Mn-Mg disordering in cummingtonite: a high-temperature neutron powder diffraction study

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ABSTRACT

The crystal structure of a manganoan cummingtonite, composition ^[M4](Na_{0.13}Ca_{0.41}Mg_{0.46}Mn_{1.00}) ^[M1,2,3](Mg_{4.87}Mn_{0.13})[Si₈O₂₂](OH)₂, (Z = 2), a = 9.5539(2) Å, b = 18.0293(3) Å, c = 5.2999(1) Å, β = 102.614(2)° from Talcville, New York, has been refined at high temperature using *in situ* neutron powder diffraction. The P2₁/m to C2/m phase transition, observed as spontaneous strains + ϵ_1 = - ϵ_2 , occurs at ~107°C. Long-range disordering between Mg²⁺ and Mn²⁺ on the M(4) and M(2) sites occurs above 550°C. Mn²⁺ occupies the M(4) and M(2) sites preferring M(4) with a site-preference energy of 24.6 ± 1.5 kJ mol⁻¹. Disordering induces an increase in χ_{Mn}^{M2} and decrease in χ_{Mn}^{M4} at elevated temperatures. Upon cooling, the ordered states of cation occupancy are 'frozen in' and strains in lattice parameters are maintained, suggesting that re-equilibration during cooling has not taken place.

Keywords: cummingtonite, order-disorder, cation partitioning, neutron diffraction, phase transition.

Introduction

A quantitative knowledge of the temperatures and pressures of formation of mineral assemblages is fundamental to understanding the thermal evolution of the Earth, and to the development of wellconstrained petrological and geophysical models. For some time, geothermometric and geobarometric deductions have been based on the compositional variations of coexisting rockforming minerals (e.g. cation partitioning between orthopyroxene/clinopyroxene; orthopyroxene/garnet; magnetite/ilmenite). Information on cooling rates (geospeedometry) is also potentially available from the knowledge of intracrystalline cation site partitioning (e.g. cation ordering within pyroxene or olivine).

Amphiboles provide ideal candidates for application as thermometric indicators, since non-convergent cation ordering occurs within them as a function of temperature, and they are stable across a wide range of temperatures, pressures and rock compositions, corresponding to environments from the crust to the upper mantle (including important subduction environments). Very limited use has been made of amphiboles as thermometric indicators, however, because of their compositional and structural complexity, and a limited understanding of their thermodynamic properties. The crystal-chemical complexity that makes amphiboles such a challenge is itself a potential recorder of the thermal history of the mineral, and in so doing can lock away a wealth of information on the timetemperature paths of the rocks in which they are found. If a working knowledge can be established of the temperature dependence of cation ordering in amphiboles, a treasure-trove of thermometric petrological information is likely to become available.

This is the first part of a wider investigation into the temperature-dependent cation ordering within the cummingtonite-grunerite series, a group of Mg-Fe-Mn-Li amphiboles. The cummingtonite-grunerite series of amphiboles are monoclinic and in the system described by Leake (1997), have the general series formula

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 $(Mg,Fe^{2+},Mn,Li)_7Si_8O_{22}(OH)_2$ (Li <1.00). The term cummingtonite applies to compositions with Mg/(Mg+Fe^{2+}) ≥ 0.50 , grunerite being the Fe²⁺-rich end-member. The solid-solution endmembers (Mn₂Mg₅) and (Mn₂Fe_5²⁺) correspond to manganocummingtonite and manganogrunerite respectively. Cummingtonite occurs as polymorphs with space groups C2/m and P2₁/m with a phase transition occurring at relatively low temperatures for all natural compositions. Figure 1 shows the structure of a cummingtonite viewed parallel to (100).

Following reports (Bown, 1966) of a primitive structure in a Mg-rich Fe-Mg-Mn amphibole, Ross et al. (1968) suggested the possibility of the phase transition by analogy of $P2_1/m$ cummingtonite with pigeonite (and its $P2_1/c-C2/c$ transition). The $P2_1/m$ structure is only observed in Fe-Mg-Mn amphiboles and is restricted to those where Mg occupies 70-90% of B sites (Maresch and Czank, 1988). Upon substitution of Mn²⁺ and Fe^{2+} for the smaller Mg²⁺, the crystal structure is forced to revert to C2/m symmetry. Yang and Smyth (1996) provide evidence that the effective size of the M(4) cation controls the stability of the C2/m and $P2_1/m$ structures. Yang and Hirschmann (1995) reported a compositional dependence of the transition such that, at room temperature, cummingtonite with $X_{Mg}^{M4} > 0.15 \pm 0.02$ will have $P2_1/m$ crystal structure. They also found ferromagnesian cummingtonite to be more stable in the $P2_1/m$ structure than manganoan cummingtonites with the same Mg-content. Also in this vein, Ghose and Ganguly (1982) found that cummingtonite with Fe/(Fe+Mg) = 0.22 has $P2_1/m$ symmetry. Hirschmann et al. (1994) reported $P2_1/m$ symmetry at room temperature in heattreated cummingtonites which had Fe/(Fe+Mg) as high as 0.38. Samples as iron-rich as Fe/(Fe+Mg) = 0.45 are also $P2_1/m$ (Ross *et al.*, 1969). Sueno *et* al. (1972) studied the $P2_1/m - C2/m$ phase transition by in situ high-temperature X-ray diffraction (XRD), following the disappearance of the 102 reflection of the (h + k = 2n + 1) set, representative of the primitive symmetry. They report a T_c of 100°C. The ferromagnesian cummingtonite investigated by Yang and Smyth (1996) shows a transition temperature of $\sim -30^{\circ}$ C.

Ordering of cations occurs in the octahedral strip, which represents the body of the 'I-beam' module in amphiboles and comprises three unique cation sites. In C2/m cummingtonite there are three pseudo-octahedral sites, M(1), M(2) and M(3) with point symmetry 2, 2 and 2/m respectively. The M(4) cation site sits at the edge of the octahedral strip. This site is surrounded by eight anions and has point symmetry 2. The coordination of the site varies with cation occupancy. The octahedral strip in $P2_1/m$ cummingtonite also contains three pseudo-octahedral cation sites but the M(1) and M(2) sites have point symmetry 1 and M(3) has point symmetry m. The general position and coordina-



FIG. 1. View down [100] of the cummingtonite structure, showing the M(1), M(2) and M(3) sites in the octahedral ribbon with adjacent M(4). Open circles show the positions of hydroxyls.

tion of the M(4) site is the same as for the C2/m structure but it has point symmetry 1 (Leake, 1997; Hawthorne, 1983).

We are focusing on metal cation partitioning between the M(4) site and the smaller octahedral sites M(1), M(2) and M(3). Whittaker (1949) showed that, in crocidolite, Mg²⁺ occupies the M(4) cation site in preference to Fe^{2+} . Ten years later using three dimensional least squares refinement of XRD data from a grunerite, Ghose and Hellner (1959) reported almost complete occupation of the M(4) site by Fe^{2+} and showed that surplus Fe²⁺ and Mg²⁺ were distributed randomly over the three remaining cation sites. Ghose (1961) determined the crystal structure of a cummingtonite from Quebec with particular interest paid to cation distribution and disordering. Work on Fe-Mg ordering in a cummingtonite by Hirschmann et al. (1994) revealed a strong preference of Fe^{2+} for the M(4) site relative to Mg. However, the first to recognize the potential of cummingtonite as a geothermometer were Ghose and Weidner (1972). Using basic principles of geothermometry that had previously been applied to pyroxenes with limited success (Mueller, 1970) and recognizing the similarity in composition, structure and order-disorder mechanisms in orthopyroxene and cummingtonite, they determined a system of temperature dependent cation ordering of Mg2+ and Fe2between the M(4) and M(1,2,3) sites.

Ghose and Yang (1989) refined the crystal structure and determined the cation distribution of a C2/m manganoan cummingtonite from Nsuta, Ghana. On the basis of bond-lengths they reported that the sequence of site preference of Mn^{2+} in the Mn-Mg amphibole is $M(4) \gg M(1) > M(2) > M(3)$ and put the compositional limit for the $P2_1/m$ to C2/m phase transition at ambient temperatures close to Mn₂Mg₅Si₈O₂₂(OH)₂. However, the kinetics of cation exchange are not fully understood and are largely unconstrained. Furthermore, what is known of cation ordering in amphiboles has been determined from room temperature studies in anneal and quench experiments, the underlying assumption being that equilibrium states are attained during annealing and retained during quenching. Recent studies of cation ordering in spinels and olivines have shown that the kinetics of re-ordering may be very rapid (Redfern et al., 1999). The possibility of rapid reequilibration during quenching and the details of the kinetic pathways away from equilibrium remain unaddressed.

In order to determine the high-*T* equilibrium behaviour and the non-equilibrium kinetics of cation ordering, we have undertaken *in situ* crystallographic studies of an iron-free manganoan cummingtonite from Talcville, New York (Ross *et al.*, 1969), using time of flight, neutron powder diffraction techniques.

Experimental procedure

Approximately 5 g of sample R14473 of natural Talcville cummingtonite of composition $[M4](Na_{0.13}Ca_{0.41}Mg_{0.46}Mn_{1.00})$ $[M_{1,2,3}](Mg_{4,87}Mn_{0,13})[Si_8O_{22}](OH)_2$ was used for neutron diffraction experiments. The composition of the cummingtonite was calculated by averaging electron microprobe analyses, normalized to 24 oxygens, of 20 separate crystals. The analyses were performed on a Cameca SX50 electron micro-probe. The sample was placed into a vanadium furnace inside the sample chamber of the POLARIS neutron powder diffractometer (Hull et al., 1992). The sample chamber was evacuated to a pressure of 10⁻⁶mbar. The sample was heated in increments of 50°C to a maximum of 700°C and assumed to have reached thermal equilibrium after ten minutes at each temperature plateau. Powder diffraction patterns were then collected over a period of 4-5 h at each temperature with 58 ³He gas tube detectors positioned at $2\theta = 145^{\circ}$ and 216 ZnS detectors at $2\theta = 90^{\circ}$. On cooling, further diffraction patterns were collected at temperatures of 500, 350 and 200°C. All diffraction patterns were refined using whole pattern fitting using the Rietveld method (Rietveld, 1969). This method was recently employed to study A-site partitioning in amphibole using X-ray diffraction (Sokolova et al., 2000). The structures were refined in space group C2/m (Z = 2) for experiments at all temperatures. The background was refined using ten coefficients of a Chebyshev function. The site occupancies of Mg^{2+} and Mn^{2+} on the M(1), M(2), M(3) and M(4) site were refined using chemical constraints. Neutron scattering lengths for all atoms were those given by Sears (1992). The starting model for the refinement used initial atomic coordinates from Sueno et al. (1972) and constrained all Mn to either the M(2) or M(4)sites after our previous unconstrained refinements yielded this result. Convergence of the least squares cycle was achieved for each refinement. R_{wp} factors of ~2% were achieved

TABLE 1. Refined structural parameters as a function of temperature. Figures in parentheses represent the estimated standard deviation. H(1)y, O(3) y, O(7)y, M(1)x, M(2)x, z, M(4)x and M(3)x, y, z are all 0. M(1)z and M(4)z are $\frac{1}{2}$. H(1)y, O(3) y, O(7)y, M(1)x, M(2)x, z, M(4)x and M(3)x, y, z are all 0. The fractional site occupancies of Na and Ca on M(4) are 0.065 and 0.205 respectively.

Atom							Tempera	$\frac{1}{1}$									
position	n 50	100	150	200	250	300	350	400	450	500	550	600	650	700	500	350	200
H(1) x z Uiso	0.2212(13) 0.7381(23) 4.68(27)	0.2215(13) 0.7481(24) 5.25(28)	0.2224(14) 0.7386(25) 6.05(32)	0.2225(15) 0.7377(27) 6.9(4)	0.2239(16) 0.7368(29) 7.7(4)	0.2241(16) 0.7362(29) 8.6(4)	0.2275(17) 0.7269(31) 9.3(5)	0.2261(18) 0.7287(33) 10.5(5)	0.2263(18) 0.7269(33) 10.6(5)	0.2277(19) 0.723(4) 11.5(6)	0.2257(21) 0.720(4) 12.2(6)	0.2235(22) 0.718(4) 12.6(7)	0.2269(23) 0.715(4) 13.3(7)	0.2265(23) 0.718(4) 13.9(8)	0.2255(20) 0.725(4) 11.4(6)	0.2264(17) 0.7335(31) 9.4(5)	0.2228(14) 0.7417(26) 6.96(35)
O(1) x y z Uiso	0.1164(4) 0.0877(2) 0.2154(7) 0.475(16)	0.1168(4) 0.0876(2) 0.2146(7) 0.479(16)	0.1168(4) 0.0877(2) 0.2153(7) 0.537(16)	0.1169(4) 0.0879(2) 0.2155(8) 0.592(16)	0.1168(4) 0.0879(2) 0.2157(8) 0.650(17)	0.1169(4) 0.0878(2) 0.2145(8) 0.666(17)	0.1170(4) 0.0878(2) 0.2159(8) 0.816(19)	0.1169(4) 0.0877(2) 0.2146(8) 0.766(18)	0.1169(4) 0.0878(2) 0.2146(8) 0.823(19)	0.1171(4) 0.0877(2) 0.2146(8) 0.883(19)	0.1169(4) 0.0880(2) 0.2163(9) 1.004(21)	0.1166(4) 0.0879(2) 0.2161(9) 1.062(21)	0.1167(4) 0.0880(2) 0.2163(9) 1.140(22)	0.1169(4) 0.0877(2) 0.2147(9) 1.132(23)	0.1166(4) 0.0878(2) 0.2158(9) 0.951(20)	0.1166(4) 0.0876(2) 0.2146(8) 0.761(18)	0.1166(4) 0.0875(2) 0.2142(7) 0.568(16)
O(2) x y z Uiso	0.1215(4) 0.1727(2) 0.7182(7) 0.475(1)	0.1215(4) 0.1726(2) 0.7188(7) 0.479(2)	0.1217(4) 0.1726(2) 0.7190(7) 0.537(16)	0.1217(4) 0.1726(2) 0.7190(7) 0.592(16)	0.1217(4) 0.1727(2) 0.7190(7) 0.650(17)	0.1215(4) 0.1728(2) 0.7187(10) 0.666(17)	0.1214(4) 0.1727(2) 0.7186(8) 0.816(19)	0.1214(4) 0.1728(2) 0.7188(8) 0.766(18)	0.1213(4) 0.1729(2) 0.7188(8) 0.823(19)	0.1210(4) 0.1729(2) 0.7188(8) 0.883(19)	0.1212(4) 0.1727(2) 0.7186(8) 1.004(21)	0.1213(4) 0.1727(2) 0.7190(9) 1.062(21)	0.1209(4) 0.1728(2) 0.7189(9) 1.140(22)	0.1207(4) 0.1730(2) 0.7185(9) 1.132(23)	0.1215(4) 0.1727(2) 0.7187(8) 0.951(20)	0.1215(4) 0.1729(2) 0.7184(8) 0.761(18)	0.1217(3) 0.1728(2) 0.7186(7) 0.568(16)
O(3) x z Uiso	0.1041(5) 0.7144(10) 0.475(16)	0.1040(5) 0.7139(10) .0479(116)	0.1039(5) 0.7141(10)) 0.537(16)	0.1041(5) 0.7140(10) 0.592(16)	0.1037(5) 0.7143(10) 0.650(17)	0.1030(5) 0.7151(10) 0.666(17)	0.1035(5) 0.7145(11) 0.816(19)	0.1028(5) 0.7155(10) 0.766(18)	0.1029(5) 0.7155(11) 0.823(19)	0.1021(5) 0.7158(11) 0.883(19)	0.1034(5) 0.7149(12) 1.004(21)	0.1037(6) 0.7146(12) 1.062(21)	0.1038(6) 0.7142(12) 1.140(22)	0.1032(6) 0.7142(12) 1.132(23)	0.1039(6) 0.7148(12) 0.951(20)	0.1032(5) 0.7152(10) 0.761(18)	0.1035(5) 0.7142(10) 0.568(16)
O(4) x y z Uiso	0.3773(4) 0.2467(2) 0.7812(8) 0.475(16)	0.3768(36) 0.2470(2) 0.7817(7) 0.479(16)	0.3774(4) 0.2471(2) 0.7828(8) 0.537(16)	0.3776(4) 0.2469(2) 0.7831(8) 0.592(16)	0.3773(4) 0.2468(2) 0.7833(8) 0.650(17)	0.3766(4) 0.2466(2) 0.7832(8) 0.666(17)	0.3779(4) 0.2463(2) 0.7839(8) 0.816(19)	0.3766(4) 0.2464(2) 0.7387(8) 0.766(18)	0.3768(4) 0.2462(2) 0.7837(8) 0.823(19)	0.3765(4) 0.2461(2) 0.7834(8) 0.883(19)	0.3775(4) 0.2459(2) 0.7838(9) 1.004(21)	0.3775(4) 0.2457(2) 0.7838(9) 1.062(21)	0.3775(4) 0.2455(2) 0.7835(9) 1.140(22)	0.3770(4) 0.2453(2) 0.7824(9) 1.132(23)	0.3775(4) 0.2458(2) 0.7837(9) 0.951(20)	0.3768(4) 0.2463(2) 0.7832(8) 0.761(18)	0.3768(4) 0.2467(2) 0.7822(8) 0.568(16)
O(5) x y z Uiso	0.3472(4) 0.1289(2) 0.0596(6) 0.475(16)	0.3469(4) 0.1292(2) 0.0605(6) 0.479(16)	0.3460(4) 0.1291(2) 0.0600(6) 0.537(16)	0.3450(4) 0.1288(2) 0.0590(6) 0.592(16)	0.3449(4) 0.1285(2) 0.0588(6) 0.650(17)	0.3443(4) 0.1284(2) 0.0588(6) 0.666(17)	0.3436(4) 0.1281(2) 0.0572(6) 0.816(19)	0.3431(4) 0.1281(2) 0.0578(6) 0.766(18)	0.3429(4) 0.1280(2) 0.0576(6) 0.823(19)	0.3426(4) 0.1278(2) 0.0565(6) 0.883(19)	0.3419(4) 0.1275(2) 0.0552(6) 1.004(21)	0.3417(4) 0.1273(2) 0.0551(7) 1.062(21)	0.3415(4) 0.1270(2) 0.0538(7) 1.140(22)	0.3420(4) 0.1269(2) 0.0540(7) 1.132(23)	0.3420(4) 0.1276(2) 0.0553(6) .0951(20)	0.3433(4) 0.1281(2) 0.0573(6) 0.761(18)	0.3447(3) 0.1289(2) 0.0589(6) 0.568(16)
O(6) x y z Uiso	0.3542(3) 0.1202(2) 0.5695(6) 0.475(16)	0.3540(3) 0.1209(2) 0.5686(6) 0.479(16)	0.3543(3) 0.1211(2) 0.5670(6) 0.537(16)	0.3553(3) 0.1212(2) 0.5668(6) 0.592(16)	0.3558(3) 0.1212(2) 0.5666(6) 0.650(17)	0.3561(3) 0.1210(2) 0.5671(6) 0.666(17)	0.3566(3) 0.1213(2) 0.5666(6) 0.816(19)	0.3575(3) 0.1212(2) 0.5664(6) 0.766(18)	0.3577(3) 0.1212(2) 0.5661(6) 0.823(19)	0.3578(3) 0.1211(2) 0.5660(6) 0.883(19)	0.3581(4) 0.1214(2) 0.5653(6) 1.004(21)	0.3587(4) 0.1212(2) 0.5650(6) 1.062(21)	0.3586(4) 0.1213(2) 0.5645(7) 1.140(22)	0.3586(4) 0.1211(2) 0.5648(7) 1.132(23)	0.3584(4) 0.1213(2) 0.5646(6) 0.951(20)	0.3571(3) 0.1212(2) 0.5658(6) 0.761(18)	0.3557(3) 0.1213(2) 0.5662(6) 0.568(16)
O(7) <i>x</i>	0.3403(4)	0.3404(4)	0.3401(4)	0.3396(4)	0.3394(5)	0.3392(4)	0.3381(5)	0.3384(5)	0.3378(5)	0.3376(5)	0.3359(5)	0.3358(5)	0.3352(5)	0.3356(5)	0.3365(5)	0.3388(5)	0.3400(4)

TABLE 1. (Contd.)

Atom position	n 50	100	150	200	250	300	Tempera 350	ture (°C) 400	450	500	550	600	650	700	500	350	200
z Uiso	0.2781(8) 0.475(16)	0.2767(8) 0.479(16)	0.2567(8) 0.537(16)	0.2757(8) 0.592(16)	0.2758(8) 0.650(17)	0.2764(8) 0.666(17)	0.2766(8) 0.816(19)	0.2763(9) 0.766(18)	0.2768(8) 0.823(19)	0.2773(9) 0.883(19)	0.2772(9) 1.004(21)	0.2775(9) 1.062(21)	0.2782(10) 1.140(22)	0.2785(10) 1.132(23)	0.2766(9) 0.951(20)	0.2759(8) 0.761(18)	0.2759(8) 0.568(16)
Si(1) x y z Uiso	0.2845(5) 0.0849(2) 0.2759(8) 0.207(31)	0.2852(4) 0.0847(2) 0.2767(8) 0.212(30)	0.2852(5) 0.0848(2) 0.2761(8) 0.275(31)	0.2855(5) 0.0849(2) 0.2768(8) 0.301(31)	0.2858(5) 0.0851(2) 0.2768(9) 0.332(31)	0.2866(5) 0.0852(2) 0.2774(8) 0.339(31)	0.2873(5) 0.0852(2) 0.2767(9) 0.469(33)	0.2876(5) 0.0855(2) 0.2776(9) 0.384(32)	0.2874(5) 0.0855(2) 0.2779(9) 0.420(32)	0.2881(5) 0.0856(2) 0.2778(9) 0.437(33)	0.2877(5) 0.0857(3) 0.2776(9) 0.55(4)	0.2873(5) 0.0859(3) 0.2779(10) 0.61(4)	0.2885(6) 0.0859(3) 0.2779(10) 0.61(4)	0.2886(6) 0.0860(3) 0.2784(10) 0.60(4)	0.2873(5) 0.0859(3) 0.2773(9) 0.52(4)	0.2867(5) 0.0855(2) 0.2768(9) 0.414(32)	0.2857(5) 0.0852(2) 0.2770(8) 0.291(30)
Si(2) x y z Uiso	0.2930(5) 0.1685(2) 0.7823(8) 0.207(31)	0.2922(5) 0.1689(2) 0.7816(8) 0.212(30)	0.2922(5) 0.1691(2) 0.7816(8) 0.275(31)	0.2920(5) 0.1689(23) 0.7813(8) 0.301(31)	0.2916(5) 0.1688(2) 0.7810(8) 0.332(31)	0.2903(5) 0.1688(2) 0.7805(8) 0.339(31)	0.2899(5) 0.1687(2) 0.7801(9) 0.469(33)	0.2892(5) 0.1690(2) 0.7799(8) 0.384(32)	0.2891(5) 0.1687(2) 0.7797(9) 0.420(32)	0.2883(5) .01689(2) 0.7796(9) 0.437(33)	0.2893(5) 0.1683(3) 0.7798(9) 0.55(4)	0.2895(5) 0.1682(3) 0.7801(9) 0.61(4)	0.2884(6) 0.1680(3) 0.7796(10) 0.61(4)	0.2873(6) 0.1681(3) 0.7792(10) 0.60(4)	0.2899(5) 0.1684(3) 0.7795(9) 0.52(4)	0.2901(5) 0.1687(2) 0.7796(8) 0.414(32)	0.2914(5) 0.1688(2) 0.7802(8) 0.291(30)
M(1) y Uiso	0.0870(3) 0.088(32)	0.0871(3) 0.165(32)	0.0873(3) 0.220(33)	0.0874(3) 0.280(34)	0.0874(3) 0.36(4)	0.0873(3) 0.44(4)	0.0875(3) 0.59(4)	0.0875(3) 0.62(4)	0.0875(3) 0.70(4)	0.0875(3) 0.80(4)	0.0877(3) 0.92(4)	0.0877(3) 1.07(5)	0.0877(3) 1.23(5)	0.0874(3) 1.29(5)	0.08751(3) 0.95(4)	0.08735(3) 0.64(4)	0.0872(3) 0.342(34)
M(2) y Uiso Mn Frao Mg Frao	0.1755(3) 0.088(32) c. 0.067(6) c. 0.933(6)	0.1760(3) 0.165(32) 0.065(5) 0.935(5)	0.1761(3) 0.220(33) 0.065(6) 0.935(6)	0.1763(3) 0.280(34) 0.066(6) 0.934(6)	0.1764(3) 0.36(4) 0.063(6) 0.937(6)	0.1766(3) 0.44(4) 0.063(6) 0.937(6)	0.1763(3) 0.59(4) 0.067(6) 0.933(6)	0.1766(3) 0.62(4) 0.062(6) 0.938(6)	0.1767(3) 0.70(4) 0.063(6) 0.937(6)	0.1766(3) 0.80(4) 0.060(6) 0.940(6)	0.1765(3) 0.92(4) 0.057(6) 0.943(6)	0.1767(3) 1.07(5) 0.060(7) 0.940(7)	0.1765(3) 1.23(5) 0.068(7) 0.932(7)	0.1767(4) 1.29(5) 0.078(7) 0.922(7)	0.1766(3) 0.95(4) 0.076(6) 0.924(6)	0.1767(3) 0.64(4) 0.082(6) 0.918(6)	0.1767(3) 0.342(34) 0.083(6) 0.917(6)
M(3) Uiso	0.088(32)	0.165(32)	0.220(33)	0.280(34)	0.36(4)	0.44(4)	0.59(4)	0.62(4)	0.70(4)	0.80(4)	0.92(4)	1.07(5)	1.23(5)	1.29(5)	0.95(4)	0.64(4)	0.342(34)
M(4) y Uiso Mn Frac Mg Frac	0.2369(22 0.088(32) c. 0.503(6) c. 0.227(6)	0.2375(22 0.165(32) 0.505(5) 0.225(5)) 0.2362(22) 0.220(33) 0.505(6) 0.225(6)) 0.2356(22) 0.280(34) 0.504(6) 0.226(6)	0.2375(25) 0.36(4) 0.508(6) 0.222(6)	0.2423(24) 0.44(4) 0.507(6) 0.223(6)) 0.2396(24) 0.59(4) 0.504(6) 0.226(6)	0.2453(26) 0.62(4) 0.508(6) 0.222(6)	0.2459(26 0.70(4) 0.507(6) 0.223(6)) 0.2479(29) 0.80(4) 0.510(6) 0.220(6)	0.2438(32) 0.92(4) 0.513(6) 0.217(6)	0.2469(31) 1.07(5) 0.510(7) 0.220(7)	0.2496(28) 1.23(5) 0.502(7) 0.228(7)	0.2542(24) 1.29(5) 0.493(7) 0.237(7)	0.2483(24) 0.95(4) 0.494(6) 0.236(6)	0.2484(20) 0.64(4) 0.489(6) 0.241(6)	0.2441(18) 0.342(34) 0.487(6) 0.243(6)
a (Å) b (Å) c (Å) $\beta (°) = 1$	9.5539(2) 18.0293(3) 5.2999(1) 02.614(2)	9.5566(2) 18.0373(3) 5.3034(1) 102.592(2)	9.5611(2) 18.0458(3) 5.3056(1) 102.569(2)	9.5661(2) 18.0531(3) 5.3069(1) 102.549(2)	9.5714(2) 18.0610(3) 5.3082(1) 102.529(2)	9.5761(2) 18.0678(3) 5.3089(1) 102.511(2)	9.5824(2) 18.0767(3) 5.3104(1) 102.493(2)	9.5876(2) 18.0841(3) 5.3113(1) 102.475(2)	9.5933(2) 18.0925(3) 5.3124(1) 102.457(2)	9.5994(2) 18.1008(3) 5.3135(1) 102.440(2)	9.6061(2) 18.1101(3) 5.3151(1) 102.422(2)	9.6120(2) 18.1206(4) 5.3166(1) 102.397(2)	9.6182(2) 18.1323(4) 5.3185(1) 102.363(2)	9.6236(2) 18.1425(4) 5.3198(1) 102.335(2)	9.6004(2) 18.1087(3) 5.3152(1) 102.404(2)	9.5823(2) 18.0835(3) 5.3113(1) 102.454(2)	9.5663(2) 18.0607(3) 5.3080(1) 102.511(2)
R_{wp}	0.0258	0.0214	0.0207	0.0194	0.0194	0.0193	0.0182	0.0176	0.0171	0.0168	0.0165	0.0162	0.016	0.0161	0.0172	0.0182	0.021

for profiles obtained for the detector banks at 90° and 145°20. Here, R_{wp} , the *R*-weighted profile is used to assess the quality of the refinement since the numerator is the residual of the fit. It is defined as:

$$R_{wp} = \left[\frac{\sum_{i} w_{i}(I_{i} - I_{i,calc})^{2}}{\sum_{i} w_{i}I_{i}^{2}}\right]^{1/2}$$

where I_i and $I_{i,calc}$ are the observed and calculated intensities at the *i*th point in the pattern respectively and the weighting, w_i is related to the estimated standard deviation in the intensity of the *i*th point by $w_i = 1/\sigma_i^2$.

An infrared powder absorption spectrum of the sample was recorded at room temperature in the wavenumber region $500-4500 \text{ cm}^{-1}$ (Boffa Ballaran, unpublished data) using a Bruker 67V FT-IR spectrometer. The sample was prepared as a pressed pellet, diluted to 0.29 wt.% of the CsI pellet.

Results

Table 1 displays the refined structural parameters of sample R14473 as a function of temperature. Also shown are the R factors for each refinement.



The exchange reaction of Mn^{2+} and Mg^{2+} between the M(4) and M(2) sites, has the equilibrium constant:

$$K_{\rm D} = rac{{
m Mn}^{{
m M}(4)}(1-{
m Mn}^{{
m M}(2)})}{{
m Mn}^{{
m M}(2)}(1-{
m Mn}^{{
m M}(4)})}$$

Therefore, a value of $K_{\rm D} = 1$ would represent complete disorder between M(4) and M(2), $K_{\rm D} = 0$



FIG. 2. The time-of-flight neutron powder diffraction pattern of cummingtonite R14473 at 650°C. The vertical markers show the calculated positions of reflections and the Rietveld fit is shown by the solid line. Also shown is the residual between calculated pattern and the pattern determined by experiment.

corresponds to complete anti-order and $K_{\rm D} = \infty$ would imply complete order.

There is a suggestion of an initial increase in the occupancy of the M(4) site by Mn^{2+} (see Fig. 3) until a temperature of ~550°C, at which point a sharp decline in X_{Mn}^{M4} commences and K_D decreases from a maximum of 17.4 to a minimum of 11.5 on heating, corresponding to disordering. Another interesting feature of Fig. 3 is the retention of the high-temperature disorder on cooling. Our results show that exchange is predominantly between M(4) and M(2). Alternative refinements, constraining all Mn to the M(4) site at lower temperatures, produced negative isotropic temperature factors. Once unconstrained, these models immediately converged upon site occupancies identical to those of the M(4)-M(2) model with the same R_{wp} s and temperature factors. Additional models that constrained all Mn to just the M(4) and M(1)sites were also found to be erroneous and unstable.

The distribution coefficient, K_D , is related to the Gibbs free energy for the exchange of cations, as follows:

$\Delta G = -RT \ln K_D$

where ΔG is the Gibbs free energy of disorder and *T* is the absolute temperature. The data from the three highest temperatures were used to determine this exchange energy as these represent equilibrium conditions, and gave an exchange energy of 24.6 ± 1.5 kJ mol⁻¹.

The cell parameters of our sample (Fig. 4) show linear relationships with increasing temperature, but in two or three segments. The a and blattice parameters both show two stages or rates of expansion on heating, the *a* parameter strain behaviour showing a 'kink' at roughly 150°C and the *b* parameter expansion rate increases at 500-550°C. The strain behaviour of the cparameter on heating may be divided into three linear portions, the nodes of which coincide with the temperatures at which the change in rate of expansion occurs in the a and b parameters. At the higher of the two temperatures, marked changes in the β angle and the volume of the unit cell (Fig. 4) also occur. It is also noticeable that on cooling, a displacement of all parameters except a is maintained

Figure 5 shows the positional behaviour of the hydrogen atom within the structure upon heating and cooling. The decrease in z and increase in x above 100°C are the result of the $P2_1/m$ to C2/m phase transition. The behaviour of the hydrogen atom as a direct result of the onset of disordering at ~550°C cannot be defined within the errors illustrated. The *in situ* results do show that during cooling of the sample, the hydrogen atom returns to the positions it originally occupied (within error) at the respective temperatures during heating.

The infrared spectrum of the amphibole (Fig. 6) has a strong sharp peak centred at 3670 cm^{-1} with a small shoulder at 3674 cm^{-1} . The main peak corresponds to an O(3) cation triplet MgMgMg



FIG. 3. Mn^{2+} occupancy of the M(4) site. Note the 'frozen in' disordered state during cooling.



FIG. 4. Cell parameters and volume as a function of temperature.

(Burns and Strens, 1966), consistent with complete occupancy of M(1) and M(3) sites by Mg. Subtle splitting of main absorption bands has been observed in amphiboles with mixed M(4) site occupancy. In a slightly synthetic tremolite with minor Mg at M(4), Hawthorne *et al.* (1996) observed a small shoulder at ~3670 cm⁻¹ due to MgMgMg/^{M(4)}Mg in addition to the strong main peak at 3674 cm⁻¹ due to MgMgMg/^{M(4)}Ca. Thus, for the Talcville cummingtonite (with Mn as the main M(4) cation), it seems reasonable to ascribe the main absorption at 3670 cm⁻¹ to

MgMgMg/^{M(4)}Mn (and ^{M(4)}Mg ?) and the peak at 3674 cm⁻¹ to MgMgMg/^{M(4)}Ca, in line with the assignments of Burns and Strens (1966) and Hawthorne *et al.* (1996). Mn substitution for Mg at M(1) and/or M(3) would, by analogy with Fe²⁺ for Mg (Burns and Strens, 1966), be expected to lead to peaks at frequencies 15-20 cm⁻¹ lower than those due to MgMgMg, and so we can be confident that the 3674 cm⁻¹ peak is not due to Mn at M(1) and/or M(3).

Table 2 lists some octahedral bond lengths in the structure at 750, 250 and 50° C. Also listed are





FIG. 5. The positional behaviour of the hydrogen atoms within the unit cell as a function of temperature. The open circles represent the position at the temperatures labelled during cooling.

the same bond lengths as reported by Sueno *et al.* (1972), for the same structure. Our results for bonds to M(4) are subject to a relatively high error, due to the low total scattering length of the M(4) site, where positive scattering (principally from Ca which has b = +4.70 fm, but also from Mg and Na) is reduced by the large negative scattering contribution from Mn (b = -3.73 fm). This means that the positional error on M(4) is high. Papike *et al.* (1969) noted that in cummingtonites, when the M(4) site is occupied



FIG. 6. Infra-red spectra showing the region containing the hydroxl stretching peak.

by Fe and Mn, the O(5) oxygens are lost outside the M(4) coordination sphere, the M(4) cations move in the b direction towards the octahedral strip. Our bond lengths show that this effect is even more exagerrated than previously thought and a covalency between M(4) - O(2) is confirmed by bond lengths considerably shorter than the sum of the ionic radii of Mn^{2+} and O^{2-} . This type of covalent bonding has already been reported on the basis of short M(4)-O(4) bonds in Mg-Mn amphiboles (Ghose and Yang, 1989). The M(4)-O(4) bonds given by our refinements also show a lesser degree of covalency. In the most disordered state we observed that the average M(4) cation position has moved parallel to [010], away from the octahedral strip, decreasing the degree of M(4)-O(2) covalent bonding.

Discussion

The data presented show a definite preference of Mn^{2+} for the M(4) site with some disorder into the smaller M(2) site occurring at high temperature. It has been recognized previously (Ghose and Yang, 1989; Hawthorne and Grundy, 1977) that, in the absence of Fe²⁺, the preference of Mn²⁺ for the M(2) site is greatly increased. This is confirmed in our results by the site preference sequence M(4) \gg M(2) \gg M(1,3), compared to that reported by Ghose and Yang

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Bond		Sueno <i>et al.</i> , 1972		
	750°C	250°C	50°C	270°C
M1-01	2.073 (5)	2.064 (4)	2.060 (4)	2.063 (4)
M1-O2	2.130 (6)	2.121 (5)	2.118 (5)	2.112 (5)
M1-O3	2.077 (6)	2.069 (5)	2.062 (5)	2.087 (4)
<m1-o></m1-o>	2.093	2.085	2.080	2.087
M2-O1	2.151 (7)	2.136 (5)	2.119 (5)	2.141 (5)
M2-O2	2.083 (4)	2.083 (4)	2.082 (4)	2.082 (4)
M2-O4	2.039 (6)	2.010 (5)	2.023 (5)	2.031 (5)
<m2-o></m2-o>	2.091	2.076	2.075	2.085
M3-01	2.134 (4)	2.126 (3)	2.117 (3)	2.089 (4)
M3-O3	1.986 (6)	1.984 (5)	1.984 (5)	2.059 (6)
<m3-o></m3-o>	2.085	2.079	2.073	2.079
M4-O2	2.072 (32)	1.867 (28)	1.856 (25)	2.215 (4)
M4-O4	2.102 (5)	2.119 (7)	2.108 (6)	2.109 (5)
M4-O6	2.70 (4)	2.96 (4)	2.986 (33)	2.584 (5)
< M1 - M1	3.169 (13)	3.156 (10)	3.139 (10)	3.147 (6)
M1-M2	3.115 (5)	3.103 (4)	3.093 (4)	3.109 (2)
M1-M3	3.096 (3)	3.087 (3)	3.079 (2)	3.085 (1)
M1-M4	3.03 (4)	2.71 (4)	2.70 (4)	3.202 (4)
M2-M3	3.206 (6)	3.186 (5)	3.164 (5)	3.195 (3)
M2-M4	3.008 (22)	2.873 (17)	2.873 (15)	3.089 (2)

TABLE 2. Bond lengths as given by our refinements and those of Sueno *et al.* (1972). All bond lengths are in angstroms and figures represented in parentheses represent the error in the last digit of the bond length given.

(1989) of M(4) \gg M(1)>M(2)>M(3) in a Mn-Mg cummingtonite with 0.15 Fe per formula unit. It seems likely that the absence of Fe in the Talcville sample allows the occupation of M(2) by Mn²⁺, as indicated by our neutron refinements and room temperature infrared spectrum.

During heating, an initial increase in X_{Mn}^{M4} occurs as the amphibole adjusts towards the equilibrium Mn partitioning for these temperatures, until ~550°C, whereupon disordering into the smaller M(2) site becomes kinetically possible, showing a site preference energy of 24.6 ± 1.5 kJ mol⁻¹. Analogous 'relaxation' behaviour has been observed in olivines and spinels (Redfern et al., 1996; Henderson et al., 1996). This is a greater exchange energy than 8.95 kJ mol⁻¹, reported by Ghose and Yang (1989) for Fe-Mg exchange in an amphibole with $X^{Mn}/X^{Fe} = 0.378$ and than 18.33 kJ mol⁻¹ found in Mn-Mg amphibole with $\chi^{Mn}/\chi^{Fe} =$ 0.350. Hirschmann et al. (1994) reported an ordering energy of Fe-Mg between M(1) and $M(4),(-RT\ln K_{1,4})$ of 18.2 ± 0.3 kJ mol⁻¹, in natural ferromagnesian clinoamphiboles with Fe/(Fe+Mg) as great as 0.38. They also reported a decrease in this ordering energy in very magnesian compositions but found the reaction to be otherwise independent of temperature over the range 600-750°C. The variation in quoted exchange energies may be due to differences in composition or oxygen fugacity at the temperatures of study. We note that our *in situ* experiments were conducted under very low oxygen fugacity, at the vanadium-vanadium oxide buffer. It is apparent that the disordered structural arrangements are retained during cooling of the sample.

The distortion in lattice parameters during heating above 100°C is interpreted as resulting from the P_{21}/m to C_{2}/m phase transition. The strain behaviour in the lattice parameters shows that the spontaneous strain resulting from the P_{21}/m $m \rightarrow C_{2}/m$ transition is predominantly a shear with $+\varepsilon_{1} \approx -\varepsilon_{3}$. Taking the data above 150°C as the paraphase (the high symmetry phase), we have calculated spontaneous strains of $\varepsilon_{1} = 0.0734\%$ and $\varepsilon_{3} = -0.0708\%$ at room temperature, which decrease in magnitude on heating to T_{c} . The scalar



FIG. 7. Scalar strain as a function of temperature, falling to zero at the transition temperature of 107° C.

strain may be calculated as the geometric average of ε_1 and ε_3 and falls to zero at a T_c of 107°C. This $T_{\rm c}$ is higher than for the Fe-free cummingtonite also from the Talc district, New York, given by Prewitt *et al.* (1970), who reported a T_c of 45°C, but is comparable to the figure of Sueno et al. (1972) who give a T_c of 100°C (Fig. 7). In their samples, all but the c parameter, were greater than the cell parameters refined here. From our limited data, the spontaneous strain appears to be linearly dependent on temperature below $T_{\rm c}$. Since, for this transition, strain must behave as the square of the order parameter (the transition is a zoneboundary instability) this indicates that the $P2_1/m$ \rightarrow C2/m transition is second order, or close to second-order in thermodynamic character (Salje, 1990). Additional strains, $+\varepsilon_2$, $+\varepsilon_3$ and $-\varepsilon_5$, all resulting in a volume strain, are associated with the M-site disordering at $T > 550^{\circ}$ C. The fact that both M-site ordering and the P to C transition induce measurable spontaneous strains provides a mechanism for interaction between each. We anticipate that changes in M-site order will induce changes in the characteristics of the $P2_1/m \rightarrow$ C2/m transition through the common strain interaction.

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