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The crystal structure of vauquelinite and the relationships to fornacite

By L. FANFANI and P. F. ZANAZZI

Istituto di Mineralogia dell'Università di Perugia

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Auszug

Vauquelinit Pb₂CuCrO₄PO₄OH hat die Gitterkonstanten a = 13,754, b = 5,806, c = 9,563 Å, $\beta = 94^{\circ}34'$. Raumgruppe ist $P2_1/n$. Die Struktur wurde nach der Methode "trial and error", von den im Pb₂CuCrO₄AsO₄OH gefundenen Atomlagen ausgehend, bestimmt. Die Verfeinerung nach der Ausgleichsmethode ergab R = 0,089. Die Atomanordnung im Vauquelinit ist sehr ähnlich der des Fornacits; geringe Unterschiede bestehen nur in der Umgebung der Pb-Ionen und in der Anordnung der Symmetrieelemente (Fornacit hat die Raumgruppe $P2_1/c$).

Abstract

Vauquelinite, $Pb_2Cu[CrO_4PO_4OH]$, is monoclinic, with a = 13.754, b = 5.806, c = 9.563 Å, $\beta = 94^{\circ}34'$, space group $P2_1/n$. The crystal analysis of the mineral was determined by the trial-and-error method starting from the atomic positions found in fornacite. The refinement carried out by the least-squares method gave a final discrepancy index R of 0.089.

The atomic packing in vauquelinite is very similar to that in fornacite. Some differences occur in coordination around lead ions and in the arrangement of symmetry elements in the two minerals.

Introduction

The mineral vauquelinite is a basic lead and copper chromophosphate belonging to the monoclinic system with space group $C_{2h}^5 - P 2_1/n$ (BERRY, 1949). GUILLEMIN and PROUVOST (1951) assigned the formula Pb₂Cu[CrO₄PO₄OH] to the mineral. From diffractometric data and chemical analogies between vauquelinite and fornacite, a basic lead and copper chromoarsenate, these authors suggested the two minerals belong to an isomorphous series. BARIAND and HERPIN (1962) determined the unit cell of fornacite and related its lattice parameters to those of vauquelinite. The crystal analysis of fornacite was carried out (Cocco, FANFANI and ZANAZZI, 1967). In order to explain better the relations between the two minerals, the present investigation was undertaken.

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Crystal data

Crystals of vauquelinite from Beresov were used for the present work. The lattice parameters previously reported (BERRY, 1949) were refined by least-squares computations employing data from a powder diffractogram. The unit-cell constants are as follows:

$$\begin{array}{l} a = 13.754 \pm .005 \text{ \AA} \\ b = 5.806 \pm .006 \text{ \AA} \\ c = 9.563 \pm .003 \text{ \AA} \\ \beta = 94^{\circ}34' \pm 2'. \end{array}$$

The space group is $P2_1/n$, Z = 4 and $D_x = 6.16$ g cm⁻³. The observed value D is 6.16 g cm⁻³ (GUILLEMIN and PROUVOST, 1951). The linear absorption coefficient μ is 1021 cm⁻¹ for CuK α radiation.

A spherical specimen with radius 0.11 mm was prepared for the intensity-data collection. X-ray diffraction effects h0l, h1l, h2l, and h3l were recorded by an integrating Weissenberg apparatus on multiple films using Ni-filtered Cu $K\alpha$ radiation. A total of 1067 independent reflections were observed and they were measured with the help of a microdensitometer. Empirical correction for $\alpha_1 - \alpha_2$ doublet resolution was applied. Then Lorentz-polarization and absorption corrections were carried out. The transmission factors at different θ for a value $\mu R = 11.3$ were obtained by graphical interpolation from the values of EVANS and EKSTEIN (1952).

Crystal-structure determination

There are evident similarities between fornacite and vauquelinite. The lattice parameters of vauquelinite are very close to those of fornacite when one chooses as a and c axes of the unit-cell the [101] and [101] directions. The values of the parameters of vauquelinite according the new orientation are here compared with those of fornacite:

vauquelinite a = 16.110 Å, b = 5.806 Å, c = 17.366 Å, $\beta = 110°28'$ fornacite a = 8.101 Å, b = 5.893 Å, c = 17.547 Å, $\beta = 110°00'$.

The two minerals show the same prominent pseudocell, corresponding to the cell of fornacite with c halved. Furthermore, assuming the same orientation for the two cells, the intensities of correspondent spots are similar. Figure 1 shows a part of the h3l layer of the weighted reciprocal lattice for vauquelinite and fornacite.

From these considerations it follows that the two structures are closely related. Therefore we were led to propose a trial arrangement

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for the heavy atoms in vauquelinite derived from the arrangement found in fornacite. The agreement between calculated and observed structure factors was satisfactory. A first refinement of the locations of these atoms was carried out with a Fourier synthesis. Then it was possible to locate oxygen atoms from difference-Fourier syntheses and stereochemical considerations.



Fig. 1. A part of the h3l layer of the reciprocal lattice of (a) vauquelinite, and and (b) fornacite. The size of spots is set approximately proportional to the F_{a}^{2}

The refinement of the structure was performed with the leastsquares method. The weighing scheme suggested by CRUICKSHANK et al. (1961) was employed and the unobserved reflections were not included in the calculations. After four cycles of isotropic refinement, each followed by a proper rescaling of $|F_o|$'s, the discrepancy index $R = \Sigma ||F_o| - |F_c|| / \Sigma |F_o|$ for 523 observed reflections fell to the final

 Table 1. Fractional atomic coordinates with standard deviations and isotropic

 temperature factors

Atom	x		y		z		В
Pb(1)	$.7363 \pm$.0002	$.2256 \pm$: .0013	.4954 ±	.0002	$2.99\mathrm{\AA}^2$
Pb(2)	.0535	1	.7686	12	.1666	2	2.22
Cu(1)	.0000	—	.0000		.5000		2.96
Cu(2)	.0000		.5000	_	.5000		1.33
Cr	.8620	6	.2625	47	.1811	8	1.69
Р	.1584	9	.2737	59	.3207	13	1.83
O(1)	.1203	37	.0478	128	.3806	53	3.13
O(2)	.1104	37	.4780	117	.3868	54	3.25
O(3)	.1192	29	.2589	179	.1679	43	2.53
O(4)	.2683	31	.2951	136	.3470	45	2.50
O(5)	.8910	36	.0281	124	.1013	53	2.53
O(6)	.9103	36	.4836	124	.0964	54	1.98
O(7)	.9113	28	.2360	192	.3381	40	1.91
O(8)	.7470	30	.2735	145	.1838	44	2.32
OH	.9529	28	.7837	181	.3841	42	2.21

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Table 2. Observed and calculated structure factors

	h k l	Fo	Fc	h k :	l F _o	Fc	h	k 1	Fo	Fc	h k	l F _o	P
	$ \begin{array}{ccc} 2 & 0 & 0 \\ 4 & 0 & 0 \end{array} $	190.4	7.2 215.0	80- 100	6 5 153.0	17.2 -150.6	8 9	1 - 1 1 1	214.0	- 12.6	61- 71	4 221.6 4	-215.4 22.8
	600 800	250.2 135.6	-256.6 114.0	10 0 - 12 0	6 183.8 6	-200.4 - 25.4	9 10	1 - 1 1 1	73.1	71.8 15.2	71-81	4 4 258.8	- 4.6 244.6
	$ \begin{array}{cccc} 10 & 0 \\ 12 & 0 \\ \end{array} $	254.2	-237.6 8.8	120- 10	6 45.9 7	47.4 14.0	10 11	$ \begin{array}{c} 1 - 1 \\ 1 & 1 \end{array} $	57.4	11.6 - 67.6	81- 91	4 122.8 4	-116.6 - 3.0
	1400 1600	78.1	4.4 69.8	10- 30	7. 155.2	27.4 -164.0	11 12	$ \begin{array}{c} 1 - 1 \\ 1 1 \end{array} $	122.5	105.2 5.0	91 - 101	4	- 26.0 17.6
	$1 0 - 1 \\ 3 0 1$	90.5 252.9	117.8	30- 50	7 105.3	100.0 - 86.2	12 13	$ \begin{array}{c} 1 - 1 \\ 1 & 1 \end{array} $	155.9	- 24.8 -143.8	10 1 - 11 1	4 186.5 4	-167.2 12.0
	30-1 50 1	182.9	51.4 -186.2	50- 70	7 143.6 7 229.7	135.0 -241.2	13 14	1 - 1 1 1	68.5	- 54.6 13.8	11 1 - 12 1	4 4 154.5	29.8 138.0
	50 - 1 70 1	$159.2 \\ 396.9$	169.0 -395.0	70- 90	7	- 19.6	14 15	$ \begin{array}{c} 1 - 1 \\ 1 & 1 \end{array} $		- 4.4 - 8.4	12 1 - 13 1	4 111.0 4	93.2 - 19.4
	70 - 1 90 1	103.0	- 91.8 - 2.0	90- 110	7 51.7 7 74.0	- 45.2 - 73.0	15 16	1 - 1 1 1	28.9	- 29.2 7.4	131 - 141	4 4 30.6	3.6 - 14.6
	90-1 110 1	157.4	- 2.4	11 0 - 13 0	7 169.5	-177.2 57.8	16 17	1 - 1 1 1	52.5	5.4 39.8	14 1 - 15 1	4 41.1 4	- 37.8 - 7.0
	$11 \ 0 \ - \ 1$ $13 \ 0 \ 1$	289.0 142.3	-273.2 108.8	130-	7 8	- 25.4 41.6	17	1 - 1 1 2	97.8 171.9	- 88.6 208.4	15 1 - 16 1	4 4 50.4	8.8 50.8
	150 - 1		- 35.8	20-	8 168.0 8	-172.0	1	1 - 2 1 - 2		- 45.4 9.6	161-01	4 88.0 5	80.8 - 12.6
	17 0 1	150.5	108.2	40-	B 305.1	291.8	2	1 - 2 1 - 2	236,6	-288.2	11-	5 205.6	-211.6 16.2
	0 0 2	107.0	113.0	60-1	8 759	19.6	3	1 - 2		- 51.8	21-	5	35.2
	20-2	183.8	-242.8	80-	8 147.2 8 56 6	137.6	4	1 - 2	124.9	-134.0	31-	5 375.4	390.4
	40 - 2	536.1	585.4	10 0 - 1	5 J0.0 5 6 62 0	26.4	5	1 - 2	263 7	29.6	41~	5	- 29.2
	60-2 80 2	192.7	187.0	120 - 140 - 140	8 27.7 8 70.5	39.2	6	1 - 2	90.5	- 86.8	51-	5 113.1	-107.0
	80-2 100 2	278.3	287.0	10	9 129.8	-131.4	.7	1 - 2	03.2	45.4	6 1 - 7 1	5 273.4	9.2
	$10 \ 0 \ - \ 2$ $12 \ 0 \ 2$	209.2	24.4	30	9 123.5	-129.6	8	1 ~ 2	255.7	237.8	71-	5	46.4
	12 0 - 2 14 0 2	61.5 60.7	56.0 70.4	50 50 -	9 43.7	42.6	9 10	1~2	230.7	- 17.8	81 - 91	5 76.9	- 37:8
	140 - 2 160 2	112.4	-109.0 67.6	70	9	- 3.8	10 11	1 - 2	-2	6.4	91 - 101	5 176.0	-157.0
	160-2 103	66.9 263.1	- 52.6	90 90 -	9 76.3 9 96.8	79.0 97.2	11 12	1 - 2	136.0	- 7.4	10 1 - 11 1	5 66.1	4.0
	10-3 30-3	267.2 212.3	-316.6	11 0 11 0 -	9	12.0	12 13	1 ~ 2 1 2	201.8	171.4	11 1 - 12 1	5 76.9	- 69.6
	30-3 50-3	$229.7 \\ 104.8$	-250.2 93.8	130- 001	9 49.1 D 59.3	41.6 72.0	13	$1 - 2 \\ 1 2$	30.6	- 21.4 - 18.6	12 1 - 13 1	5 41.1	10.8
	50-3 70 3		14.2 - 48.0	201	0 50.8 0 102.6	- 51.0	14 15	1 - 2 1 2		- 2.4 4.0	131 - 141	5 136.0 5	-129.2
	70-3 903	68,2 186,0	- 63.8 154.4	401 40-1	0 112.4 0	138.0 - 26.6	15 16	1 - 2 1 2	106.5	3.8 81.4	14 1 - 15 1	5 5 35.1	25.2 - 21.2
	90-3 110 3	220.8	193.2	601 60-1	0 58.9 0 88.3	68.8 - 99.0	16 17	$1 - 2 \\ 1 2$	61.9	50.2 - 9.0	151 - 01	5	18.0 9.0
	11 0 - 3 13 0 3	74.0	32.4 100.8	80 1	0 71.8 0 125.8	76.6	17	1 - 2		-19.6 -62.0	11	6	4.8
	150-5	146.3	-126.0	10 0 -1	1 69.1	78.2	1	1 - 3 1 - 3	356.9 386.9	-399.8	$21 \\ 21 -$	6 84.2 6 112.0	109.0
	150 - 3 170 - 3	157.9	-193.2	3 0 1		- 11.4	2	1 - 3		19.2	31-	6	21.6 15.2
	204	149.9	-152.8	50 1	L 46.4	- 55.8	3	1 - 3		54.2	41-	6 192.0	187.0
	40 4	459.4	504.8	70-1	107.9	- 92.2	4	1 - 3	310.0	- 39.0	51-	6	- 26.8
	60 4 60 - 4	154.3	164.4	20'1	2	48.6	5	1 - 3	370.5	-368.6	61-	6 76.2	71.4
	80 4 80 - 4	190.9	168.0	40-1	2 50.0	70.2	6	$\hat{1} - \hat{3}$		45.0	71- 81	6 101.9	- 24.2
	1004 100-4		6.0 46.0	21	D 131.2	143.0 27.4	7	1 - 3		- 4.6	81 - 91	6 140.9 6	134.2
	1204. 120-4	74.9 170.8	68.6 166,8	41 51	0 300.2 0	326.4 - 13.0	. 8	1 - 3	200.7 د	2.4 -183.8	91 - 101	6 6 79.0	- 20.0
	1404 140-4	59.3 73.1	- 57,6 74,4	61 71	o •	60.0 - 1.0	9 10	1 - 3 1 3	203.2	-186.4 37.4	10 1 - 11 1	6 73.8 6	- 65.4 - 1.0
	1604 160-4	49.5 83.0	- 56.4 81.4	81 91	0 168.7 D	163.4 - 32.2	. 10 11	1 - 3 1 3	143.7	25.4 133.2	11 1 - 12 1	6 6	0.6 - 8.2
	105 10-5	152.1	168.2 - 24.2	10 1 11 1	0 133.9 0	-109.0 - 13.8	11 12	1 - 3 1 3	217.1	195.2 8.8	12 1 - 13 1	6	- 35.8 - 11.4
	305 30-5	188.2	31.0 -175.6	$12 1 \\ 13 1$	0	- 21.2 - 31.4	12	1 - 3 1 3	79.7	~ 2.8 85.0	131 - 141	6 6 123.5	- 16.2 -127.6
,	50 5 50 - 5	152.5	152.2	14 1 15 1	0 203.2	-177.2	13	1 - 3	67.5	68.4	141 - 01	6 128.7 7	-128.4
	70-5	67.3 262.2	- 67,4	16 1 17 1	0 40.0	24.0	14 15	1 - 3 1 - 3	76.9	18.4	11-	7 176.7	- 37.4
	90-5	63.8	- 32.6	11	1	- 28.4	15	1 - 3	88.7	- 2.0	21~	7	18.4
	11 0 - 5	130.2	-142.4	11-21	1 245.0	-282.2	10	1-3	36.5	25.4	31-	7 61.2	273.0 59.4
	130-5	68.2	69.6	31	1 527.4	599.2	1	1 4	140.1	- 4.6	41-	Ż	- 19.0
	150-5	435.3	31.8 483.2	41	1	- 53.8	2	1 4	254.7	-277.8	51-	7	- 41.6
	20 6	• • • • • • •	11.4	51	56.7	- 56.4	3	1 4	10.4	16.2	6 1 - 7 1	7	24.2
	40 6 40 - 6	172.6 227.0	159.6	6 1 6 1 -	1	5.4 53.4	44	1 4 1 - 4	76.9	- 73.8	71- 81	7 289.1 7	270.8 - 13.0
	60 6 60 - 6	91.4 141.8	- 83.4	7 1 7 1 -	1 1 440.4	22.8 448.6	55	1 4 1 - 4		- 9.2	81 - 91	7 7 99.5	- 11.4
	80 6	58.4	53.0	8 1	1	- 22.0	6	14	108.9	-104.8	91 -	7	6.4

.

The crystal structure of vauquelinite

Table 2. (Continued)

bk 1	F.	F	hk 1	F	P	hk 1	F	F	h k l	P	P
10 1 7	0	1.8	16 2 0	42.3	- 29.4	12-4	95.6	90.2	727	145.9	155.4
10 1 - 7	24.7	16.4	021	47.6	84.2	224	250.5	269.4	72-7	59.7	- 50.8
11 1 - 7	70,3	73.6	12 - 1	216.2	-239.6	324	29110	- 79.2	82-7		1.6
12 1 7 12 1 - 7		- 5.6	22 1 22 - 1	54.8	56.2 9.0	· 42 4	212.0	- 44.0 -220.8	927 92-7	41.2	- 42.4 - 33.4
1317	60.2	- 73.2	32 1 32 1	85,8	88.8	42-4	137.6	126.8	10 2 7		- 4.4
01 8	142.3	146.6	4 2 1	192.0	22.0	52-4	40.7	17.6	11 2 7	26.8	25.4
11 - 8 11 - 8		- 18.4 2.8	42~1 52 1		- 3.8 39.6	624 62-4	346.5	- 30.4 342.6	11 2 - 7 12 2 7	99+4	101.0
21 8	110 7	- 12.4	52-1	291.0	-309.4	724	,,	- 14.2	12 2 - 7		- 14.2
31 8	142.)	- 13.6	62 - 1	07.0	41.0	72-4 82 4	124.7	- 69.0	132 - 7 028	63.9	58.6
31-8 41 8		- 9.6	721 72-1	218.4	201.0	82-4	141.7	-132.4	128		49.0
41-8	97.8	- 94.0	82 1	10.1	- 52.0	9.2 - 4		11.0	2 2 8	155.3	184.6
51 - 8		- 22.0	82 - 1 92 1	117.5	0.6	1024 102-4	45.7	33.0 - 3.2	22-8 32 8	99.4	115.8 - 27.8
618	121.1	-135.8	92-1	80.5	- 68.8	11 2 4		17.0	32-8		- 57.8
71 8		6.2	102 - 1		75.2	1224		- 57.0	42-8	182.9	-193.0
71-8	42.8	17.8	11 2 1 11 2 - 1	71.0 212.0	61.0 187.6	122 - 4 132 4	98.6	- 92.4 21.0	528 52-8		6.2 20.4
81-8	110.6	105.0	12 2 1		- 44.4	132-4		8.6	62 8	139.4	163.0
91 - 8		- 16.0	122 - 1 132 1	147.8	- 22.8	1424 142-4	98.3	102.2	62-8 72 8		11.8
10 1 8	107.8	-124.2	132 - 1		- 18.0	15 2 4		- 4.6	72-8		- 21.2
11 1 8		4.6	142 - 1 142 - 1		3.0	0 2 5		- 59.8	82-8	66.9	- 75.0
11 1 - 8 12 1 8	43.5	- 3.0 50.8	152 1 152 - 1	37.8 68.4	- 49.8	12 5	220.3	-244.8	92 8 92 8		- 2.0
121-8	85.9	105.2	16 2 1		- 19.2	2 2 5	11010	- 8,6	10 2 8		- 22.0
11 9	101.2	- 21.2 -121.0	102 - 1 022	96.0	- 31.8	22-5	122.4	13.8	102 - 8 1128	34.4	27.6
11-9	157.3	-170.4	122	108.0	102.0	32-5	50.0	19.2	11 2 - 8		9.2
21-9		10.0	12 - 2 2 2 2	453.5	502.6	42 0	52.9	23.0	122-8		5.4 - 12.6
31 9	33.4	- 30.8	22 - 2	157.2	189.2	525	194.2	-214.4	129	48.7	52.8
41 9		- 6.6	32-2	111.6	-103.6	62 5	02.4	55.8	22 9	10.1	6,2
41-9 51 9	109.9	- 17.8 -127.2	422	104.7 386.2	107.4	62-5		28.2 - 18.0	22-9	46.9	- 9.6
51-9	148.9	-156.0	522		17.0	72-5	164.0	154.4	32-9	,	32.4
61 - 9		17.6	52-2 62 2	318.9	322.6	82 5		- 8.0 - 42.8	429		- 27.6
719	35 1	- 0.4	62-2	70 7	20.8	92 5	72.9	- 68.6	52 9	74.1	- 82.8
81 9	JJ.1	10.2	72 - 2	19.5	- 35.8	10 2 5	21.4	42.4	52-9 62 9	55.7	- 11.2
81-9	52.9	10.6	822 82-2	112.6	-103.0	10 2 - 5	145 9	- 18.2	62-9	97.9	- 14.2
9 1 - 9	69.9	- 81.8	922	,,,,,	10.2	11 2 - 5	42.3	42.8	72-9	60.1	- 48.4
10 1 9		27,6	92-2 102 2		50.0	1225 122-5		- 12.4	82 9 82 - 9		- 17.2
11 1 - 9	100.2	112.0	102 - 2	68,8	48.4	13 2 5	117 5	- 0.8	929	79.7	- 98.0
1 1 10	10.7	- 9.0	11 2 - 2		15.6	14 2 5	117.9	7.0	10 2 9	120.0	17.6
1 1 -10 2 1 10	104.7	- 19.0 -121.0	1222 122-2	86.9	- 75.0	142-5	40.1	9.0	102 - 9 112 - 9	61.6	9.6
2 1 -10	51.8	47.6	13 2 2		11.4	0 2 6	326.5	-356.8	0 2 10	01.0	5.6
31 10 31 -10		- 17.2	132 - 2 142 - 2		25.4	12 - 6 12 - 6		61.2 59.4	1 2 10 1 2 -10		- 5.0 31.4
4 1 10	34.1	- 31.0	142 - 2	139.1	138.6	226	117 0	11.8	2 2 10	85.0	100.0
5 1 10		- 5.6	15 2 - 2	<i>.</i>	- 9.0	326	147.0	- 3.2	3 2 10	110.0	- 34.8
51-10 61 10	54.6	- 9.0 - 60.2	1622 162-2	60.8 90.7	- 37.6 88.8	32 - 6 42 - 6		- 17.6	32-10 42 10	71.0	- 16.0 - 96.2
6 1 -10	87.3	- 91.4	023		- 9.8	42-6		- 50.0	4 2 -10	53.3	50.6
7 1 -10		- 0.6	12 - 3	123.2	135.6	52-6		75.8	5 2 -10		4.8
8 1 10 8 1 -10	79.0	99.4 - 73.2	22 3		1.4	626 62-6	184.0	191.0	6 2 10 6 2 -10	40.4	- 47.6
91-10		- 7.6	32 3	74.4	64.6	726	1001)	1.4	7 2 -10	10,11	- 33.2
0 1 11	11.5	- 00.8	2 - 3 4 2 3	42.7	- 63.2	72-6		- 5.4 26.6	82 - 10 02 11	54.8	- 61.2 - 20.8
1 1 11	52.5	- 66.4	42-3	199.0	- 80.4	82-6		28.6	1 2 11	88.1	- 95.2
21 11	40.)	20.8	52-3	167.8	-162.8	92-6		25.6	2 2 -11 2 2 11		- 2,6
21 - 11 31 11	40.4	11.2	62 3 62 3		- 24.4	10 2 6	139.8	155.6	2 2 -11	48 4	4.4
31-11	115.5	133.2	7 2 3	60.5	- 54.4	11 2 6		- 24.4	3 2 -11		11.8
4 1 11 4 1 - 11		5.6 - 11.8	72-3		- 35.2	11 2 - 6 12 2 6	38.9	- 32.0 48.2	4 2 -11 5 2 -11	43.5	12.8
5 1 11	16 6	- 27.2	82-3	079 7	- 19.4	122 - 6		16.4	6 2 -11		7.0
1 2 0	93.5	99.8	92-3	229.8	-223.4	132 - 6		- 10.8	1 3 0	59.5 57.1	45.0 - 65.2
22 0	182.9	175.8	10 2 3		25.2	142-6	34.4	33.6	230	134.3	-115.4
420	163.6	-155.6	11 2 3	72.2	- 83.6	12 7	99.4	-110.4	430	230.0	-227.0
520 620	98.4 255.8	100.8 260.8	$11 \ 2 \ - \ 3 \\ 12 \ 2 \ 3$	91.8	- 97.8 - 7.2	12 - 7 22 7	120.9	-122.0 36.6	530 630		33.6 - 41.2
720	49.5	- 13.6	122 - 3	174 0	- 6.2	22 - 7	66 -	1.4	730	60.2	35.6
920 920	22.0	27.0	132 - 3 132 - 3	145.9	-127.4	527 32-7	158.7	-148.4	830 930	120.8	-122.0 68.4
10 2 0	343.1	325.2	14 2 3		39.2	42 7		- 7.4	10 3 0	75.3	69.4
12 2 0	45.0	50.8	15 2 3	100.1	85.6	52 7	. (19.4	12 3 0		22.4
1) 4 0 14 2 0		- 3.6 23.8	152 - 3 024	88.8	79.6	52-7 627	163.3	-160.6 28.6	1330 1430	32.4 145.9	34.0 138.8
15 2 0		- 19.0	124		1.0	62-7		27.2	15 3 0		- 29.6

437

Table 2. (Continued)

hk l	F	P.	hk l	F.	F	h k l	P	F	h k l	F	F,
1630	20.5	- 15.4	13-3	282.5	308.4	535	74.9	71.8	103-7	•	0.8
031		63.0	233		- 33.0	53-5	86.1	84.0	11 3 7		29.4
13 1	a1.5.1	10.6	23-3		- 34.4	63 5		- 65.0	11 3 - 7	44.4	- 54.0
23 1	50.6	- 63.8	33-3	51.7	- 41.8	0) -) 7 3 5	171.0	- 5.0	12 3 - 7	20 7	50.8 28.6
23 - 1	125.4	-129.8	43 3	51.7	78.8	73-5	1/1.0	- 18.8	038	97.2	-105.8
33 1	350.8	-367.0	43-3	112.0	106.2	83 5	49.8	46.6	13 8	,,	32.6
33-1	64.8	- 65.6	533	231.2	241.2	83-5		75.6	13-8	39.0	- 24.8
43 1	50.7	110.2	53-3	228.1	229.4	935	59.4	- 64.0	238	00 7	2.8
531	63.7	53.0	63-3	Ju. J	- 60.0	10 3 5	110.0	5.0	338	90.1	22.2
53-1	70.6	64.4	733		14.8	10 3 - 5		- 3.0	33-8		- 14.2
631		- 5.0	73-3		27.0	11 3 5	47.1	- 47.8	438		- 12.0
63-1	91.2	- 83.4	833		- 8.2	11 3 - 5	49.8	48.8	43-8	66,8	72.4
73-1	326.9	-330.2	0 3 3	129.7	118.8	12 3 - 5		42.4	53-8	20.1	- 30.6
831	90.8	85.2	9 3 - 3	155.1	141.8	13 3 5	23.2	22.8	638	81.4	101.6
83-1	67.1	69.8	10 3 3		- 52.8	133-5	103.4	100.6	63-8		16.2
93 1	129.3	128.8	10 3 - 3		- 72.0	14 3 - 5	21.6	- 21.4	738		- 28.6
9 5 - 1	51.7	- 49.8	11 3 3	101.9	-105.0	176		- 12.0	73-8	70.0	- 50.0
10 3 - 1		- 11.8	123 3	47.9	11.8	13-6		- 47.2	83-8	69.8	- 79.0
11 3 1	48.6	58.6	12 3 - 3	43.6	11.0	236	63.3	- 68.2	938	• ,	9.8
11 3 - 1	70.2	- 64.4	13 3 3	56.3	- 64.2	23-6	83.4	- 88,8	93-8		0.8
12 3 1		0.6	13 3 - 3	60.2	- 62.6	33 6	55.2	- 60.4	10 3 8	71.8	92.8
12 3 - 1	115.0	49.8	14 3 3		- 6.2	55-0 13 6	168.3	- 48.2	$10 \ 3 - 8$	22.8	- 25.0
13 3 - 1	42.4	36.8	15 3 3	45.2	- 51.4	4 3 - 6	146.6	-146.0	12 3 - 8	68.3	- 82,6
14 3 1	30.1	- 36.4	153-3	68.3	- 63.2	536		10.8	039		72.0
143-1	30.1	21.0	034	94.9	99.4	53-6		16.0	139	73.3	94.4
1531		5.4	134		- 0.6	636	61 7	- 30.0	13-9	110.4	129.8
16 3 1		- 6.8	234	186.8	204.6	736	01.7	2.4	23-9		- 4.6
163-1		20.2	23-4	50.2	- 51.8	73-6		17.2	339	30.9	37.4
032	135.8	-138.2	334		- 49.0	836	65.6	- 73.0	33-9		- 14.8
13 2	80 7	79.8	33-4	67 7	53.8	83-6	86.1	- 90.6	439		34.4
23 2	00.9	- 6.4	4 7 4	0).)	- 15.2	93-6		39.4	4) - 9	67.1	40.0
23-2	202.6	213.8	534	54.0	- 13.8	10 3 6	51.7	52.0	53-9	96.5	112.2
332	50.9	44.4	53-4		47.8	10 3 - 6	46.7	49.0	639		- 17.0
33-2		- 32.6	634	74.9	70.0	11 3 6		- 11.6	63-9		- 35.0
4 3 2	109.2	- 25.0	0 3 - 4	102 6	144.4	11 3 - 0		2.0	73-9	97.0	- 4.4
5 3 2	74.9	74.2	73-4	1.1.	- 37.6	12 3 - 6		27.0	83 9	-/	- 5.8
53-2		- 25.6	834	174.0	-173.8	13 3 6		27.0	83-9		5.0
632	184.8	183.4	83-4	92.2	96.8	13 3 - 6	23.9	24.6	93-9	52.1	60.0
73 9	59.0	- 36 6	934		- 4.2	14 3 - 0	00.0	95.2	1 3 10	57.0	4).0
73-2	93.6	-103.6	10 3 4		- 15.8	137		32.2	1 3 -10		17.8
83 2	79.9	85.6	10 3 - 4	132.0	129.2	13-7	105.0	122.2	2 3 10	81.8	93.2
83-2	191.0	-180.8	11 3 4		~ 20.0	237		- 25.0	2 3 -10	35.9	- 35.4
932	62.1	40.8	11 3 - 4	100 7	~ 74.8	23-7	176 7	- 70.0	3310		- 33.2
10 3 2	153.6	148.2	12 3 - 4	68.7	- 65.6	33-7	1/0./	- 29.4	4 3 10	27.0	26.0
10 3 - 2	1,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	- 11.4	13 3 4		35.2	437		70.2	4 3 -10		15.2
11 3 2		- 74.8	133-4		- 3.8	43-7		- 0.2	5 3 10		- 1.6
113 - 2		- 26.2	14 3 4		3.0	537		- 6.0	5 3 -10	07.0	11.2
12 3 + 9	93.4	- 84.8	143-4	24.3	21.6	53-7		25-4 16.4	6 3 -10	27.8	41.8
13 3 2	11 91 9	- 15.6	13 5	126.2	138.0	63-7		- 58.6	7 3 -10		- 2.6
13 3 - 2		43.0	13-5	52.9	- 42.0	737		4.2	8 3 -10	49.4	54.8
14 3 2		11.4	23 5	106.6	- 99.8	73-7	199.5	-204.6	0 3 11	or -	14.6
143 - 2		- 2.0	23-6	71.0	- 54.6	837		42.0	1 3 11	24.3	47.2
$10 \ 3 - 2$	37.8	- 38.2	33-5	284.8	-295.4	937	69.8	85.0	2 3 -11	12.0	- 15.0
033	132.8	140.4	435		11.0	<u> 9</u> 3 - 7	.,	- 17.0	3 3 -11	80.3	-102.0
13 3	215.7	229.0	43-5	106.8	98.0	10 3 7		6.4			

value 0.089. The R index without the contributions of the oxygen atoms was 0.15.

The atomic coordinates with their standard deviations and the isotropic thermal parameters are given in Table 1. The observed and calculated structure factors are compared in Table 2. The scattering-factor values by CROMER and WEBER (1965) for the Pb⁺² ion, and by International Tables (1962) for Cu⁺², Cr, P and O⁻¹, were used for the calculations. Contribution of the real component of the anomalous dispersion to the scattering factors of the heavy atoms was taken into account: correction was applied with the values $\Delta f'$ determined for CuK α radiation by CROMER (1965). All the calculations were performed with an IBM 1620 computer.

Discussion of the structure

Bond lengths and angles, as well as their standard deviations (CRUICKSHANK and ROBERTSON, 1953; DARLOW, 1961) are listed in Table 3 and 4. The atomic array of vauquelinite projected along b axis is shown in Fig. 2.

The arrangement of oxygen atoms around phosphorus and chromium is tetrahedral. The mean P—O and Cr—O distances are 1.52 and 1.62 Å respectively, in agreement with those found in literature.

The Cu⁺² ions are in special position at inversion centers. They have six nearest oxygen atoms forming distorted tetragonal bipyramids. Two of the six oxygen atoms belong to hydroxyl groups. The distances in the planar squares range from 1.76 to 2.10 Å.

Pb(1) has nine nearest oxygen neighbours, the Pb—O bond lengths varying from 2.40 to 3.17 Å. Two larger distances occur with values 3.36 and 3.38 Å. Pb(2) binds ten near oxygen atoms with distances in the range 2.47 to 3.09 Å.

Pb(1,I)-O(1',II)	2.73 Å	\pm .06 Å	Cu(1,I) - O(1,I)	2.10 Å -	05 Å
O(2,II)	2.88	.06	OH(',I)	1.76	.08
O(3, IV)	2.40	.04	O(7',I)	2.34	.07
O(4,II)	3.17	.07			
O(5,III)	2.60	.06	Cu(2,I) - O(2,I)	1.94 Å ∃	$\pm .05$ Å
O(6', III)	2.56	.06	OH(',I)	2.06	.09
O(7,I)	2.94	.04	O(7',I)	2.44	.08
O(8,I)	3.01	.04			
O(8',III)	3.15	.07	Cr(1,I) - O(5,I)	$1.63 \text{ \AA} \pm$	$\perp .07$ Å
	9.90	05	O(6,I)	1.68	.07
O(4', 11)	3.38	.07	O(7,I)	1.60	.04
O(4, IV)	3.36	.04	O(8,I)	1.59	.04
Pb(2,I) = O(1',I)	2.71 Å	\pm .06 Å		{	
O(2,I)	2.76	.06	P(1,I)-O(1,I)	1.54 Å 🗄	± .07 Å
O(3,I)	3.09	.10	O(2,I)	1.52	.07
O(3',I)	2.99	.10	O(3,I)	1.51	.04
O(4,III)	2.47	.04	O(4,I)	1.52	.04
O(5',I)	2.73	.06			
O(5', II)	2.97	.05	OH(I)-O(8,III)	2.77 Å ∃	06 Å
O(6',I)	2.62	.06	· ·		
O(6',II)	2.99	.05		[
OH(',I)	2.59	.04	})	
	1		•	1	

Table 3. Bond lengths and their standard deviations

(I: x, y, z; II: $\overline{x}, \overline{y}, \overline{z}$; III: $\frac{1}{2} - x, \frac{1}{2} + y, \frac{1}{2} - z$; IV: $\frac{1}{2} + x, \frac{1}{2} - y, \frac{1}{2} + z$; the label indicates atoms of adjacent cells)

Table 4. Bond angles and their standard deviations in ${\rm CuO}_4({\rm OH})_2,$ ${\rm PO}_4$ and ${\rm CrO}_4$ coordination polyhedra

O(1,I)-P(I)-O(2,I)	$110^\circ\pm3^\circ$
-O(3,I)	102° 4°
O(4,I)	112° 4°
O(2,I)-P(I)-O(3,I)	108° 4°
-O(4,I)	109° 4°
O(3,I) - P(I) - O(4,I)	116° 2°
O(5,I)-Cr(I)-O(6,I)	107°±3°
-O(7,I)	105° 4°
-O(8,I)	109° 3°
O(6,I)- $Cr(I)$ - $O(7,I)$	112° 4°
-O(8,I)	114° 3°
O(7,I)— $Cr(I)$ — $O(8,I)$	110° 2°
O(1,I)-Cu(1,I)-OH(I')	$91^{\circ}\pm2^{\circ}$
-O(7,I')	87° 2°
OH(I')-Cu(1,I)-O(7,I')	82° 3°
O(2,I)— $Cu(2,I)$ — $OH(I')$	$89^{\circ} \pm 2^{\circ}$
-O(7,I')	89° 2°
OH(I')-Cu(2,I)-O(7,I')	92° 3°

The presence of hydrogen bond OH(I)-O(8,III), 2.77 Å long, was deduced from the interatomic distances between the OH group and the neighbouring oxygen atoms.



Fig. 2. The structure of vauquelinite projected along the b axis

The vauquelinite structure consists of chains of linked polyhedra of oxygen atoms and hydroxyls about Cu extending parallel to the b axis. The individual polyhedra are joined together by an edge. These chains are linked to phosphate and chromate tetrahedra and to lead polyhedra in a compact three-dimensional array which explains the lack of cleavage in the mineral.

Relationships between vauquelinite and fornacite

As expected from the close relations between fornacite and vauquelinite structures, the packing of the atoms is essentially identical in the two minerals. In Table 5 the atomic coordinates of vauquelinite

Table 5. Comparison of atomic parameters in vauquelinite and fornacite The atomic coordinates of vauquelinite are referred to the cell having the same b, 2a' = [101] and $c' = [10\overline{1}]$

Atom		Vauquelinite	Fornacite	Atom		Vauquelinite	Fornacite
	x	.232	.219		x	.287	.290
Pb(1)	y	.226	.220	O(3)	\boldsymbol{y}	.259	.209
	z	.380	.376		z	.024	.015
	\boldsymbol{x}	.220	.223		\boldsymbol{x}	.614	.638
Pb(2)	y	.769	.773	O(4)	y	.295	.315
	z	.057	.059	ļ	\boldsymbol{z}	.040	.048
	x	.500	.514		x	.993	.994
Cu(1)	y	.000	.008	O(5)	y	.028	.032
	z	.250	.251		z	.105	.102
	x	.500	.486		x	.007	.004
Cu(2)	y	.500	.508	O(6)	y	.484	.473
	z	.250	.249		z	.096	.094
	x	.479	.487		x	.250	.250
P,As	y	.274	.260	O(7)	y	.236	.248
	z	.081	.081		z	.213	.214
	x	.043	.050		x	.931	.927
\mathbf{Cr}	y	.263	.260	O(8)	y	.274	.289
	z	.159	.159		z	.219	.218
	x	.501	.541		x	.338	.344
0(1)	y	.048	.028	OH	y	.784	.761
	z	.132	.138	1	z	.215	.219
	x	.498	.472				
O(2)	y	.478	.478	1			
	z	.140	.132	1			

referred to the unit cell with 2a' = [101] and $c' = [10\overline{1}]$ are compared with those found in fornacite.

Because of the particular locations of Pb(1), Pb(2), Cr, P, O(3), O(4), O(7), O(8) and OH at y about 1/4 and 3/4, and of Cu(1), Cu(2), O(1), O(2), O(5) and O(6), lying two by two at the same x and z coordinates and at y approximately 0 and $\frac{1}{2}$, the two structures simulate the presence of mirror planes at y = 1/4 and 3/4. In such a way it is possible to explain the presence of a pseudocell with the same orientation as in fornacite but with c halved and with space group



Fig. 3. The different arrangement of symmetry elements in vauquelinite (a) and in fornacite (b). The pseudocells are marked by dashed line

 $P2_1/m$. Recently the new formula $Pb_2Cu[SO_4PO_4OH]$ was assigned to the mineral tsumebite (BIDEAUX, NICHOLS and WILLIAMS, 1966) which crystallizes in the space group $P2_1/m$ with the following lattice parameters: a = 8.70 Å, b = 5.80 Å, c = 7.85 Å and $\beta = 111^{\circ}30'$. Similarities in the chemical formula and comparison of the lattice parameters and space group of tsumebite with the pseudocell found in fornacite and vauquelinite, suggest that the structure of this mineral can be taken as a model from which the structures of vauquelinite and fornacite derive if we suppose that the replacement of SO_4 with CrO_4 groups cause the disappearance of the mirror planes with a general rearrangement of atoms in the space group $P2_1/n$. A private communication of M. C. NICHOLS on the crystal structure of tsumebite confirms our supposition.

Some differences occur in the coordination of oxygen atoms around the lead ions in fornacite and vauquelinite. In fornacite both distinct lead ions in the unit cell show coordination number 9 + 1, while in vauquelinite the number is 9 + 2 for Pb(1) and 10 for Pb(2).

The Cu^{+2} ions in vauquelinite are at inversion centers, while in fornacite they are located near to the screw axis. It is remarkable

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in fact that, though fornacite and vauquelinite belong to the same space group C_{2h}^5 , the symmetry elements in the cells are arranged in a different way, as shown in Fig. 3.

In conclusion the two structures are closely related, and according GUILLEMIN and PROUVOST (1951) the minerals could form an isomorphous series. However the chemical analyses in literature show only a small miscibility.

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