, 1972), only five have been reported to exist. They are  $C2/c$ ,  $P2/n$ ,  $C2$ ,  $P2_1/c$ , and  $P2$ . Although  $P2_1/n$  was reported for clinoenstatite (Lindeman, 1961), it is considered by Smith (1969) to be erroneously assigned. Furthermore, recent study by Graham on spodumene (1974) has raised a serious doubt of the possibility of  $C2$  symmetry for clinopyroxenes. The first three structure types ( $C2/c$ ,

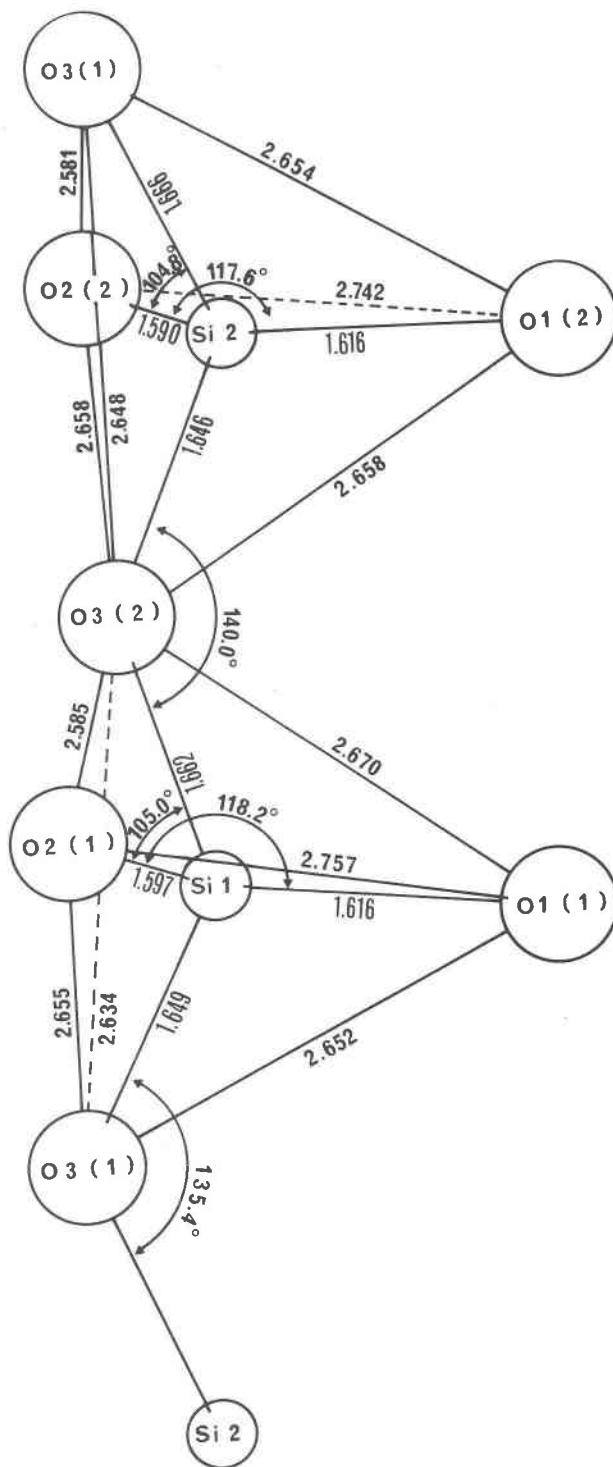


FIG. 1. Silicate chain in  $P2/n$  omphacite. Bond distances and angles are given.

$P_2/n$ ,  $C2$ ) have only one kind of  $\text{SiO}_3$  chain, and the other two types have two kinds of chains in the cell. In the structure of the  $P_2/n$  omphacite, crystallographically different tetrahedra alternate along the  $c$  axis and form only one kind of chain in the structure.

According to the present and previous studies, three different space groups for omphacite mineral— $C2/c$ ,  $P_2/n$ , and  $P2$ —have been reported. The crystallographic and chemical data for these omphacites are compared in Table 1. The chemical compositions of these three specimens are similar. The Norwegian omphacite, which has the largest cell volume and possesses the higher  $C2/c$  space group symmetry, is considered to belong to a high temperature facies (Banno, 1970). The  $P_2/n$  omphacite is considered to transform to the  $C2/c$  omphacite by an order-disorder transition. An antiphase domain structure which has been attributed to this order-disorder transition has been observed for the  $P_2/n$  omphacite (Champness, 1973; Phakey and Ghose, 1973) as for the  $P2_1/c$  pigeonite (Morimoto and Tokonami, 1969).

Because the difference in temperature of omphacite crystallization between the Sambagawa and the Californian occurrences is not large, it seemed necessary to examine the apparent discrepancy in symmetry

TABLE 5. Metal-Oxygen Bond Distances for the Four  $M$  Cation Sites

	$M_1$	$M_1(1)$	$M_2$	$M_2(1)$
O1(1)	2.132(5) Å	1.951(4) Å	2.360(5) Å	2.394(5) Å
O1(2)	2.062(4)	2.010(5)		2.394(5)
O2(1)		1.900(5)	2.370(4)	
O2(2)	2.019(5)			2.390(4)
O3(1)			2.703(5)	2.482(4)
O3(2)			2.468(4)	2.777(4)
Mean of 6	2.071	1.954	2.399	2.422
Mean of 8			2.475	2.511

\* The standard deviations in parentheses are expressed in the unit of the last digit stated.

between the present specimen and the Californian omphacite. Dr. Clark kindly sent us the Californian omphacite which she had studied. We examined the specimen by the precession method at the precession angle of  $\bar{\mu}=30^\circ$  with an exposure of 100 hours for  $\text{CuK}\alpha$  X-rays at 100 mA. Only four weak reflections ( $40l$  and its equivalent reflections) violating the systematic absences for the  $n$ -glide planes appeared in the  $h0l$  net. However, these reflections were caused to disappear by changing the precession angle to  $\bar{\mu}=25^\circ$  (Fig. 2). The disappearance of  $40l$  and its equivalent reflections by the change of the diffraction geometry indicates that the reflections violating  $h+l=\text{even}$  in

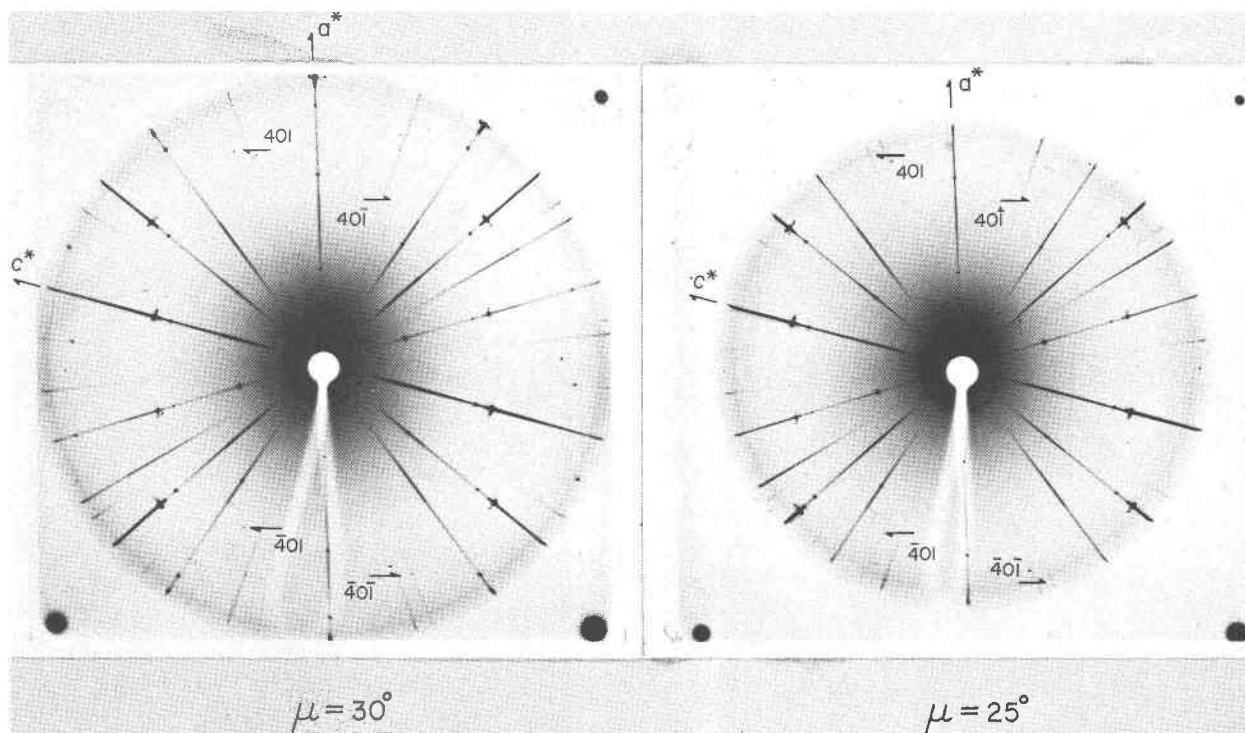


FIG. 2. Precession photographs of  $h0l$  for  $P_2/n$  omphacite from California.  $\{402\}$  reflections violating  $h+k/\text{even}$  in  $h0l$  are shown by arrows in the photograph taken with  $\bar{\mu}=30^\circ$  (left). All  $\{40l\}$  reflections are not observed in the photograph taken with  $\bar{\mu}=25^\circ$  (right). Both photographs were exposed more than 100 hours with  $\text{CuK}\alpha$  radiation of 100 mA.

the  $h0l$  net observed in the earlier experiment are multiple reflections (Azároff, 1968) and the true space group of the Californian omphacite is not  $P2$  but  $P2/n$ . The  $h0l$  electron diffraction pattern of the Californian omphacite presented by Phakey and Ghose (1973, Fig. 1c) also gives evidence for the presence of an  $n$ -glide, indicating that the true space group is  $P2/n$ .

The Mössbauer spectrum of the  $P2/n$  omphacites described in the present paper has been reported by Matsui, Syono, and Maeda (1972). The spectrum was similar to those of the  $P2$  omphacites reported by Bancroft, Williams, and Essene (1969) with broad absorption bands due to  $Fe^{2+}$ . In the calcium-rich pyroxenes, the broad peaks due to  $Fe^{2+}$  are better interpreted as due to the variety of local configurations around  $Fe^{2+}$  rather than in terms of superposed peaks of  $Fe^{2+}$  in nonequivalent positions (Williams *et al.*, 1971; Matsui *et al.*, 1972; Dowty and Lindsley, 1973). Thus, although it is not possible to decide uniquely the space group of the Ca-rich pyroxenes by the Mössbauer spectrum alone, it is highly probable that the omphacites reported by Bancroft *et al.* (1969) actually have the space group  $P2/n$ .

A statistical study of the distribution of crystalline substances with known space groups has shown that only two out of 5572 inorganic crystals are reported to have the  $P2$  symmetry (Nowacki, Matsumoto, and Edenharter, 1967a,b). Moreover, the two  $P2$  substances, metaheulandite and quenselite, have since been found to possess the space groups  $P2_1/m$  (Donnay and Ondik, 1973) and  $P2_1/c$  (Povarennykh, 1972), respectively. In this statistical distribution, most groups with polar axes ( $C_{2v}^x$ ,  $C_{4v}^x$  and  $C_{6v}^x$ ) do not appear, and the crystals with only a pure rotation axis ( $P2$ ,  $P3$ ,  $P4$ , and  $P6$ ), not with a screw axis, are very rare. It therefore seems very unlikely that omphacite would have a rare space group such as  $P2$ .

In fact, the Bessi omphacite in this study and the Fergusson omphacite (Kanazawa and Matsumoto, 1971) show  $P2/n$  symmetry, and the reexamination of the Californian omphacite reveals that this also has  $P2/n$  symmetry. Although the New Caledonian omphacite with the composition between jadeite and hedenbergite (Black, 1972) and the Venezuela omphacite (Fe-free) were reported to be  $P2$ , probably all reported  $P2$  omphacites actually possess  $P2/n$  symmetry.

#### Acknowledgments

We thank Professor Y. Iitaka of Tokyo University for his kind assistance with the computation problems; Dr. S. Banno of

Kanazawa University and Dr. J. R. Clark of the U.S. Geological Survey for providing with omphacite specimens and the geological information on the specimens; Dr. Y. Matsui of Okayama University for discussions on the Mössbauer spectrum on omphacite; and Mr. M. Kitamura of Tohoku University for his help in computation. We express our thanks to Dr. Malcolm Ross of the U.S. Geological Survey for reviewing the manuscript and providing numerous suggestions for its improvement. Thanks are also due to Mr. Nakamura, Miss Kino, and Miss Hirano for preparing figures and tables and for typing the manuscript. Part of the expenses of this work were defrayed by a research grant from the Ministry of Education of the Japanese Government.

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*Manuscript received, July 29, 1974; accepted for publication, February 13, 1975.*