# Crystal structure of ilmenite $\left(\mathrm{FeTiO}_{3}\right)$ at high temperature and at high pressure 

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#### Abstract

The structures of two single crystals of synthetic ilmenite were refined using X-ray intensity data collected at $24,400,600,800$, and $1050^{\circ} \mathrm{C}(1 \mathrm{~atm})$ and $0.001,25.4,34.6$, and 46.1 kbar (room temperature). Thermal expansion of the unit cell was nearly isotropic, whereas compression was relatively anisotropic, with c/a decreasing linearly with increasing pressure. The isothermal bulk modulus and its pressure derivative determined from cell volume data are $K_{\mathrm{o}}=1.70(7) \mathrm{Mbar}, K_{\mathrm{o}}^{\prime}=8(4)$, or $K_{\mathrm{o}}=1.77(3)$ if $K_{\mathrm{o}}{ }^{\prime}$ is assumed to be 4(1). Mean $\mathrm{Fe}-\mathrm{O}$ and Ti-O distances increased linearly with temperature and decreased linearly with pressure, $\langle\mathrm{Fe}-\mathrm{O}\rangle$ being about twice as expandable and compressible as $\langle\mathrm{Ti}-\mathrm{O}\rangle$. The responses of the two octahedral sites to temperature and pressure were quite different from one another, however. The longer of the two independent $\mathrm{Fe}-\mathrm{O}$ bonds was more expandable and less compressible than the shorter one, whereas the opposite was true for the Ti site. The Ti atom was displaced toward the centroid of its coordination polyhedron at high temperature, but the Fe atom moved further away from its centroid position. Cation shifts were much smaller with pressure than with temperature. These results indicate that the reponses of the ilmenite structure to temperature and pressure are not inverse in character. The cation sites remained fully ordered at all temperatures and pressures studied.


## Introduction

Ilmenite $\left(\mathrm{FeTiO}_{3}\right)$ occurs as an accessory mineral in a wide variety of igneous and metamorphic rocks (Haggerty, 1976; El Goresy, 1976a,b; Rumble, 1976). One of its most valuable characteristics for petrogenetic studies has been the use of compositions of coexisting hematiteilmenite and magnetite-ulvöspinel solid solutions as an indicator of temperature and oxygen fugacity at the time of last equilibration (Lindsley, 1963; Buddington and Lindsley, 1964). More recently, other geothermometers have been based upon coexisting ilmenite and olivine or pyroxene (Andersen and Lindsley, 1979; Bishop, 1980) and have utilized solution models to extend the experimental calibrations. The ilmenite structure may also be an important one for metasilicates undergoing high-pressure transformations in the Earth's mantle (e.g., Ringwood, 1969; Liu, 1977a). In order to improve thermochemical models, understand crystal-chemical partitioning behavior, and characterize the pressure-temperature systematics of compounds with the ilmenite structure, it would be

[^0]useful to determine the effects of elevated temperature and pressure upon the crystal structure of ilmenite.
The ilmenite structure was determined by Barth and Posnjak (1934). Shirane et al. (1959) determined the magnetic structure at low temperature using neutron diffraction, and the structure of lunar ilmenite was studied by Raymond and Wenk (1971). Numerous other investigations have elucidated the magnetic properties of ilmenites and hematite-ilmenite solutions (e.g., Ishikawa, 1958, 1962; Shirane and Ruby, 1962; Shirane et al., 1962; Thorpe et al., 1977) and have suggested the possibility of an order-disorder transformation at high temperatures as is observed for intermediate compositions. Burton (1980) studied such a transformation in an intermediate hema-tite-ilmenite by single-crystal X-ray diffraction.
Recently, high-pressure structure refinements have been reported for several materials with the closely related corundum structure (Finger and Hazen, 1980). Compression of ilmenite has also previously been studied by X-ray diffraction (Liu et al., 1974) and Mössbauer spectroscopy (Vaughan and Drickamer, 1967) on polycrystalline specimens. A number of other studies have considered the elasticity, crystal-chemical systematics, and high-pressure phase transformations in other compounds possessing the ilmenite structure (Liebermann,

1976; Liu, 1977b; Kirfel et al., 1978; Ito and Matsui, 1979).

The present study was undertaken to characterize changes in the crystal structure of ilmenite with temperature and under isothermal, hydrostatic compression and to compare this behavior with that found for similar materials.

## Experimental procedures

## Synthesis of samples

The ilmenite used in this study was synthesized by D. H. Lindsley (run no. L679). The starting material was a stoichiometric mix of $\mathrm{Fe}+\mathrm{Fe}_{2} \mathrm{O}_{3}+\mathrm{TiO}_{2}$. It was loaded dry into a Ag capsule and reacted in a piston-cylinder apparatus at $20 \mathrm{kbar}, 1000^{\circ} \mathrm{C}$ for 1 day, 22 hours. The run products consisted of single crystals of ilmenite, generally equant and subhedral, $\sim 50-150 \mu \mathrm{~m}$ in diameter.

## Precession camera studies

A single crystal cemented to a quartz glass fiber and sealed in an evacuated silica capillary was studied at high temperature on a precession camera. Precession photos of the $h 0 l$ orientation were exposed for $\sim 24$ hours each at $500,700,900,1000$, and $1150^{\circ} \mathrm{C}$. Three relatively weak but observable reflections which are allowed in space group $R \overline{3}$ but forbidden in $R \overline{3} c$ were found to be present at all temperatures. The reflections monitored were $\overline{2} 01$, 107 , and 205 , which are excluded by the condition $l=2 n$ in $R \overline{3} c$. This evidence precludes the possibility of a space group transformation from $R \overline{3}$ to $R \overline{3} c$, which would be indicative of complete cation disorder, to $1150 \pm 20^{\circ} \mathrm{C}$. No decomposition or loss of resolution in diffraction spots was observed throughout the heating experiment.

## High temperature data collection

Another ilmenite crystal from the same synthesis run was studied at high temperature on an automated fourcircle diffractometer. Three-dimensional X-ray intensity data were collected at $24,400,600,800$, and $1050^{\circ} \mathrm{C}$, and again at room temperature after heating (rtah). The crystal was held at temperature for 3 to 4 hours before data collection was begun. All reflections with two theta

Table 1. Unit-cell parameters of ilmenite at high temperature

| $T\left({ }^{\circ} \mathrm{C}\right)$ | $a(\AA)$ | $c(\AA)$ | $V\left(\AA^{3}\right)$ | $c / a$ |
| :---: | :---: | :---: | :---: | :---: |
| 24 | $5.0884(1) *$ | $14.0855(4)$ | $315.84(1)$ | 2.7682 |
| 400 | $5.1080(1)$ | $14.1287(6)$ | $319.25(1)$ | 2.7660 |
| 600 | $5.1182(1)$ | $14.1566(6)$ | $321.16(1)$ | 2.7659 |
| 800 | $5.1280(1)$ | $14.187(1)$ | $323.08(3)$ | 2.7666 |
| 1050 | $5.1412(1)$ | $14.2250(6)$ | $325.62(1)$ | 2.7669 |
| RTAH** | $5.0889(1)$ | $14.0933(5)$ | $316.08(1)$ | 2.7594 |

[^1]less than $70^{\circ}$ for graphite-monochromated MoK $\alpha$ radiation were measured. At room temperature, data were collected in a hemisphere of reciprocal space, while at high temperatures, only one quadrant of reciprocal space was studied in order to minimize the total exposure at high temperature. Intensity data were converted to structure factors by correcting for background and Lorentzpolarization factors. Following the collection of intensity data at each temperature, $2 \theta$ values of from 12 to 15 reflections were measured, and the average of the positive and negative $2 \theta$ values was used in a least-squares refinement of the unit-cell parameters (Table 1).

## High pressure data collection

A third crystal from the same synthesis run was selected for high pressure study. Precession and Weissenberg photos showed the sample to be a single crystal with sharp diffraction spots.

Three-dimensional X-ray intensity data were collected at room temperature and pressure. All reflections with $2 \theta$ less than $70^{\circ}$ were measured in one hemisphere of reciprocal space. Structure refinement based on these data (see below) yielded essentially identical parameters to those obtained from the crystal used for high-temperature study. The crystal was then placed in a Merrill and Bassett-type miniature opposed anvil diamond cell (Merrill and Bassett, 1974) for high pressure diffraction measurements. An Inconel X-750 gasket was used ( 0.25 mm thickness) with a 0.35 mm hole for the sample chamber. The crystal was attached to one diamond face with a small amount of the alcohol-insoluble fraction of petroleum jelly, which partially covered a portion of the crystal. The pressure-transmitting medium was a $4: 1$ mixture of methanol:ethanol (Piermarini et al., 1973). A ruby crystal $\sim 30 \mu \mathrm{~m}$ in diameter was placed in the sample chamber to monitor the pressure. Pressure was calibrated by measuring the shift of the $\mathrm{R}_{1}$ ruby fluorescence line (Barnett et al., 1973; Piermarini et al., 1975; King and Prewitt, 1980). The estimated precision of the pressure determination is $\pm 0.5 \mathrm{kbar}$. Pressure was determined immediately after loading the diamond cell at each pressure and again following data collection. In general, at least 24-48 hours elapsed between loading and the start of data collection, during which time some relaxation occurred. The pressures quoted for each experiment were those determined following the completion of data collection.

Initial loading was at 12.2 kbar , followed by data collection at 25.4 kbar . After this, the diamond cell was opened to move the crystal back to the center of the gasket hole. Following data collection at 34.6 kbar , the cell was again opened to move the crystal back to the center. Because of the thickness of the gasket at 12 kbar , a significant amount of shielding of the X-ray beam occurred. Therefore, the refinements at this pressure will not be considered further here. However, the unit-cell
determination at this pressure appears quite good. Subsequent data collection at higher pressures was only minimally affected by gasket cutoff, resulting in a relatively small number of reflections which were excluded from the refinements.

Intensity data were collected in the fixed-phi mode and intensities were measured using the constant-precision scanning technique (Finger et al., 1973). All accessible reflections with $2 \theta$ less than $90^{\circ}$ in a sphere of reciprocal space were collected. Due to the unfavorable orientation of the crystal at 35 and 46 kbar , only reflections with small values of $l$ could be measured, resulting in the relatively large uncertainties in the $z$ coordinates for these refinements. All intensities were corrected for absorption due to the diamond and beryllium in the pressure cell, using the method described by Finger and King (1978).

Unit-cell parameters were determined at both room pressure and at high pressures from the settings for 20-24 centered reflections corrected for errors in crystal centering and diffractometer zeroes using the procedures of King and Finger (1979). The triclinic cell, with no constraints, was in every case consistent with rhombohedral symmetry, suggesting that hydrostatic stress was maintained during data collection. Unit-cell parameters are reported in Table 2.

Precession photos of the crystal were taken in both $h 0 l$ and $h k 0$ orientations following high-pressure data collection. These suggest no deterioration of the crystal as a result of compression nor was there any indication of twinning as has been observed in shock-compressed ilmenites (Sclar et al., 1973).

## Absorption correction

Absorption corrections were applied to all intensity data using linear absorption coefficients varying from 106.3 to $103.1 \mathrm{~cm}^{-1}$ for the high-temperature data and 106.3 to $109.0 \mathrm{~cm}^{-1}$ for the high-pressure data. The crystals studied at high temperature and high pressure measured $\sim 0.06 \times 0.08 \times 0.12 \mathrm{~mm}$ and $\sim 0.05 \times 0.07 \times$ 0.10 mm , respectively. Extinction factors were also calculated for all reflections. Although it would have been better to use a constant absorption coefficient for all data sets, we are confident that this inadvertent error has not significantly affected the final results. Examination of the transmission and extinction factors indicates that the

Table 2. Unit-cell parameters of ilmenite at high pressure

| $P$ (kbar) | $a\left(\frac{1}{4}\right)$ | $c(\AA)$ | $v\left(k^{3}\right)$ | d/a |
| :---: | :---: | :---: | :---: | :---: |
| 0.001 | 5.0875 (5)* | 14.0827 (7) | 315.68 (4) | 2.7681 |
| 12.2 | 5.0785 (5) | $14.0358(17)$ | 313.50 (6) | 2.7638 |
| 25.4 | 5.0691 (4) | 13.9849 (13) | 311.21 (4) | 2.7589 |
| 34.6 | $5.0635(2)$ | 13.9518(16) | 309.79(4) | 2.7554 |
| 46.1 | $5.0561(4)$ | 13.9115 (19) | 307.99 (5) | 2.7514 |
| Standard deviations are given in parentheses and refer to the estimated error in the least significant units. This convention is followed in all tables. |  |  |  |  |

principal effect of varying the absorption coefficient was a simple scaling, by a maximum of $2-3 \%$ for transmission and $5-7 \%$ for extinction factors. The deviations in individual structure factors not accounted for by the overall scale factor and extinction parameter ( $r^{*}$ ) are smaller than other sources of statistical uncertainties in the data.

All reflection data were averaged prior to refinement to produce a set of symmetry-independent reflections. For the high-pressure data, a number of reflections that differed significantly from their equivalents were omitted prior to averaging.

## Structure refinements

Structure refinements were carried out using the leastsquares program RFInE4 (Finger and Prince, 1975). Starting coordinates were taken from Shirane et al. (1962), and the neutral atom scattering factors of Doyle and Turner (1968) were used. Real and imaginary parts of the anomalous dispersion corrections were also included for all atoms. Reflections were weighted on the basis of counting statistics, and those with $F<3 \sigma_{\mathrm{F}}$ (high temperature) or $I<2 \sigma_{\mathrm{I}}$ (high pressure) were excluded from the refinements. A scale factor, positional parameters, isotropic or anisotropic temperature factors, and an isotropic secondary extinction correction were varied in the final cycles of refinement. Final values of refined parameters are reported in Tables 3 and 4. Final observed and calculated structure factors for all data sets are listed in Table $5 .{ }^{2}$ Selected interatomic distances and angles (uncorrected for thermal motion) and coefficients of expansion and compression are given in Tables 6 and 7.

In the final cycles of refinement of the high-temperature data, the weighting scheme of Prince (1978) was employed. Although none of the refined parameters changed significantly as a result of this weighting scheme, the statistical parameters were improved. Also, from 3 to 5 observed reflections were rejected from each refinement on the basis of very high delta/sigma values. It is believed that these reflections may have been affected by "powder rings" arising from recrystallization of the hightemperature cement holding the crystal in place. For the high-pressure data, a few reflections having large delta/sigma values believed to have been affected by gasket cutoff were excluded.

The 35 kbar refinement is the most uncertain of the high-pressure results. The Fe atom $z$ coordinate in this refinement is particularly anomalous, lying off the trend defined by the $1 \mathrm{~atm}, 25$ and 46 kbar results by about 3 esd. This may have resulted from the unfavorable orientation of the crystal during data collection at this pressure, which was limited to reflections with $l$ less than or equal to 5 .

[^2]Table 3. Final positional parameters and isotropic temperature factors ( $\AA^{2}$ ) of ilmenite at high temperature

|  |  | $24^{\circ} \mathrm{C}$ | $400^{\circ} \mathrm{C}$ | $600^{\circ} \mathrm{C}$ | $800^{\circ} \mathrm{C}$ | $1050{ }^{\circ} \mathrm{C}$ | RTAH |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Fe | $x$ | 0 | 0 | 0 | 0 | 0 | 0 |
|  | $y$ | 0 | 0 | 0 | 0 | 0 | 0 |
|  | $z$ | 0.35537 (2) | 0.35605 (3) | 0.35650 (4) | 0.35689 (5) | 0.35732 (6) | 0.35542 (2) |
|  | B | $0.582(8)$ | 1.17(1) | 1.51(1) $\dagger$ | 1.86 (2) $\dagger$ | 2.37(2) $\dagger$ | 0.57 (1) |
| Ti | x | 0 | 0 | 0 | 0 | 0 | 0 |
|  | $y$ | 0 | 0 | 0 | 0 | 0 | 0 |
|  | $z$ | 0.14640 (2) | 0.14676 (4) | 0.14696 (4) | 0.14722 (5) | 0.14748 (6) | 0.14645 (3) |
|  | B | $0.458(7)$ | 0.87(1) | $1.10(1)+$ | 1.32 (1) $\dagger$ | $1.61(2) \dagger$ | 0.47 (1) |
| 0 | $x$ | 0.31743 (18) | $0.31796(29)$ | 0.31864 (34) | 0.31919 (39) | 0.31867 (44) | 0.31745 (26) |
|  | $y$ | $0.02332(17)$ | $0.02432(29)$ | $0.02438(34)$ | $0.02499(36)$ | 0.02491 (43) | 0.02345 (25) |
|  | $z$ | $0.24506(5)$ | 0.24479 (8) | $0.24479(11)$ | $0.24496(13)$ | 0.24475 (16) | 0.24485 (7) |
|  | B | $0.58(1)+$ | $1.06(2) \dagger$ | $1.31(2) \dagger$ | 1.65 (3) $\dagger$ | 1.99 (3) $\dagger$ | $0.58(2) \dagger$ |
| $r^{*}$ | $\left(\times 10^{5}\right)+\dagger$ | 1.09 (5) | 0.96 (6) | 0.83 (6) | 0.84 (7) | 1.05 (8) | 0.46 (4) |
| $N$ (obs) |  | 285 | 253 | 255 | 245 | 248 | 271 |
| $R(w t)$ |  | 0.015 | 0.020 | 0.024 | 0.026 | 0.028 | 0.020 |
| $R$ |  | 0.019 | 0.028 | 0.036 | 0.038 | 0.047 | 0.024 |

+ Equivalent isotropic $B$.
t+ Sacondary extinction parameter.


## Results

## Unit-cell parameters

Thermal expansion was nearly isotropic between room temperature and $1050^{\circ} \mathrm{C}$. The $a$ cell dimension increased linearly with temperature, whereas $c$ and the cell volume appeared to increase somewhat more rapidly at high temperature than at lower temperatures. However, because our methods for determining lattice parameters of this crystal did not explicitly take account of possible errors in crystal orientation and centering, the reported uncertainties are probably underestimated. It is likely that the true standard deviations of the high-temperature cell parameters are on the order of five times those

Table 4. Final positional parameters and isotropic temperature factors $\left(\AA^{2}\right)$ of ilmenite at high pressure

|  |  | 1 ata | 25.4 kbax | 34.6 kbar | 46.1 kbax |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Fe | $x$ | 0 | 0 | 0 | 0 |
|  | $y$ | 0 | 0 | 0 | 0 |
|  | z | 0.35540 (1) | 0.35562 (3) | 0.35530 (14) | 0.35580 (11) |
|  | B | $0.625(8){ }^{+}$ | 0.68 (2) | 0.63 (2) | 0.63 (2) |
|  | * | 0 | 0 | 0 | 0 |
|  | $y$ | 0 | 0 | 0 | 0 |
|  | $z$ | 0.14638 (2) | 0.14637 (4) | 0.14650 (19) | 0.14644 (14) |
|  | B | 0.505 (8) $^{\text { }}$ | $0.53(1)$ | 0.50(2) | 0.52 (2) |
| $\bigcirc$ | $x$ | $0.31719(11)$ | 0.31596 (30) | 0.31657 (36) | 0.31649 (32) |
|  | 9 | 0.02340 (12) | 0.02301 (27) | 0.02284 (29) | 0.02165 (26) |
|  | $z$ | $0.24502(4)$ | 0.24537 (11) | 0.24520 (28) | 0.24545 (25) |
|  | B | $0.62(1){ }^{+}$ | $0.61(2)$ | 0.63 (3) | 0.65 (3) |
| $r^{*}\left(x 10^{5}\right)^{+\dagger}$ |  | 2.27 (10) | 2.28(16) | 1.36(15) | 1.32(12) |
| $N$ (obs) |  | 308 | 140 | 75 | 91 |
| $R(w t)$ |  | 0.022 | 0.023 | 0.022 | 0.020 |
| R |  | 0.015 | 0.020 | 0.019 | 0.019 |

[^3]reported, and possibly more. Therefore, we cannot be confident about the curvature in the $c$-dimension with temperature. A small increase was noted in $c$ determined at room temperature after heating. This may have been due to misalignment of the crystal and is not believed to be indicative of any structural changes resulting from heating.

The $c$ cell dimension in ilmenite was approximately twice as compressible as $a$ between 1 atm and 46 kbar . The compression in both directions was curvilinear, decreasing slightly with increased pressure, while the cla ratio decreased linearly.

The volume compression data were fit to a BirchMurnaghan equation of state (Bass et al., 1981), in order to determine the zero-pressure isothermal bulk modulus and its pressure derivative. Since no rigorous constraint on $K_{\mathrm{o}}^{\prime}$ is available, both $K_{\mathrm{o}}$ and $K_{\mathrm{o}}^{\prime}$ were varied, yielding $K_{\mathrm{o}}=1.70(7) \mathrm{Mbar}$ and $K_{\mathrm{o}}^{\prime}=8(4)$. However, if $K_{\mathrm{o}}^{\prime}$ is assumed to be $4(1)$ (see discussion below), the derived value of $K_{0}=1.77(3) \mathrm{Mbar}$. (The assumed uncertainty in $K_{0}^{\prime}$ was included in calculating the uncertainty of $K_{0}$.) This compares well with values determined for a natural single crystal of ilmenite, $K_{\mathrm{o}}=1.79 \mathrm{Mbar}$ (Madelung and Fuchs, 1921; Birch, 1966), and on a polycrystalline specimen of magnesian ilmenite, $K_{0}=1.68(12) \mathrm{Mbar}$ (Liu et al., 1974). It is also in good agreement with the bulk modulus vs. molar volume systematics for ilmenite-type compounds (Liebermann, 1976), which suggest $K=1.74$ Mbar for $\mathrm{FeTiO}_{3}$ (R. C. Liebermann, pers. comm.).

## Structural changes

The ilmenite structure is based on the $\mathrm{R}_{2} \mathrm{O}_{3}$ corundum structure in which oxygens form a nearly hexagonal close-packed framework. Layers of edge-sharing actahedral cation sites extend in the (001) planes. Each cation shares one octahedral face with a cation in an adjacent layer, whereas the face opposite this is "shared" with a

Table 6. Selected interatomic distances $(\AA)$, angles $\left({ }^{\circ}\right)$, and thermal expansion coefficients of ilmenite at high temperature

|  | $24^{\circ} \mathrm{C}$ | $400^{\circ} \mathrm{C}$ | $600^{\circ} \mathrm{C}$ | $800^{\circ} \mathrm{C}$ | $1050^{\circ} \mathrm{C}$ | RTAH | $\alpha^{*}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Fe-0 | 2.2013 (8) | 2.219 (1) | 2.230 (2) | $2.238(2)$ | 2.248 (2) | $2.204(1)$ | 20.6 |
| $\mathrm{Fe}-\mathrm{O}$ | 2.0778 (8) | 2.086 (1) | 2.086 (2) | 2.088 (2) | 2.093 (2) | 2.080 (1) | 7.1 |
| <Fe-0> | 2.1396 | 2.152 | 2.158 | 2.163 | 2.171 | 2.142 | 14.3 |
| Ti-0 | 2.0886 (8) | 2.090 (1) | 2.095 (1) | $2.100(2)$ | 2.099 (2) | 2.087 (1) | 4.8 |
| ti-O | 1.8744 (8) | 1.879 (1) | 1.882 (2) | 1.885 (2) | 1.892 (2) | 1.874(1) | 9.1 |
| <Ti-0> | 1.9815 | 1.985 | 1.988 | 1.993 | 1.996 | 1.980 | 7.1 |
| QE** ( Fe ) | 1.0271 | 1.0285 | 1.0292 | 1.0300 | 1.0311 | 1.0272 |  |
| QE (Ti) | 1.0277 | 1.0273 | 1.0267 | 1.0262 | 1.0259 | 1.0278 |  |
| $\mathrm{FeO}_{6}$ vol. ( $\mathrm{A}^{3}$ ) | 12.562 | 12.766 | 12.855 | 12.930 | 13.052 | 12.604 |  |
| Tio ${ }_{6}$ vol. ( $A^{3}$ ) | 10.001 | 10.051 | 10.119 | 10.191 | 10.238 | 9.978 |  |
| $\mathrm{Fe}-\mathrm{Ti}$ | $2.9435(4)$ | $2.9570(7)$ | 2.9663 (8) | 2.975 (1) | 2.985 (1) | $2.9450(5)$ | 13.7 |
| $\mathrm{Fe}-\mathrm{Fe} 1^{\dagger}$ | 3.0027(1) | $3.0182(2)$ | 3.0269 (3) | 3.0352 (3) | $3.0457(4)$ | 3.0033 (2) | 14.0 |
| $\mathrm{Fe}-\mathrm{Fe} 2$ | 4.0744 (4) | 4.0677 (6) | 4.063 (1) | $4.061(1)$ | 4.059 (1) | 4.0752 (4) | -3.6 |
| Ti-Ti 1 | 2.9928 (1) | 3.0023 (2) | $3.0072(2)$ | $3.0117(3)$ | $3.0180(3)$ | $2.9928(2)$ | 8.2 |
| Ti-Ti 2 | 4.1242 (4) | 4.1471 (8) | 4.161 (1) | 4.177 (1) | 4.196 (1) | 4.1279 (6) | 17.0 |
| -0-0 $1^{\dagger \dagger}$ | 2.701 (1) | 2.712 (2) | 2.723 (3) | 2.731 (3) | 2.734 (3) | $2.701(2)$ | 11.9 |
| --0 2 | 3.216 (1) | 3.234 (2) | 3.238 (3) | 3.247 (3) | 3.257 (3) | 3.217 (2) | 12.4 |
| 0-0 3 | 3.051 (1) | $3.072(2)$ | 3.080 (3) | 3.086 (4) | 3.098 (4) | $3.058(2)$ | 15.0 |
| 0-0 4 | 3.005 (1) | 3.019 (2) | 3.023 (3) | 3.024 (3) | 3.038 (4) | $3.010(2)$ | 10.7 |
| 0-0 5 | 2.921 (1) | 2.925 (2) | 2.927 (3) | 2.928 (3) | 2.939 (3) | 2.920 (2) | 6.0 |
| 0-0 6 | $2.607(1)$ | 2.605 (2) | 2.611 (3) | 2.619 (4) | 2.620 (4) | $2.602(2)$ | 4.9 |
| 0-0 7 | 2.885 (1) | $2.892(2)$ | 2.896 (3) | 2.907 (3) | 2.911 (4) | 2.882 (2) | 8.8 |
| $\mathrm{O}-\mathrm{Fe}-\mathrm{O}$ | 75.68 (3) | 75.35 (5) | 75.26 (6) | 75.20(7) | 74.88 (8) | 75.55 (4) |  |
| $\mathrm{O}-\mathrm{Fe}-\mathrm{O}$ | 90.92 (3) | 91.02 (5) | 91.00 (6) | 90.95 (7) | 90.97 (8) | 91.03 (4) |  |
| $\mathrm{O}-\mathrm{Fe}-\mathrm{O}$ | 89.15 (4) | 98.99 (6) | 88.87 (8) | 88.64 (9) | 88.7(1) | 89.23 (6) |  |
| $\mathrm{O}-\mathrm{Fe}-\mathrm{O}$ | 101.40(3) | 101.65 (4) | 101.81 (6) | 102.07(7) | 102.18(8) | 101.32(4) |  |
| O-Ti-O | 80.56 (3) | 80.88 (5) | 81.06(7) | 81.13 (8) | 81.26 (9) | 80.65 (4) |  |
| O-Ti-O | 82.07 (3) | 81.84 (5) | 81.89(7) | 81.97 (8) | 81.9(1) | 81.97 (4) |  |
| O-Ti-O | 93.28(4) | 93.37(7) | 93.33 (9) | 93.5(1) | 93.5(1) | 93.24 (6) |  |
| O-Ti-0 | 102.35(3) | 102.26(5) | 102.14 (6) | 101.88(7) | 101.88(9) | 102.40(4) |  |

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\({ }^{*} \alpha=\left[\left(1 / d_{24}\right)\left(d_{1050^{-d}}^{24}\right) / 1026\right] \times 10^{6}\left({ }^{\circ} \mathrm{C}^{-1}\right)\).
**Quadratic elongation.
†Metal-metal distances are indicated as follows:
1--across shared edge between adjacent metal sites; 2-across vacant octahedral position, along [00l].
†年xygen-oxygen distances are indicated as follows:
I--Fe-Ti shared face; 2-Fe site, face opposite the shared face; 3--Fe site, shared edge; 4--Fe site, unshared edge;
5--Ti site, face opposite the shared face; 6--Ti site, shared edge; 7--Ti site, unshared edge.
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vacant octahedral position. In ilmenite, Fe and Ti are completely ordered into alternating layers along $\mathbf{c}$, so that each cation shares three edges with other octahedral cations of the same type, but the common octahedral face is shared with a cation of the other type. On either side of each vacant octahedral position along $\mathbf{c}$ lie cations of the same type. Both cation sites lie on threefold axes, and each has a single variable positional parameter, $z$. Deviations of $z$ from $1 / 3$ and $1 / 6$ for Fe and Ti sites, respectively, are indicative of "puckering" of the cation layers above and below planes parallel to ( 001 ).
The Fe and Ti atom $z$ coordinates both increased linearly with temperature, corresponding to movement toward the centroid of the coordination polyhedron for Ti and away from the centroid position for Fe. "Puckering" of the Fe layer was significantly increased, and the $\mathrm{Fe}-\mathrm{Fe}$ distance across the vacant octahedral site in the Ti layer actually decreased at high temperatures. The longer of the two independent $\mathrm{Fe}-\mathrm{O}$ bonds increased nearly three times as rapidly as the shorter distance, whereas for the Ti atom, the shorter bond distance increased twice as rapidly as the longer one (see thermal expansion coefficients in Table 6). Thus, the $\mathrm{FeO}_{6}$ octahedron became significantly more distorted at high temperature, while
the $\mathrm{TiO}_{6}$ octahedron became more regular, as indicated by the quadratic elongation (Robinson et al., 1971; see Table 6). Mean $\mathrm{Fe}-\mathrm{O}$ and Ti-O distances increased linearly with temperature, with $\langle\mathrm{Fe}-\mathrm{O}\rangle$ increasing about twice as much as $\langle\mathrm{Ti}-\mathrm{O}\rangle$ between 24 and $1050^{\circ} \mathrm{C}$.

The fractional coordinate $z$ of the Fe atom increased slightly with pressure, whereas the $\mathrm{Ti} z$ coordinate was unchanged. Small shifts were found for all three oxygen coordinates, with $y$ changing the most and $z$ the least with increasing pressure. The Fe and Ti sites were affected quite differently by compression. The longer of the two independent $\mathrm{Fe}-\mathrm{O}$ distances was somewhat less compressible than the shorter $\mathrm{Fe}-\mathrm{O}$ distance, whereas the longer Ti-O distance was more than twice as compressible as the shorter one (Table 7). However, overall distortions of the $\mathrm{FeO}_{6}$ and $\mathrm{TiO}_{6}$ polyhedra, as measured by the quadratic elongation and octahedral angle variance, were only slightly affected by pressure. Mean Fe-O and Ti-O distances decreased linearly with pressure, with the $\langle\mathrm{Fe}-\mathrm{O}\rangle$ distance about twice as compressible as $\langle\mathrm{Ti}-$ 0).

Although the change in the oxygen $z$ coordinate with pressure is small, it reflects the difference in behavior between the Fe and Ti sites. The octahedral height

Table 7. Selected interatomic distances ( $\AA$ ), angles $\left({ }^{\circ}\right)$, and coefficients of compressibility of ilmenite at high pressure

|  | 1 atm | 25.4 kbar | 34.6 kbar | 46.1 kbar | $8{ }^{*}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Fe-O | 2.2005 (6) | 2.184 (1) | 2.181 (3) | 2.180 (3) | 20.2 |
| $\mathrm{Fe}-\mathrm{O}$ | 2.0784 (5) | 2.067 (1) | 2.065 (2) | 2.052 (2) | 27.6 |
| < Fe -O> | 2.1395 | 2.126 | 2.123 | 2.116 | 23.8 |
| Ti-0 | 2.0871 (5) | 2.076 (1) | 2.072 (3) | 2.072 (3) | 15.7 |
| Ti-0 | 1.8742 (5) | 1.872 (1) | 1.868 (3) | 1.869 (2) | 6.0 |
| <Ti-O> | 1.9806 | 1.974 | 1.970 | 1.970 | 11.6 |
| QE** ( Fe ) | 1.0272 | 1.0277 | 1.0268 | 1.0275 |  |
| QE (Ti) | 1.0279 | 1.0279 | 1.0276 | 1.0272 |  |
| $\mathrm{FeO}_{6} \text { vol. }\left(\mathbb{A}^{3}\right)$ | 12.558 | 12.303 | 12.277 | 12.147 |  |
| $\mathrm{TiO}_{6}$ vol. ( $\mathrm{A}^{3}$ ) | 9.984 | 9.881 | 9.829 | 9.839 |  |
| $\mathrm{Fe}-\mathrm{Ti}$ | 2.9436 (4) | 2.9263 (8) | 2.913 (4) | 2.913 (3) | 22.5 |
| Fe-Pe ${ }^{+}{ }^{+}$ | 3.0023 (3) | 2.9923 (3) | 2.9870 (8) | 2.9853 (7) | 12.3 |
| Fe-Fe 2 | 4.0727 (3) | 4.038 (1) | 4.038 (4) | 4.012 (3) | 32.3 |
| Ti-Ti 1 | 2.9923 (3) | 2.9812 (3) | 2.977 (1) | 2.9729 (8) | 14.1 |
| Ti-Ti 2 | 4.1229 (6) | 4.094 (1) | 4.088 (5) | 4.074 (4) | 25.7 |
| $0 \rightarrow 01^{\text {+ }}$ | 2.698 (1) | 2.679 (2) | 2.682(3) | 2.682 (3) | 12.9 |
| 0-0 2 | 3.217 (1) | 3.214 (2) | 3.200 (2) | 3.185 (2) | 21.6 |
| 0-0 3 | 3.051 (1) | 3.022 (3) | 3.020 (7) | 3.003 (6) | 34.1 |
| O-0 4 | 3.005 (1) | 2.982 (3) | 2.979 (7) | 2.968 (6) | 26.7 |
| $0-0$ | 2.921 (1) | 2.918 (2) | 2.912 (2) | 2.913 (2) | 5.9 |
| 0-0 6 | 2.604 (1) | 2.596 (3) | 2.590 (7) | 2.595 (6) | 7.5 |
| $0-07$ | 2.884 (1) | 2.877 (3) | 2.866 (6) | 2.861 (5) | 17.3 |
| $\mathrm{O}-\mathrm{Fe}-\mathrm{O}$ | 75.61 (2) | 75.66 (6) | 75.88 (14) | 75.90 (12) |  |
| $\mathrm{O}-\mathrm{Fe}-\mathrm{O}$ | 90.93 (2) | 90.56 (6) | 90.63 (13) | 90.33 (11) |  |
| $0-\mathrm{Fe}-\mathrm{O}$ | 89.18 (3) | 89.04 (8) | 89.06 (13) | 89.00 (12) |  |
| $\mathrm{O}-\mathrm{Fe}-\mathrm{O}$ | 101.41(2) | 101.76(6) | 101.55(12) | 101.82(11) |  |
| O-Ti-O | 80.53 (2) | 80.37 (6) | 80.65 (14) | 80.64 (12) |  |
| O-Ti-O | 82.02 (2) | 82.06 (6) | 81.99(16) | 82.19(14) |  |
| O-Ti-O | 93.31 (3) | 93.40 (8) | 93.19(13) | 92.96(12) |  |
| O-Ti-O | $102.38(2)$ | 102.39(6) | 102.41(17) | 102.41(14) |  |

$\left.{ }^{*} \beta=-\left(11 / d_{o}\right)\left(d_{46 . I} d_{o}\right) / 46.1\right] \times 10^{5}\left(\mathrm{kbar}^{-1}\right)$.
**Quadratic elongation.
$\dagger_{\text {Metal-metal }}$ distances are indicated as follows:
1 - across shared edge between adjacent metal sites;
2 - across vacant octahedral position, along [001].
†toxygen-oxygen distances are indicated as follows:
I--Fe-Ti shared face; $2--F e$ site, face opposite the
shared face; 3-Fe site, shared edge; 4--Fe site,
unshared edge; 5--Ti site, face opposite the shared
face; 6--Ti site, shared edge; 7--Ti site, unshared edge.
(distance between upper and lower oxygen layers along c) is dependent upon the $c$ length and the oxygen $z$ coordinate. The slight increase in $z_{\text {oxy }}$ with increasing pressure indicates that the octahedral height of the Fe layer probably decreases more than twice as rapidly as that of the Ti layer. This decrease is also more than twice the linear compressibility in the a-direction. Thus, the Fe site is "flattened" relative to the Ti site, which compresses about equally along a and $c$. This is perhaps the reason for the decrease in $c / a$ with increasing pressure. The greater c-axis compression is, of course, also associated with more substantial shortening of metal-metal distances along c (i.e., $\mathrm{Fe}-\mathrm{Ti}$ across shared face, $\mathrm{Fe}-\mathrm{Fe}$ and $\mathrm{Ti}-\mathrm{Ti}$ across vacant sites) than between adjacent metal sites across shared edges.

## Cation distribution

In order to determine whether any disorder between Fe and Ti sites was present, direct cation site occupancy refinements were performed on all data sets. Total occupancies were constrained to the stoichiometric composition. No measureable disorder was found at any temperature or pressure, with estimated standard deviations in the occupancies of $\pm 1-2 \%$. The observed mean bond distances of the octahedral sites are also consistent with complete order having been maintained under all conditions.

## Temperature factors

Thermal ellipsoids calculated from all data collected at 1 atm pressure are presented in Table 8. Due to the paucity of intensity data, no attempt was made to refine anisotropic temperature factors for the high-pressure data.

Table 8. RMS amplitudes of vibration $(\AA)$ and orientation of thermal ellipsoids

|  | RTP* | $24^{\circ} \mathrm{C}$ | $400^{\circ} \mathrm{C}$ | $600^{\circ} \mathrm{C}$ | $800^{\circ} \mathrm{C}$ | $1050^{\circ} \mathrm{C}$ | RTAH |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Fe atom: |  |  |  |  |  |  |  |
| Perpendicular to $c$ | 0.0876 (6) | 0.086 | 0.122 | $0.136(1)$ | 0.150 (1) | 0.169 (1) | 0.085 |
| Parallel to c | 0.0916 (9) | 0.086 | 0.122 | 0.143 (1) | 0.160 (1) | $0.182(1)$ | 0.085 |
| Ti atom: |  |  |  |  |  |  |  |
| Parallel to $c$ | 0.0841 (10) | 0.076 | 0.105 | $0.117(1)$ | 0.126 (2) | 0.142 (2) | 0.077 |
| Perpendicular to c | 0.0778 (6) | 0.076 | 0.105 | 0.119 (1) | $0.131(1)$ | 0.143 (1) | 0.077 |
| Oxygen atom: |  |  |  |  |  |  |  |
| Axis 1 | $0.0803(14)$ | 0.077 (2) | $0.104(3)$ | $0.118(3)$ | 0.128 (3) | 0.143 (4) | 0.076 (3) |
| Angle with a | 52(11)** | 28 (6) | 65 (17) | 33 (74) | 39 (9) | 74 (25) | 60(24) |
| Angle with b | 70(10) | 95 (12) | 63 (9) | 117 (56) | 82 (7) | 61 (15) | 71 (15) |
| Angle with c | 104(6) | 78 (15) | 120 (14) | 57 (67) | 101 (8) | 130 (13) | 123(17) |
| Axis 2 | 0.0850 (13) | 0.082 (2) | $0.110(3)$ | 0.120 (3) | 0.143 (3) | 0.148 (3) | 0.081 (3) |
| Angle with a | 41(11) | 84 (17) | 141 (14) | 112 (96) | 59 (10) | 158 (19) | 144(22) |
| Angle with $b$ | 143 (7) | 126(5) | 67(10) | 118 (55) | 127 (7) | 61 (15) | 59(10) |
| Angle with $c$ | 64 (5) | 39 (8) | 129(13) | 58 (68) | 41 (8) | 112 (18) | 125 (18) |
| Axis 3 | $0.1003(13)$ | 0.097 (2) | $0.132(3)$ | 0.147 (3) | 0.160 (3) | 0.182 (3) | 0.099 (3) |
| Angle with a | 102 (3) | 117 (4) | 118 (5) | 113 (4) | 112 (5) | 105 (4) | $108(6)$ |
| Angle with $b$ | $60(3)$ | 36 (5) | $37(4)$ | 41 (4) | 38 (7) | 43 (4) | 38 (5) |
| Angle with $C$ | 30(3) | 54 (5) | 54 (4) | 49 (4) | 52 (7) | 48 (3) | 53 (5) |

*Crystal used for high-pressure study measured at room temperature and pressure.
**Angles given in degrees.

For the crystal studied at high temperature, thermal vibration of Fe and Ti was found to be essentially isotropic at room temperature and $400^{\circ} \mathrm{C}$ and only slightly anisotropic at higher temperatures. However, the room temperature and pressure refinement of the high-pressure crystal did indicate slightly anisotropic vibration of Fe and Ti , with the longer axes parallel to c . The oxygen ellipsoid was significantly anisotropic at all temperatures, with the direction of maximum vibration lying in the a-c plane, about $50-55^{\circ}$ from c for the high-temperature crystal and $30^{\circ}$ from c for the high-pressure crystal. The discrepancies between the two crystals at room temperature and pressure are not serious. Due to improved data collection procedures, we feel that the ellipsoids determined for the high-pressure crystal are probably somewhat more reliable.

Equivalent isotropic temperature factors (Hamilton, 1959) for the high-pressure crystal are slightly higher than those for the high-temperature crystal at room temperature. The $\mathrm{B}_{\mathrm{eq}}$ for Ti increased linearly with temperature, whereas those for Fe and O increased more rapidly at higher temperatures. Isotropic temperature factors for all atoms were essentially unchanged with pressure.

## Discussion

Mean $\mathrm{Fe}-\mathrm{O}$ and $\mathrm{Ti}-\mathrm{O}$ distances, uncorrected for thermal motion, increased linearly with temperature. The increase in $\langle\mathrm{Fe}-\mathrm{O}\rangle$ distance was twice as great as that for〈Ti-O〉. Values of thermal expansion coefficients (Table 6) compare well with measured values of mean $\mathrm{Fe}^{2+}-\mathrm{O}$ distances in fayalite (Smyth, 1975), wüstite (Carter, 1959), orthoferrosilite (Sueno et al., 1976), and hedenbergite (Cameron et al., 1973). The mean $\mathrm{Ti}^{4+}-\mathrm{O}$ distance expansion was also comparable to values for this species reported for anatase (Horn et al., 1972), rutile and brookite (Meagher and Lager, 1979), and titanite (Taylor and Brown, 1976). The lower rate of expansion for octahedral $\left\langle\mathrm{T}^{i^{4+}}-\mathrm{O}\right\rangle$ is consistent with the greater Pauling bond strength (cation charge/coordination number) of $\mathrm{Ti}^{4+}-\mathrm{O}$ bonds. However, as was also pointed out by Meagher and Lager (1979), the expansion coefficients for $\left\langle\mathrm{Ti}^{4+}-\mathrm{O}\right\rangle$ distances are substantially greater than those expected from the trend pointed out by Hazen and Prewitt (1977).

The polyhedral bulk moduli, $K_{\mathrm{p}}=1 / 3 \beta$ (Hazen and Finger, 1979), of the Fe and Ti sites in ilmenite are 1.4(1) and $2.9(5) \mathrm{Mbar}$, respectively. The Fe value compares well with values derived from compression of wustite (Clendenen and Drickamer, 1966; Will et al., 1980) of about $1.6 \mathrm{Mbar} . K_{\mathrm{p}}$ for the Ti site is also consistent with the value of $2.2(8)$ reported by Hazen and Finger (1981) for $\mathrm{TiO}_{2}$. The value determined in this study indicates that the $\mathrm{TiO}_{6}$ polyhedron is among the least compressible octahedra yet found. The polyhedral bulk modulus for the Fe site is compatible with the semiempirical relation derived by Hazen and Finger (1979), although the Ti site has a somewhat smaller $K_{\mathrm{p}}$ than is predicted by this
relation. Hazen and Finger (1981) also noted that $K_{\mathrm{p}}$ values for tetravalent ions show systematic deviations from the trend suggested by Hazen and Finger (1979).

The ilmenite structure is derived from the corundum structure by ordering of the octahedral sites into two nonequivalent layers. It is thus interesting to compare these results with those for $\mathrm{R}_{2} \mathrm{O}_{3}$ corundum structures reported by Finger and Hazen (1980). The compression in ilmenite is relatively anisotropic, with c/a decreasing about twice as rapidly as in $\mathrm{Fe}_{2} \mathrm{O}_{3}$, as compared with no change with pressure for $\mathrm{Al}_{2} \mathrm{O}_{3}$ and $\mathrm{Cr}_{2} \mathrm{O}_{3}$, and a rapid increase for $\mathrm{V}_{2} \mathrm{O}_{3}$. The decrease in cla ratio and change in Fe coordinate in ilmenite are indicative of further departure from hexagonal close packing and the ideal corundum structure with increased pressure. However, this is partially offset by the changing oxygen $y$ and $z$ coordinates, which become more corundum-like at high pressure. Whereas the structural parameters for $\mathrm{Fe}_{2} \mathrm{O}_{3}$, $\mathrm{Cr}_{2} \mathrm{O}_{3}$, and $\mathrm{Al}_{2} \mathrm{O}_{3}$ remain essentially constant as pressure is increased, somewhat more distortion is observed in ilmenite, presumably due to the presence of two nonequivalent cation sites.

The bulk modulus and its pressure derivative are indicative of the mechanism of compression of crystal structures (Hazen and Finger, 1978). In a fully edgelinked structure such as that of ilmenite, the compressibility is expected to be mainly determined by shortening of M-O bonds. The fraction of the unit-cell volume occupied by the cation polyhedra in ilmenite is, in fact, constant between 1 atm and 46 kbar , as it is between 24 and $1050^{\circ} \mathrm{C}$ as well. Thus, although some distortion of the structure occurs under pressure, the overall rate of compression must be controlled by the compressibilities of the component polyhedra themselves. This being the case, it is reasonable to suggest that the actual $K_{\mathrm{o}}^{\prime}$ for ilmenite is probably in the range of 4 to 5 , as is observed in similar materials. Therefore, the bulk modulus determined with $K_{\mathrm{o}}^{\prime}$ constrained to be 4(1), which gave $K_{\mathrm{o}}=1.77(3) \mathrm{Mbar}$ (see above), may provide a slightly better estimate than the value determined with both $K_{\mathrm{o}}$ and $K_{\mathrm{o}}^{\prime}$ allowed to vary ( $K_{\mathrm{o}}=1.70(7), K_{\mathrm{o}}^{\prime}=8(4)$ ).

Some of the difference in compressional behavior between the Fe and Ti sites can perhaps be understood by considering the nature of the structure in the a and $c$ directions. The ilmenite structure consists of alternating layers of edge-sharing Fe and Ti octahedra stacked along c. Compression along a is constrained by the more rigid polyhedron, i.e., Ti, and both cation sites are compressed at virtually identical rates in this direction. Parallel to c, however, the two cation layers may be compressed more or less independently of one another. Therefore, differences between the overall volume compressibilities of the two sites may be expected to be expressed mainly in the $\mathbf{c}$ direction. Of course, this does not necessarily require a change in the cla ratio unless one of the sites compresses equally in both directions, as Ti does in ilmenite. Similar


Fig. 1. Variation of ilmenite cell parameters with $V / V_{o}$.
behavior may also pertain to compression of other minerals having the ilmenite structure.

## Comparison of temperature and pressure effects

Hazen and Prewitt (1977) suggested that in compounds where all component polyhedra have similar values of $\alpha / \beta$, the mechanism of compression will be essentially equivalent to that of cooling, i.e., compression and expansion have inverse effects. Although this criterion is satisfied in ilmenite, clearly the mode of compression is not the inverse of expansion. In Figure 1, $a, c$, and $c / a$ are plotted against $V / V_{0}$ (unit-cell volume at $T, P$ divided by volume at $24^{\circ} \mathrm{C}, 1 \mathrm{~atm}$ ). The striking difference between expansion and compression is clearly demonstrated by $c / a$. The linear decrease with pressure is contrasted with a small decrease followed by an even smaller increase with increasing temperature. Whereas the high-temperature behavior is characterized by nearly isotropic expansion of the unit cell and significant structural distortion, at high pressure the structural changes are smaller and the unitcell compression is quite anisotropic.
Figure 2 demonstrates the linear relationship between mean $\mathrm{Fe}-\mathrm{O}$ and $\mathrm{Ti}-\mathrm{O}$ distances and $V / V_{\mathrm{o}}$ in ilmenite.


Fig. 2. Variation of mean $\mathrm{Fe}-\mathrm{O}$ and $\mathrm{Ti}-\mathrm{O}$ distances in ilmenite with $V / V_{o}$.


Fig. 3. Variation of $\mathrm{Fe}-\mathrm{Fe}$ and $\mathrm{Ti}-\mathrm{Ti}$ distances across vacant octahedral sites in ilmenite with $V / V_{0}$.

Thus, the difference between expansional and compressional behavior is not related to the mean $\mathrm{M}-\mathrm{O}$ distances. It is interesting, however, to observe the individual bond distances which make up the coordination polyhedra. In both the Fe and Ti sites, the more expandable of the two independent $\mathrm{M}-\mathrm{O}$ bonds are also the less compressible ones, the opposite of what might be expected if the rates of expansion and compression were proportional to individual bond strengths. The latter notion is reasonably useful when considering mean bond distances, however.
The oxygen coordinates vary approximately inversely with temperature and pressure, although changes in the cation coordinates are decidedly noninverse. As with increasing pressure, the octahedral height (along $c$ ) of the Fe layer probably changes much more rapidly than that of the Ti layer at high temperature. However, the net expansion along $\mathbf{c}$ is about equal to the expansion along a. This is perhaps due to metal-metal repulsion between adjacent Ti sites, resulting in increased separation and consequently greater expansion of the Ti layer along a than c .

The displacement of the Fe position at high temperature may also reflect the importance of metal-metal repulsions. The retreat of the Fe position away from the Ti across the shared face is suggestive of a significant repulsive interaction. This results in greater "puckering", of the Fe layer and an increase in $\mathrm{Fe}-\mathrm{Fe}$ distances across shared edges. On the other hand, this shift also results in a decrease in the $\mathrm{Fe}-\mathrm{Fe}$ separation across the vacant position along $\mathbf{c}$ at high temperature (Figure 3). Presumably the $\mathrm{Fe}-\mathrm{Fe}$ interaction in this direction is weaker than the corresponding Ti-Ti repulsion, resulting in the tendency of the Fe site to distort in this fashion.

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[^1]:    *Standard deviations are given in parentheses and refer to the estimated error in the least significant units. This convention is followed in all tables.
    ** Room temperature after heating.

[^2]:    ${ }^{2}$ To receive a copy of Table 5, order Document AM-83-235 from the Business Office, Mineralogical Society of America, 2000 Florida Avenue, N. W., Washington, D. C. 20009. Please remit $\$ 5.00$ in advance for the microfiche.

[^3]:    ${ }^{\dagger}$ Equivalent isotropic B.
    ${ }^{\dagger \dagger}$ Secondary extinction parameter.

