# SINNERITE, $\mathrm{Cu}_{6} \mathrm{As}_{4} \mathrm{~S}_{9}$, FROM THE LENGENBACH QUARRY, BINN VALLEY, SWITZERLAND: DESCRIPTION AND RE-INVESTIGATION OF THE CRYSTAL STRUCTURE 

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#### Abstract

We have characterized the crystal structure of sinnerite, $\mathrm{Cu}_{6} \mathrm{As}_{4} \mathrm{~S}_{9}$, a rare sulfosalt mineral from the ores of the Lengenbach quarry, Binn Valley, Canton Valais, Switzerland, by single-crystal X-ray diffraction and chemical analysis. We found sinnerite to be structurally identical to synthetic $\mathrm{Cu}_{6} \mathrm{As}_{4} \mathrm{~S}_{9}$. It is triclinic, space group $P 1$, with cell parameters: $a$ 9.103(2), $b 9.860(3), c$ $9.111(2) \AA, \alpha 90.27(2), \beta 109.53(2), \gamma 107.58(2)^{\circ}, V 729.6(4) \AA^{3}$, and $Z=2$. Semi-quantitative SEM-EDS analyses confirmed the $\mathrm{Cu}_{6} \mathrm{As}_{4} \mathrm{~S}_{9}$ stoichiometry. The crystal structure of an untwinned crystal has been refined to $R_{1}=5.45 \%$. It consists of a sphalerite substructure with $2 / 5$ of the tetrahedra replaced by $\mathrm{AsS}_{3}$ pyramids; four pyramids form $\mathrm{As}_{4} \mathrm{~S}_{12}$ clusters around the vacant anion positions of the sphalerite archetype. These pyramids are linked into twisted and branched chain-like structures with compositions $\mathrm{As}_{3} \mathrm{~S}_{7}$ and $\mathrm{As}_{5} \mathrm{~S}_{11}$. The chains are linked by $\mathrm{CuS}_{4}$ tetrahedra. Packing of these chains results in the OD (order-disorder) character of the sinnerite structure.


Keywords: sinnerite, crystal structure, sulfosalts, Lengenbach, Switzerland

## Introduction

The Lengenbach quarry, located in the Binn Valley, Canton Valais, Switzerland, is one of the premium localities for sulfosalt minerals, including Pb -sulfosalts (e.g., sartorite, baumhauerite, rathite, liveingite, dufrénoysite, jordanite), $\mathrm{Pb}-\mathrm{Tl}$-sulfosalts (e.g., hutchinsonite, hatchite, wallisite, dalnegroite), $\mathrm{Pb}-\mathrm{Ag}-\mathrm{Cu}$-sulfosalts (e.g., marrite, seligmannite, lengenbachite), and Tl-sulfosalts (e.g., lorandite, imhofite, raberite, philrothite). Copper- (e.g., binnite, sinnerite, nowackiite) and Ag -sulfosalts (e.g., stephanite, pyrargyrite, proustite,
xanthoconite) are more rare but present. Among these minerals, sinnerite was identified as a new mineral species by Marumo \& Nowacki (1964), who studied ore minerals occurring on the Lengenbach dolomite. Preliminary X-ray investigations of the mineral pointed out a complicated superlattice structure pattern with a small subcell. The reported dimensions for the subcell were: $a 3.72(1), b 3.70(1), c 5.24(1) \AA$, and $\alpha=\beta=\gamma$ $=90^{\circ}$. Later, Makovicky \& $\operatorname{Skinner}(1972)$ were able to solve the composition and symmetry of sinnerite using the material synthesized by Maske \& Skinner (1971) during their study of the $\mathrm{Cu}-\mathrm{As}-\mathrm{S}$ system. Despite the

[^0]presence of an extremely pronounced sphalerite-like substructure with $a \sim 5.25 \AA$, Makovicky \& Skinner (1972) demonstrated the triclinic nature of sinnerite and concluded that both natural and synthetic crystals are complexly twinned (by reticular pseudo-merohedry). Later, the same authors (Makovicky \& Skinner 1975) were able to propose a structural model for the synthetic analogue of sinnerite and showed that the twinning in such a compound produces twin aggregates containing 24 individuals and simulates a $\overline{4} 3 m$ cubic symmetry. Due to the pervasive twinning and to the very low number of collectable X-ray reflections (607 reflections, $R \mathrm{w}=17.2 \%$ ) from a six-fold twin, the atom coordinates and the bond distances given by Makovicky \& Skinner (1975) showed large errors. Moreover, a crystal-structure refinement of the natural material was not done at that time.

To help resolve the details of the structure of sinnerite, here we present new structural data from a gemquality, untwinned sinnerite crystal recovered from a specimen originating from the Lengenbach quarry, Binn Valley, Switzerland.

## Occurrence, Composition, and X-Ray Crystallography

Sinnerite was found in a rock-sample from the realgar-rich zone (the so-called zone 1 ; Graeser et al. 2008) collected in 1998. It occurs as very rare elongated crystals grown on realgar and is closely associated with coloradoite, described for the first time for the Lengenbach quarry (Fig. 1). Sinnerite exhibits a subhedral to anhedral grain morphology, and does not show any inclusions of, or intergrowths with, other minerals. The maximum grain size of sinnerite is about $150 \mu \mathrm{~m}$.

A chemical analysis using energy dispersive spectrometry was performed using a SEM JEOL-5610 LV. The crystal fragment was found to be homogeneous within analytical error and the $\mathrm{Cu}_{6} \mathrm{As}_{4} \mathrm{~S}_{9}$ stoichiometry was confirmed (Cu 39.3, As 30.9, and S 29.8 wt. \% of elements).

A crystal fragment $(100 \times 115 \times 130 \mu \mathrm{~m})$ was selected for the X-ray single-crystal diffraction study that was done with a STOE-STADI IV CCD singlecrystal diffractometer (Table 1). No systematic absences were observed in the collected data set, thus leading to the choice of the space groups $P 1$ and $P \overline{1}$. The statistical tests on the distribution of $|E|$ values $\left(\left|E^{2}-1\right|=0.745\right)$ did not indicate the presence of an inversion center, thus suggesting the choice of the space group $P 1$. Detectable traces of twinning were absent. The positions of most of the atoms ( $\mathrm{Cu}, \mathrm{As}$, and some S atoms) were determined by means of direct methods (Sheldrick 2008). A least-squares refinement on $F^{2}$ using these heavy-atom positions produced an $R$ factor of 0.135 . Three-dimensional difference Fourier synthesis yielded the position of the remaining sulfur atoms. The SHELXL program (Sheldrick 2008) was used for the refinement of the
structure. The occupancy of all the sites was left free to vary ( Cu versus vacancy; As versus vacancy; S versus vacancy) and all refined to full occupancy. Neutral scattering curves for $\mathrm{Cu}, \mathrm{As}$, and S were taken from the International Tables for X-ray Crystallography (Ibers \& Hamilton 1974). At the final stage, with isotropic atomic displacement parameters for all atoms and no constraints, the residual value settled at $R=0.0545$ for 1028 observed reflections [ $2 \sigma(I)$ level] and 153 parameters and at $R=0.0567$ for all 3456 independent reflections. Experimental details and $R$ indices are given in Table 1. Fractional atomic coordinates and isotropic displacement parameters are reported in Table 2. Bond distances are given in Table 3. A list of the observed and calculated structure factors is available from the Depository of Unpublished Data, MAC website [document Sinnerite CM51_851].

## Results and Discussion

## Crystal structure - a dual description

The crystal structure of sinnerite is a close homeotype of the zincblende (sphalerite) structure, as revealed by the strong reflections of a pseudocubic subcell (Makovicky \& Skinner 1972). The strongest contributions to the true-cell reflections result from the presence


FIG. 1. Sinnerite (SIN) on realgar associated with coloradoite (COL).
of sulfur vacancies in the centers of two crystallographically independent $\mathrm{As}_{4} \mathrm{~S}_{12}$ clusters and from the deviation of As sites from the regular tetrahedral arrangement.

The structure of sinnerite contains eight different $\mathrm{AsS}_{3}$ coordination pyramids and 12 distinct $\mathrm{CuS}_{4}$ coordination tetrahedra (Fig. 2). There are 18 distinct S positions in these polyhedra. Two groups of four $\mathrm{AsS}_{3}$ pyramids form two crystallographically distinct $\mathrm{As}_{4} \mathrm{~S}_{12}$ clusters, with As barycentres at $(0.18610,0.04947$, 0.18190 ) (Fig. 3) and ( $0.53835,0.64395,0.63825$ ) in terms of sinnerite lattice, and with individual $\mathrm{AsS}_{3}$ pyramids in clusters separated from one another. The majority of pyramids have average As-S bond lengths in the range 2.26-2.31 $\AA$, but As6 has an average As-S bond length equal to $2.423 \AA$, whereas As3 shows 2.217 $\AA$, followed by As 5 with 2.227 A. These deviations are accompanied by deviations of calculated bond-valence

## TABLE 1. CRYSTALLOGRAPHIC DATA AND REFINEMENT

 PARAMETERS FOR SINNERITE| Crystal data |  |
| :---: | :---: |
| Ideal formula | $\mathrm{Cu}_{6} \mathrm{As}_{4} \mathrm{~S}_{9}$ |
| Crystal system | triclinic |
| Space group | P1 |
| Unit-cell parameters ( $\AA$, ${ }^{\circ}$ ) | $\begin{gathered} 9.103(2) 9.860(3) 9.111(2) \\ 90.27(2) 109.53(2) \\ 107.58(2) \end{gathered}$ |
| Unit-cell volume ( $\AA^{3}$ ) | 729.6(4) |
| Z | 2 |
| Crystal size (mm) | $0.100 \times 0.115 \times 0.130$ |
| Data collection |  |
| Diffractometer | STOE-STADI IV CCD |
| Temperature (K) | 298(3) |
| Radiation, wavelength ( $\mathcal{A}$ ) | MoKa, 0.71073 |
| $2 \theta_{\text {max }}$ for data collection( ${ }^{\circ}$ ) | 58.02 |
| Crystal-detector dist. (mm) | 60 |
| $h, k, I$ ranges | -9 to 12, -12 to 12, -12 to 9 |
| Axis, frames, width $\left({ }^{\circ}\right)$, time per frame (s) | $\omega, 435,1.00,40$ |
| Total reflections collected | 7725 |
| Unique reflections ( $R_{\text {int }}$ ) | 3845 (0.081) |
| Unique reflections $1>2 \sigma(1)$ | 1028 |
| Data completeness to $\theta_{\text {max }}(\%)$ | 99.7 |
| Absorption correction method | X -RED and X -SHAPE |

## Structure refinement

Refinement method
Data/restraints/parameters
$R_{1}[I>2 \sigma(I)], w R_{2}[I>2 \sigma(I)]$ $R_{1}$ all, $w R_{2}$ all
Goodness-of-fit on $F^{2}$
Full-matrix least-squares on $F^{2}$
1028/3/154
$0.0545,0.0555$
0.0567, 0.0612
1.042

Largest diff. peak and hole ( $\mathrm{e}^{-} / \AA^{3}$ )
$0.98,-0.78$

[^1]values from the bulk of As atoms. The sulfurs S7 and S11, bonded to As6, have elevated displacement parameters (Table 2), as does As7, whereas S2 and S15, attached to As5, and S3, attached to As6, display higher bond-valence values. Placement of these atoms in the structure and possible reasons for these deviations from the average values will be discussed below.

The average of bond-valence values (calculated from the curves of Brese \& O'Keeffe 1991) for As is 2.945 $b v u$, but those for $\mathrm{Cu}(1.372 \mathrm{bvu})$ and $\mathrm{S}(2.223 \mathrm{bvu})$ are higher than expected (Table 4). Cu 1 and Cu 9 have elevated displacement parameters; these can tentatively be explained by their bonds to S atoms bonded to the aforementioned As atoms with elevated displacement parameters and/or deviating bond characteristics.

An alternative description of the crystal structure of sinnerite, in terms of chains of short As-S bonds (Makovicky \& Skinner 1975), discerns two types of chains: twisted branched chains with compositions $\mathrm{As}_{3} \mathrm{~S}_{7}$ and $\mathrm{As}_{5} \mathrm{~S}_{11}$ (Fig. 4). The longer chain is an extended version of the shorter one. The chains are 'immersed' in an environment of $\mathrm{CuS}_{4}$ tetrahedra of the zincblende-like structure. The first type of $\mathrm{As}_{4} \mathrm{~S}_{12}$ cluster combines As2 and As3 from the $\mathrm{As}_{3} \mathrm{~S}_{7}$ chain and As1 and As4 from the $\mathrm{As}_{5} \mathrm{~S}_{11}$ chain. The As-As distances vary between 3.36 and $3.62 \AA$, the distances of As atoms to their barycenter are $2.07-2.23 \AA$, and $\mathrm{S}-\mathrm{S}$ distances in the periphery of the cluster are in the range of 3.37-3.89 $\AA$. The second type of $\mathrm{As}_{4} \mathrm{~S}_{12}$ cluster combines As8 from the $\mathrm{As}_{3} \mathrm{~S}_{7}$ chain with three arsenic atoms (As5, 6, and 7) from the $\mathrm{As}_{5} \mathrm{~S}_{11}$ chain. This cluster appears larger, with As-As distances from 3.48 to $3.71 \AA$ (the longest distance occurs between As8 and As6), As-to-barycenter distances from 2.14 to $2.26 \AA$, and S-S distances from 3.37 to $3.89 \AA$. Both $\mathrm{As}_{4} \mathrm{~S}_{12}$ clusters share $\mathrm{S}-\mathrm{S}$ edges with three adjacent clusters and are arranged in (101) planes of the sinnerite structure, being separated by As-free interspaces. The relationship between clusters (represented as cubooctahedra defined by peripheral S atoms) is illustrated in Figure 5, in which relevant fragments of As-S chains are also included.

## OD phenomena

The OD phenomena are best described by the arrangement of the twisted branched $\mathrm{As}_{3} \mathrm{~S}_{7}$ and $\mathrm{As}_{5} \mathrm{~S}_{11}$ chains, whereas the $\mathrm{CuS}_{4}$ tetrahedra enveloping them can be considered a 'passive' geometrical element. An alternative description of these phenomena, in terms of contact and attachment schemes for the two types of $\mathrm{As}_{4} \mathrm{~S}_{12}$ clusters present in the sinnerite structure, is given in Makovicky \& Skinner (1975).

The two types of branched chains are arranged as alternating $\mathrm{As}_{3} \mathrm{~S}_{7}$ and $\mathrm{As}_{5} \mathrm{~S}_{11}$ layers parallel to (010) of the sinnerite lattice (Fig. 6). Although not obvious in the views along [100] or [001], the $\mathrm{As}_{3} \mathrm{~S}_{7}$ chains are distributed in their layer in a highly symmetrical cm


Fig. 2. The crystal structure of sinnerite. As: black spheres, Cu : grey spheres, S : larger white spheres. Short $\mathrm{As}-\mathrm{S}$ bonds are rendered in white, and the tetrahedral $\mathrm{Cu}-\mathrm{S}$ bonds as thin lines. The thick black lines are As-As joins, too long for any bonding interactions, and are used here to delineate the inner volumes of tetrahedral $\mathrm{As}_{4}$ clusters.


Fig. 3. A cubo-octahedral $\mathrm{As}_{4} \mathrm{~S}_{12}$ cluster from the crystal structure of sinnerite composed of four $\mathrm{AsS}_{3}$ coordination pyramids. As: black spheres, S: large white spheres. A small white sphere: barycenter of the $\mathrm{As}_{4}$ cluster. Short As-S bonds: thick white sticks, schematic $\mathrm{S}-\mathrm{S}$ joins: thin white, As-As joins: grey, Barycentre-As joins: black lines.

Fig. 4. The $\mathrm{As}_{5} \mathrm{~S}_{11}$ (left, dark bonds) and $\mathrm{As}_{3} \mathrm{~S}_{7}$ (right, light bonds) chains from the crystal structure of sinnerite.


Fig. 5. The arrangement of $\mathrm{As}_{4} \mathrm{~S}_{12}$ clusters (opaque cubo-octahedra) in the crystal structure of sinnerite. The $(10 \overline{1})$ planes of the sinnerite structure, occupied by the clusters, and separated by As-free interspaces, are inclined in the figure, running from the upper left corner towards the right lower corner. Portions of As-S chains have the same coloring as in Figure 4.

TABLE 2. ATOM COORDINATES ( $\AA$ ) AND ISOTROPIC ATOMIC DISPLACEMENT PARAMETERS $\left(\AA^{2}\right)$ FOR SINNERITE

| atom | $x / a$ | $y / b$ | $z / c$ | $U_{\text {iso }}$ |
| :---: | :---: | :---: | :---: | :---: |
| As1 | $0.376(2)$ | $0.234(1)$ | $0.326(2)$ | $0.019(5)$ |
| As2 | $0.192(1)$ | $0.057(1)$ | $-0.036(1)$ | $0.010(4)$ |
| As3 | $0.959(1)$ | $0.062(1)$ | $0.188(1)$ | $0.013(3)$ |
| As4 | $0.225(2)$ | $0.845(1)$ | $0.275(2)$ | $0.021(4)$ |
| As5 | $0.534(2)$ | $0.641(1)$ | $0.394(2)$ | $0.027(5)$ |
| As6 | $0.291(1)$ | $0.626(1)$ | $0.638(1)$ | $0.010(3)$ |
| As7 | $0.589(2)$ | $0.462(2)$ | $0.734(2)$ | $0.037(5)$ |
| As8 | $0.737(2)$ | $0.849(2)$ | $0.790(2)$ | $0.024(4)$ |
| Cu1 | $0.777(2)$ | $0.644(2)$ | $0.130(2)$ | $0.036(6)$ |
| Cu2 | $0.340(2)$ | $0.450(2)$ | $-0.010(2)$ | $0.023(5)$ |
| Cu3 | $0.471(2)$ | $0.840(2)$ | $0.027(2)$ | $0.014(4)$ |
| Cu4 | $0.022(2)$ | $0.649(2)$ | $0.880(2)$ | $0.029(6)$ |
| Cu5 | $0.975(2)$ | $0.845(1)$ | $0.517(2)$ | $0.016(4)$ |
| Cu6 | $0.827(2)$ | $0.460(2)$ | $0.490(2)$ | $0.023(5)$ |
| Cu7 | $0.137(2)$ | $0.245(2)$ | $0.571(2)$ | $0.025(5)$ |
| Cu8 | $0.898(1)$ | $0.244(1)$ | $0.862(1)$ | $0.020(4)$ |
| Cu9 | $0.681(2)$ | $0.041(2)$ | $0.437(2)$ | $0.036(7)$ |
| Cu10 | $0.440(2)$ | $0.047(2)$ | $0.689(2)$ | $0.022(5)$ |
| Cu11 | $0.624(2)$ | $0.242(2)$ | $0.097(2)$ | $0.029(5)$ |
| Cu12 | $0.075(2)$ | $0.434(2)$ | $0.225(2)$ | $0.024(5)$ |
| S1 | $0.276(3)$ | $0.655(3)$ | $0.886(3)$ | $0.016(8)$ |
| S2 | $0.478(3)$ | $0.832(3)$ | $0.301(3)$ | $0.014(8)$ |
| S3 | $0.884(3)$ | $0.244(2)$ | $0.107(3)$ | $0.015(6)$ |
| S4 | $0.707(2)$ | $0.047(2)$ | $0.691(2)$ | $0.018(6)$ |
| S5 | $0.405(3)$ | $0.247(2)$ | $0.598(3)$ | $0.021(6)$ |
| S6 | $0.769(3)$ | $0.652(2)$ | $0.376(3)$ | $0.023(6)$ |
| S7 | $0.061(4)$ | $0.432(3)$ | $0.471(3)$ | $0.037(8)$ |
| S8 | $-0.002(3)$ | $0.865(3)$ | $0.791(3)$ | $0.014(8)$ |
| S9 | $0.621(3)$ | $0.226(2)$ | $0.332(3)$ | $0.017(7)$ |
| S10 | $0.836(3)$ | $0.451(2)$ | $0.741(3)$ | $0.027(7)$ |
| S11 | $0.232(4)$ | $0.845(3)$ | $0.519(4)$ | $0.035(8)$ |
| S12 | $0.134(3)$ | $0.241(3)$ | $0.814(3)$ | $0.016(8)$ |
| S13 | $0.932(3)$ | $0.043(2)$ | $0.412(3)$ | $0.014(7)$ |
| S14 | $0.733(3)$ | $0.868(2)$ | $0.035(3)$ | $0.019(6)$ |
| S15 | $0.326(3)$ | $0.441(3)$ | $0.242(4)$ | $0.018(8)$ |
| S16 | $0.017(3)$ | $0.638(3)$ | $0.132(4)$ | $0.021(7)$ |
| S17 | $0.428(3)$ | $0.051(3)$ | $0.948(3)$ | $0.018(7)$ |
| S18 | $0.585(3)$ | $0.434(3)$ | $-0.011(3)$ | $0.020(6)$ |
|  |  |  |  |  |

scheme, with deviations from this symmetry equal only to a fraction of one $\AA$. All $\mathrm{As}_{3} \mathrm{~S}_{7}$ chains point in the same direction along the short diagonal of the (010) face (Figs. 7 and 8). The $\mathrm{As}_{3} \mathrm{~S}_{7}$ layer is also polar in the [010] direction, with the 'front side' containing protruding S atoms and 'back side' with near-horizontal As-S bonds (Fig. 6). The $\mathrm{As}_{5} \mathrm{~S}_{11}$ chains form a polar layer of their own, pointing again along one direction of the short diagonal of the (010) face but their asymmetric attachment (Figs. 7 and 8) reduces the layer symmetry to $p 1$ or, in order to keep the interlayer match simple, to $c 1$, which has the same mesh axes as those selected for the $\mathrm{As}_{3} \mathrm{~S}_{7}$ layer. Again, the 'top' and the 'bottom' of the $\mathrm{As}_{5} \mathrm{~S}_{11}$ layer are different. The 'front side' of it, with protruding S atoms, contains an additional group
of two As polyhedra and the 'front' sides of the two layer types face one another, as also do the 'back' sides of them (Fig. 6).

When choosing the 'central' As atoms of the two groups (As8 for $\mathrm{As}_{3} \mathrm{~S}_{7}$ and As 4 for $\mathrm{As}_{5} \mathrm{~S}_{11}$ ) as arbitrary origins, in the 'front-to-front' contact of the layers the As4 atom lies above the As 3 atom of the $\mathrm{As}_{3} \mathrm{~S}_{7}$ group. Because of the extreme regularity of the $\mathrm{As}_{3} \mathrm{~S}_{7}$ layer, it could equally well lie above the opposing, As 2 , atom, but the $\mathrm{As}_{5} \mathrm{~S}_{11}$ group must then be an enantiomorph (chiral edition, a mirror image) of the group depicted in Figure 7. There is a sideways shift between the origins of the two layer types, defined by the As8 and As4 atoms, respectively, which is equal to $0.09 \boldsymbol{a}+0.34 \boldsymbol{c}$ in

Fig. 6. The two types of branched chains (indicated by light and dark As-S bonds, respectively) are arranged as alternating $\mathrm{As}_{3} \mathrm{~S}_{7}$ and $\mathrm{As}_{5} \mathrm{~S}_{11}$ layers parallel to (010) of the sinnerite lattice, at $y=0.5$ and $y=$ 0.0 , respectively. The S9-As1-S12-S3 line defines the 'front-to-front' contact of the two layer types; the S2-S11-S8-As8 line defines the 'back-to-back' contact of them (for implications see text and Figs. 7-8). Black dots with three black lines radiating from them towards As atoms (the fourth one is vertical) are barycentres of $\mathrm{As}_{4}$ clusters.


Fig. 7. A pair of $\mathrm{As}_{3} \mathrm{~S}_{7}$ and $\mathrm{As}_{5} \mathrm{~S}_{11}$ layers parallel to (010) of the sinnerite lattice in a front-tofront contact. A slightly inclined projection on (010). The $\mathrm{As}_{3} \mathrm{~S}_{7}$ chains have light-colored As-S bonds, the $\mathrm{As}_{5} \mathrm{~S}_{11}$ chains have dark colored bonds. Black dots are barycentres of $\mathrm{As}_{4}$ clusters, with barycentre-As joins illustrated as black lines. Copper coordination tetrahedra (not illustrated) fill the remaining spaces. The OD potential of this layer pair is outlined in the text.


Fig. 8. A pair of $\mathrm{As}_{3} \mathrm{~S}_{7}$ and $\mathrm{As}_{5} \mathrm{~S}_{11}$ layers parallel to (010) of the sinnerite lattice in a back-to-back contact. For conventions and comments see Figure 7.
terms of sinnerite axes (in the projection along [010]*, not along [010]).

With the same choice of layer origins, the 'back-toback' fit of the two layer types forms a pair where the As4 atom (and the $\mathrm{As}_{5} \mathrm{~S}_{11}$ group) is shifted from the coincidence with the As8 atom by $1 / 2$ of the short face diagonal of (010) in such a way that the terminal As7 atom of the 'branch' of the $\mathrm{As}_{5} \mathrm{~S}_{11}$ group overlaps the 'origin' (i.e., the As8 atom) of the $\mathrm{As}_{3} \mathrm{~S}_{7}$ group (Fig. 8). The origin of the $\mathrm{As}_{5} \mathrm{~S}_{11}$ layer, fixed on As4, is displaced from the origin of the $\mathrm{As}_{3} \mathrm{~S}_{7}$ layer (the As8 atom) by $0.49 \boldsymbol{a}+0.48 \boldsymbol{c}$ of the sinnerite lattice (in projection along [010]* of the sinnerite lattice). This symmetrical disposition is desymmetrized by the one-sided branching of the $\mathrm{As}_{5} \mathrm{~S}_{11}$ group, and within this layer pair there is an equal probability of attachment of the $\mathrm{As}_{5} \mathrm{~S}_{11}$ group as drawn in Figure 8 or of attachment of its enantiomorph (mirror image), which will have the additional As1-As7 branch situated on its opposite arm. In both described cases, attachment of the enantiomorph groups results in exchange of the $a$ and $c$ axes of the unit cell.

To summarize, sinnerite is an OD structure composed of two kinds of polar layers, with plane groups cm and $p 1$ (conveniently described as $c 1$ ), respectively, which allow alternative choices of layer stacking according to which enantiomorph of the $p 1$ structure is present. This choice takes place at every layer contact and proceeds differently on the opposite surfaces of the thinner, $\mathrm{As}_{3} \mathrm{~S}_{7}$ layer. According to Makovicky \& Skinner (1975), a twin law resulting from one occurrence of the enantiomorph attachment is $m \|(\overline{4} \overline{1} 4)$ of the sinnerite lattice.

Slicing the two types of layers and their contact into individual (010) atomic planes reveals the extreme underlying regularity and local cm plane-group symmetry of this $P 1$ structure. Atom configurations in the (010) planes through the cores of the $\mathrm{As}_{3} \mathrm{~S}_{7}$ and $\mathrm{As}_{5} \mathrm{~S}_{11}$ groups are identical: bonded $\mathrm{As}-\mathrm{S}$ groups paired around the imaginary barycenter of the $\mathrm{As}_{4}$ cluster, aligned parallel to the long diagonal of the (010) face, and interspaced by one intermediate S atom. We observe an overall cm pattern. The back-to-back boundary of the two layer kinds, mentioned above, is unique, with kinked S-As-S groups arranged in a cm pattern,

TABLE 3. SELECTED BOND DISTANCES (Å)
FOR SINNERITE

| As1-S9 | 2.24(3) | Cu4-S10 | 2.20(3) |
| :---: | :---: | :---: | :---: |
| As1-S15 | 2.30(3) | Cu4-S1 | 2.28(3) |
| As1-S5 | 2.40(3) | Cu4-S16 | 2.31(3) |
|  |  | Cu4-S8 | 2.32(3) |
| As2-S17 | 2.22(3) |  |  |
| As2-S8 | 2.29(3) | Cu5-S6 | 2.24(3) |
| As2-S12 | 2.35(3) | Cu5-S13 | 2.26(3) |
|  |  | Cu5-S11 | 2.34(3) |
| As3-S13 | 2.14(3) | Cu5-S8 | 2.44(3) |
| As3-S3 | 2.16(2) |  |  |
| As3-S14 | 2.35(2) | Cu6-S10 | 2.26(3) |
|  |  | Cu6-S6 | 2.28(3) |
| As4-S11 | 2.21(3) | Cu6-S7 | 2.29(4) |
| As4-S2 | 2.28(3) | Cu6-S9 | 2.54(3) |
| As4-S16 | 2.33(3) |  |  |
|  |  | Cu7-S7 | 2.25(4) |
| As5-S6 | 2.17(3) | Cu7-S12 | 2.23(3) |
| As5-S2 | 2.20(3) | Cu7-S13 | 2.34(3) |
| As5-S15 | 2.31(3) | Cu7-S5 | 2.36(3) |
| As6-S1 | 2.33(3) | Cu8-S3 | 2.28(3) |
| As6-S7 | 2.40(3) | Cu8-S4 | 2.31(2) |
| As6-S11 | 2.54(3) | Cu8-S12 | 2.34(3) |
|  |  | Cu8-S10 | 2.45(3) |
| As7-S10 | 2.27(3) |  |  |
| As7-S5 | 2.30(3) | Cu9-S9 | 2.20(3) |
| As7-S18 | 2.36(3) | Cu9-S4 | 2.24(3) |
|  |  | Cu9-S2 | 2.31(3) |
| As8-S4 | 2.20(3) | Cu9-S13 | 2.36(3) |
| As8-S14 | 2.25(3) |  |  |
| As8-S8 | 2.34(3) | Cu10-S5 | 2.22(3) |
|  |  | Cu10-S11 | 2.38(3) |
| Cu1-S16 | 2.20(3) | Cu10-S4 | 2.42(3) |
| Cu1-S6 | 2.27(3) | Cu10-S17 | 2.40(3) |
| Cu1-S18 | 2.30(3) |  |  |
| Cu1-S14 | 2.47(3) | Cu11-S9 | 2.16(3) |
|  |  | Cu11-S18 | 2.20(3) |
| Cu2-S18 | 2.29(3) | Cu11-S17 | 2.21(3) |
| Cu2-S15 | 2.34(3) | Cu11-S3 | 2.33(3) |
| Cu2-S1 | 2.39(3) |  |  |
| Cu2-S12 | 2.44(3) | Cu12-S3 | 2.11(3) |
|  |  | Cu12-S15 | 2.22(3) |
| Cu3-S1 | 2.15(3) | Cu12-S7 | 2.28(3) |
| Cu3-S14 | 2.30(3) | Cu12-S16 | 2.33(3) |
| Cu3-S17 | 2.31(3) |  |  |
| Cu3-S2 | 2.47(3) |  |  |

although they alternatively come from the groups to the left and to the right of the boundary, i.e., they are $p m$ in (hidden) detail. Finally, the front-to-front boundary is the cm arrangement of kinked S-As-S groups spaced with two S atoms in rows parallel to the long diagonal of the face. Thus, the $a$ and $c$ axes are practically identical in these sections and probability of order-disorder phenomena is very high.

## Non-OD twinning

The above analysis and the fact that the 'core portions' of the $\mathrm{As}_{5} \mathrm{~S}_{11}$ groups are copies of the entire $\mathrm{As}_{3} \mathrm{~S}_{7}$ groups, to which a two-As attachment is applied (see Fig. 6), bring us to realize that every time that the $\mathrm{As}_{5} \mathrm{~S}_{11}$ group is growing in a 'back-to-back' fashion on the (010) layer of $\mathrm{As}_{3} \mathrm{~S}_{7}$ groups, it can stop at the $\mathrm{As}_{3} \mathrm{~S}_{7}$ stage. In that case, it must be followed by a layer of $\mathrm{As}_{5} \mathrm{~S}_{11}$ groups in a 'front-to-front' relationship, i.e., we observe two $\mathrm{As}_{3} \mathrm{~S}_{7}$ layers 'back-to-back' together. The same happens when the thin layer in the 'back-to-back' attachment does not stop accreting and grows to become an $\mathrm{As}_{5} \mathrm{~S}_{11}$ layer, followed by the $\mathrm{As}_{3} \mathrm{~S}_{7}$ layer in a 'front-to-front' orientation. Now we have a 'back-to-back' pair of $\mathrm{As}_{5} \mathrm{~S}_{11}$ layers. In the former example, the last layer of $\mathrm{As}_{5} \mathrm{~S}_{11}$ groups can grow either in the $n(010)$-related orientation to the previous $\mathrm{As}_{5} \mathrm{~S}_{11}$ layers, resulting in the $n(010)$ twin law valid for the entire structure, or it can grow in a $2|\mid[101]$ related orientation to the previous layers, resulting in the $2 \|[101]$ twin law.

Makovicky \& Skinner (1975) quote one more twin law, $n \|(1 \overline{1} 0)$, again based on exchange of a combined $\mathrm{As}_{3} \mathrm{~S}_{7}$ and $\mathrm{As}_{5} \mathrm{~S}_{11}$ layer by a pure $\mathrm{As}_{3} \mathrm{~S}_{7}$ and $\mathrm{As}_{3} \mathrm{~S}_{7}$ layer, based on the 'unfinished' $\mathrm{As}_{5} \mathrm{~S}_{11}$ groups, i.e., not on an OD principle. This proceeds on the ( $1 \overline{1} 0$ ) plane of the sinnerite lattice and involves the combined $\mathrm{As}_{3} \mathrm{~S}_{7}$ \& $\mathrm{As}_{5} \mathrm{~S}_{11}$ slabs with this orientation (easily traceable in Fig. 6). A complete analysis of twin orientations resulting from these phenomena exceeds the scope of this paper; the interested reader is referred to Makovicky \& Skinner (1975).

We suggest that an undetected array of OD and non-OD defects of the kinds presented here is responsible for the deviating As-S bond-distances and displacement parameters of As and S, which were summarized above. In Figures 7 and 8 we see that, except for As3 and the S3 attached to it, both of which form part of the $\mathrm{As}_{3} \mathrm{~S}_{7}$ chain, the As and S atoms in question form part of the $\mathrm{As}_{5} \mathrm{~S}_{11}$ chain. They are concentrated on its branches: As7 with a high displacement factor, As6 from the short branch of the $\mathrm{As}_{5} \mathrm{~S}_{11}$ group, which is associated with S atoms with high displacement factors, and As5 with attached S2 and S15 (for details see above). These branches are sites of enantiomorphous exchange, chain-length mistakes, and OD phenomena. Thus, we suggest that, in spite of a pure single-crystal appearance, the examined sinnerite crystal contains a portion of the above-described defects. These produce spurious contributions to the measured reflections, as well as contributions to the subcell reflections and, in turn, produce effects superimposed onto a regular structure in the process of Fourier transformations, resulting in the observed deviations from a simple, more regular structure model. The near-perfect character of the natural crystal can be tentatively ascribed to slow

TABLE 4. BOND VALENCE SUMS FOR ATOMS IN SINNERITE

|  | As1 | As2 | As3 | As 4 | As5 | As6 | As7 | As8 | Cu1 | Cu2 | Cu3 | Cu4 | Cu5 | Cu6 | Cu 7 | Cu8 | Cu9 | Cu10 | Cu11 | Cu12 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| S1 |  |  |  |  |  | 0.855 |  |  |  | 0.265 | 0.506 | 0.356 |  |  |  |  |  |  |  |  | 1.982 |
| S2 |  |  |  | 0.979 | 1.215 |  |  |  |  |  | 0.213 |  |  |  |  |  | 0.328 |  |  |  | 2.735 |
| S3 |  |  | 1.354 |  |  |  |  |  |  |  |  |  |  |  |  | 0.356 |  |  | 0.311 | 0.564 | 2.585 |
| S4 |  |  |  |  |  |  |  | 1.215 |  |  |  |  |  |  |  | 0.328 | 0.397 | 0.244 |  |  | 2.184 |
| S5 | 0.708 |  |  |  |  |  | 0.927 |  |  |  |  |  |  |  | 0.287 |  |  | 0.419 |  |  | 2.341 |
| S6 |  |  |  |  | 1.317 |  |  |  | 0.366 |  |  |  | 0.397 | 0.356 |  |  |  |  |  |  | 2.436 |
| S7 |  |  |  |  |  | 0.708 |  |  |  |  |  |  |  | 0.347 | 0.386 |  |  |  |  | 0.356 | 1.797 |
| S8 |  | 0.953 |  |  |  |  |  | 0.832 |  |  |  | 0.320 | 0.231 |  |  |  |  |  |  |  | 2.336 |
| S9 | 1.090 |  |  |  |  |  |  |  |  |  |  |  |  | 0.176 |  |  | 0.442 |  | 0.493 |  | 2.201 |
| S10 |  |  |  |  |  |  | 1.005 |  |  |  |  | 0.442 |  | 0.376 |  | 0.225 |  |  |  |  | 2.048 |
| S11 |  |  |  | 1.182 |  | 0.485 |  |  |  |  |  |  | 0.303 |  |  |  |  | 0.272 |  |  | 2.242 |
| S12 |  | 0.810 |  |  |  |  |  |  |  | 0.231 |  |  |  |  | 0.408 | 0.303 |  |  |  |  | 1.752 |
| S13 |  |  | 1.429 |  |  |  |  |  |  |  |  |  | 0.376 |  | 0.303 |  | 0.287 |  |  |  | 2.395 |
| S14 |  |  | 0.810 |  |  |  |  | 1.061 | 0.213 |  | 0.337 |  |  |  |  |  |  |  |  |  | 2.421 |
| S15 | 0.927 |  |  |  | 0.902 |  |  |  |  | 0.303 |  |  |  |  |  |  |  |  |  | 0.419 | 2.551 |
| S16 |  |  |  | 0.855 |  |  |  |  | 0.442 |  |  | 0.328 |  |  |  |  |  |  |  | 0.311 | 1.936 |
| S17 |  | 1.151 |  |  |  |  |  |  |  |  | 0.328 |  |  |  |  |  |  | 0.257 | 0.430 |  | 2.166 |
| S18 |  |  |  |  |  |  | 0.788 |  | 0.337 | 0.347 |  |  |  |  |  |  |  |  | 0.442 |  | 1.914 |
|  | 2.725 | 2.914 | 3.593 | 3.016 | 3.434 | 2.048 | 2.720 | 3.108 | 1.358 | 1.146 | 1.384 | 1.446 | 1.307 | 1.255 | 1.384 | 1.212 | 1.454 | 1.192 | 1.676 | 1.650 |  |

rates of growth on the one hand and to the presumed absence of (010) as a growing face on the other hand.

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[^1]:    $R_{\text {int }}=(n / n-1)^{1 / 2}\left[F_{0}{ }^{2}-F_{0}(\text { mean })^{2}\right] / \sum F_{0}{ }^{2}$
    $R_{1}=\sum\left\|F_{0}\left|-\left|F_{\mathrm{c}} \| / \sum\right| F_{0}\right|\right.$
    $w R_{2}\left\{\sum\left[w\left(F_{0}{ }^{2}-F_{0}{ }^{2}\right] / \sum\left[w\left(F_{0}\right)^{2}\right)^{2}\right]\right\}^{1 / 2}$
    Goof $=\left\{\Sigma\left[2\left(F_{0}{ }^{2}-F_{c}{ }^{2}\right)^{2}\right] /(n-p)\right\}^{1 / 2}$ Where $n=$ no. of reflections, $p=$ no. of refined parameters

