An Exploration of Theoretical and Experimental Electron Density Distributions and SiO Bonded Interactions for the Silica Polymorph Coesite

G. V. Gibbs,^{*,†} Andrew E. Whitten,[‡] Mark A. Spackman,[‡] Marilena Stimpfl,[§] Robert T. Downs,[§] and Michael D. Carducci^{||}

The Department of Geosciences, Virginia Tech, Blacksburg, Virginia 24061, Chemistry Department, School of Biomedical, Biological and Molecular Sciences, University of New England, Armidale, NSW 2351, Australia, Departments of Geosciences and Chemistry, The University of Arizona, Tucson, Arizona 85721

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A multipole representation of the experimental electron density distribution for the high-pressure silica polymorph coesite, using Hirshfeld-type radial functions, has been generated with single-crystal X-ray diffraction data recorded to a sin θ_{max}/λ value of 1.21 Å⁻¹ at 100 K. Unlike an earlier modeling of the distribution, where a more limited data set was analyzed, deformation electron density maps display bananashaped isosurfaces in the lone-pair regions of each of the oxide anions involved in the bent SiOSi angles as well as teardrop-shaped ones along each of the SiO bond vectors. They also display a ring torus isosurface about O1, the oxide anion involved in the straight angle. Laplacian $-\nabla^2 \rho$ maps display belt-shaped isosurfaces, centered near the apexes of the bent angles, that wrap about halfway around the oxide anions, with a ring torus-shaped isosurface surrounding O1. An analysis of $-\nabla^2 \rho$ revealed that the (3,-3) critical point associated with the anions involved in the bent angles are associated in general with larger maxima than that associated with the straight angle, evidence that the electron density is more locally concentrated on the oxide anions involved in the bent angles. As such, these anions are asserted to be more susceptible to electrophilic attack by hydrogen, a feature that provides an experimental basis for why hydrogen in H- and Al-bearing coesite avoids O1 and is observed to dock in the vicinity of the oxide anions involved in the bent angles. The bond critical point properties of the experimental multipole representation of the electron density distribution for coesite together with those for the very high-pressure silica polymorph, stishovite, conform with those calculated for the SiO bonded interactions for a relatively large number of silicate crystals. Not only are they similar in value with the theoretical properties, but together they correlate with the observed SiO bond lengths as predicted by the calculations. The observed SiO bonds display a relatively wide range of $\nabla^2 \rho(r_c)$ values between ~10 e Å⁻⁵ for stishovite and ~20 e Å⁻⁵ for coesite. The larger $\nabla^2 \rho(r_c)$ values recorded for coesite, considered typical of first row closed-shell ionically bonded atoms, may not be typical for a closed-shell bonded interaction involving second row atoms such as the four-coordinate Si in coesite. The maxima along the bond vectors and in the lone-pair regions displayed by the experimental $\Delta \rho$ and $-\nabla^2 \rho$ maps are indicative of shared covalent bonded interactions. The evidence suggests that the value of the electron density at the bond critical point for a given bonded interaction is a reliable measure of bond type: the larger the value $\rho(r_c)$, the greater the shared covalent interaction.

Introduction

Experimental and theoretical studies of the silica polymorphs have been a meeting place where experiment has engaged theory in advancing our understanding of silica, its physical behavior, crystal chemistry and SiO bonded interactions.^{1,2} Not only have the studies provided a basis for understanding why there are so many different stable and metastable forms of silica but also why silica has such excellent glass forming properties.^{3,4} They have also provided an underpinning for the proposal that the structure of silica is governed in large part by short-ranged molecular-like binding forces.^{5–7} A connection has also been established between the SiO bond lengths, R(SiO), and the bond critical point properties⁸ for theoretical electron density distributions, ρ , for molecular moieties of the silica polymorphs.⁹ The calculations show that the bond lengths decrease linearly as the theoretical value of the electron density at the bond critical point, $\rho(r_c)$, increases together with a concomitant increase in the curvatures of the electron density at the point both perpendicular and parallel to the bond path. A mapping of the theoretical $\Delta\rho$ deformation density, the electron localization function, ELF, and the Laplacian $-\nabla^2\rho$ distributions for the silica polymorphs quartz, coesite, and stishovite, have also served to highlight sites of potential chemical reactivity and favorable docking sites for hydrogen¹⁰⁻¹² in the lone-pair regions of the oxide anions.

Together with the theoretical advances, experimental static $\Delta \rho$ maps generated in a multipole refinement of the coesite structure display bonding maxima along each of the SiO bond vectors in the vicinity of the more electronegative oxide anions together with a low-lying bridge of density in the interior of each bent SiOSi angle.¹³ As asserted by Coppens,¹⁴ maxima along bond vectors is evidence for a shared covalent bonded interaction. On this basis it was concluded¹⁵ earlier that the SiO

[†] Virginia Tech.

[‡] University of New England.

[§] Department of Geosciences, The University of Arizona.

Department of Chemistry, The University of Arizona.

bond in coesite and related silica polymorphs is predominantly covalent in character. In sharp contrast, it was asserted by Cohen¹⁶ that the maxima displayed along the bond vectors of quartz show that bonded interactions in silica are predominantly closed-shell ionic, consisting of "nearly fully charged Si⁴⁺ and O^{2-} ions rather than as neutral atoms with covalent bonds." However, conspicuously lacking in the experimental maps for coesite¹³ are covalent features in the nonbonding regions of each of the oxide anions that can be ascribed to lone-pair electron density. With the exception of these missing features, maps calculated for representative hydroxyacid molecules with SiOSi dimers were found to be in close correspondence with static $\Delta \rho$ maps those observed for coesite.¹³ Despite the relatively small sizes of the molecules, the SiO bond lengths and SiOSi angles of the molecules likewise show a close correspondence with those observed for coesite and several other silica polymorphs.^{4,5} The $\Delta \rho$ maps for the molecules display welldeveloped maxima in both the bonding and nonbonding regions of the molecule. The close correspondence in the geometry and the electron density distributions generated for hydroxyacid silicate molecules and representative units in the silica polymorphs has been taken as evidence that the atomic interactions comprising the structure of coesite are quite similar to those of chemically and structurally similar molecules.⁴⁻⁶

In an experimental determination of the bond critical point, bcp, properties for coesite,¹⁷ it was found that the properties display a relatively wide range of values despite the small $\sim 2\%$ range in the observed bond lengths. For example, the value of $\rho(r_c)$, its curvatures, $|\lambda_1|$ and $|\lambda_2|$, perpendicular to the bond path and the Laplacian, $\nabla^2 \rho(r_c)$, each vary by ~20% whereas the curvature of $\rho(r_c)$ parallel to the path, λ_3 , varies by only ~10%. The bcp properties were also found to be independent of the observed SiO bond lengths whereas the properties calculated for H₁₂Si₅O₁₆ moieties of the structure vary, as observed above, in a regular way with bond length.⁹ In a theoretical study,¹⁸ the coesite structure was geometry optimized at zero pressure and at several pressures up to 17.4 GPa and the bond critical point properties were determined. The nonequivalent SiO bond lengths and the OSiO and SiOSi angles of the structures were found to agree within $\sim 1\%$ of those observed up to pressures of 5 GPa. In agreement with the molecular orbital calculations, the SiO bond lengths were found to be inversely correlated with the value of $\rho(r_c)$, the curvatures of $\rho(r_c)$ and $\nabla^2 \rho(r_c)$. Although the bcp properties for the model structure agree with those observed¹⁷ to within 5-10%, on average, they show a smaller range of values. Further, the ellipticity⁸ of the bond was found to decrease with increasing SiOSi angle with the bond becoming circular in cross section^{7,13} at 180°, a property, as we shall see later, that is related to features in the observed $\Delta \rho$ and $-\nabla^2 \rho$ electron density distributions. As both the observed and calculated $\nabla^2 \rho(r_c)$ values for the SiO bonds in coesite^{17,18} are large, ~23 e Å⁻⁵, and as $|\lambda_1|/\lambda_2 \sim 0.18$, the bonds necessarily classify, according to the Bader and Essën rules,19 as closedshell ionic bonded interactions. However, Downs¹⁷ has argued that the bond is more intermediate in character given that its $\rho(r_{\rm c})$ value is substantially larger (~1.05 e Å⁻³) than that observed for the predominantly ionic CaO bond, ~ 0.15 e Å⁻³, in danburite,²⁰ CaB₂Si₂O₈.

Statement of Problem

It is apparent that the bcp properties calculated for both coesite and representative moieties display systematic and welldeveloped trends when plotted against R(SiO). Although the values obtained in these calculations agree fairly well with those observed, the experimental properties fail to correlate¹⁷ with R(SiO). It can be argued that this problem is related in part to the limited number of diffraction data used in the multipole refinement of the structure.¹⁷ The absence of the maxima in the $\Delta \rho$ maps in the lone-pair regions can accordingly be ascribed to the lack of high-angle data. Furthermore, the earlier refinements^{13,17} were incomplete given the intractability and bias of the radial functions used in the multipole modeling of the electron density distribution.^{21,22} As observed above, the absence of the trend between R(SiO) and the bond critical point properties can be arguably due to the small range of the observed bond lengths. In the case of the very high-pressure silica polymorph stishovite where the SiO bond lengths show twice the range of values as observed for coesite, the experimental bcp properties were observed²³ to correlate with R(SiO). It was also found that the properties of stishovite agree with those generated for a variety of geometry optimized hydroxyacid silicate molecules both qualitatively and quantitatively.^{23,24} Further, the evidence²³ indicates that the closed-shell nature of the bond increases with increasing R(SiO) and decreasing $\rho(r_c)$ and $\nabla^2 \rho(r_c)$.

To circumvent the problem of a limited data set, a relatively large set of single-crystal X-ray diffraction data was collected for this study and used to obtain a multipole representation of the experimental electron density distribution for coesite (1) to determine whether the features in $\Delta\rho$ and $-\nabla^2\rho$ maps in the bonding and lone-pair regions of the crystal conform with those generated by theory, (2) to explore the extent to which the bcp properties of the distribution agree with those generated by theoretical calculations, and (3) to relate the properties of the SiO bond to its elusive character⁷ and bond length variations.

Coesite is an ideal material for studying SiO bonded interactions. It is centrosymmetric, consisting of two nonequivalent SiO₄ silicate tetrahedra that share corners in forming a dense framework structure. It contains eight nonequivalent SiO bond lengths that range between 1.596 and 1.622 Å, twelve nonequivalent OSiO angles that range between 108.0° and 110.5° and five nonequivalent SiOSi angles that range between 136.7° and 180.0°. Although the bond lengths in coesite are restricted to a small range of values, R(SiO) correlates with the SiOSi angle, as observed above, with the shorter bonds involving wider angles, as predicted by theoretical calculations.^{7,18,25} It will also be of interest to compare the properties of $\rho(r_c)$ with those observed for stishovite.²³ Finally, it is anticipated that the study will not only advance our understanding of the SiO bonded interaction but also provide an experimental basis for understanding why hydrogen adopts the positions that it does in Hand Al-bearing coesite and stishovite crystals synthesized and formed at high temperature and pressures.^{10,11,26,27}

Experimental Procedure and Details

The coesite crystals used for this study,²⁵ synthesized from powdered amorphous anhydrous silica at 4.5 GPa and 650 °C, were kindly supplied by Dr. Charles T. Prewitt of the Carnegie Institute of Washington, D.C. One displaying sharp extinction under the polarizing microscope was selected and was found to be highly diffracting, yielding very sharp peaks with an average width of ~0.1°. Prior to data collection, the crystal was ground to a sphere ~100 μ m in diameter to minimize the absorption of the X-ray beam and to simplify the modeling of the absorption correction.

Single-crystal X-ray diffraction intensity data were recorded at 100 K with a Bruker SMART1000 diffractometer equipped with a CCD area detector, using graphite-monochromated Mo Kα($\lambda = 0.71073$ Å) radiation. More than 14 690 frames were collected between 0 and 120° 2θ (sin $\theta_{max}/\lambda = 1.21$ Å⁻¹), using the Bruker SMART software package.²⁸ Each frame was recorded as an ω scan of 0.15° with a 10 s run time exposure with the detector set at 0° and 30 s for the other detector positions. Short runs of 50 frames each were periodically recorded to monitor the stability of the X-ray beam. The CCD area detector entry was positioned in the experiment at a distance of 40 mm from the crystal to cover a section of ~60° in 2θ.

Upon completion of the data collection, the Bruker SAINT software was used to integrate the observed intensities. The starting dimensions of the box were $X = 1.1^{\circ}$, $Y = 1.1^{\circ}$, and $Z = 0.4^{\circ}$; however, the size of the box used to integrate the intensities was optimized and a narrow frame algorithm was adopted as a integration condition due to the sharpness of the peaks. Further, to monitor crystal displacements (none was detected), the orientation matrix was updated periodically every 303 frames; no symmetry constraints were imposed on the matrix. For all runs, the dimensions of the box converged to the optimized values. The Lp corrections were applied to the intensities using SAINT of the SMART CCD package.

A total of 18 071 intensities was observed and used to generate two F_0^2 data sets: one contained all of the 18 071 unmerged $F_0^{2^*}$ s (highest and lowest redundancy of 11.05 and 4.39, respectively) and the other contained only the nonequivalent intensities. The second set was generated by averaging the equivalent $F_0^{2^*}$ s for Laue point group type 2/m, using the program SORTAV.²⁹ Systematic absences were eliminated from the data set using the limiting diffraction conditions for space group type C2/c. In this process, a total of 4018 nonequivalent $F_0^{2^*}$ s was generated. The observed $F_0^{2^*}$ s for both data sets were corrected for absorption using the program SADABS.³⁰ A regression analysis completed for 6067 observed *d* spacing generated the following cell dimensions: a = 7.1325(1) Å, b = 12.3712(2) Å, c = 7.1763(1) Å, and $\beta = 120.364(1)^\circ$ with the esds given in the parentheses.

Multipole Analyses

Our first attempt at a multipole refinement, using the 4018 merged data, was based on a conventional multipole model. This included density-localized monopole radial functions, as well as single-exponential radial functions, $r^n \exp(-\alpha r)$, for higher multipoles up to and including the hexadecapole level on both Si and O. For Si, n = 4 for all higher multipoles and for O, n = 2, 2, 4, 4, for dipoles through hexadecapoles, respectively. Along with all multipoles, a κ scaling parameter was refined separately for the Si and O valence monopoles as well as a single radial exponent for all Si atoms and a separate exponent for all O atoms. The resulting model static deformation density maps (i.e., deconvoluted from thermal motion) were found to yield the expected maxima along each of the SiO vectors and in the nonbonding regions of the oxide anions. However, the maps were also found to display a spurious ring of maxima ~ 0.25 e Å⁻³ in height at distances of ~ 0.50 Å surrounding each Si atom. The cause of this feature was isolated to the unusually large value of κ obtained in the refinement of the Si valence monopole. Whereas $\kappa(O)$ was found to be quite sensible at 0.97, the κ (Si) refined to a value of 1.43, suggesting a very large contraction of the Si atom valence monopole.

A useful model study,²¹ undertaken for a number of diatomic molecules, demonstrates that monopole deformations, deduced from Hartree–Fock wave functions, can be fitted extremely well with κ -refined valence monopole functions. Typically, the κ values were found to be much less than 1.25 and close to 1.0.

Apropos to the present study of coesite, it was found²¹ that κ (Si) = 0.990 for SiH and 1.001 for SiO and κ (O) = 0.987 for OH and 0.971 for SiO. These results provide strong evidence that the value of κ (Si) = 1.43, obtained in the initial multipole refinement, is unrealistically large and most likely not a reflection of a real electronic effect. This suggests that the experimental data are lacking the information content necessary to determine a meaningful value for κ (Si). To explore one possible reason for this problem, a plot of $|\Delta F| = |F_0| - |F_c|$ against sin θ/λ was found to reveal a large number of discrepancies at relatively high sin θ/λ values. Imposing a 3σ cutoff on $|F_0|$ removed the majority of these discrepancies, but a subsequent multipole refinement against the data subject to this 3σ cutoff yielded no changes in the refined values of κ (Si) and κ (O). It was concluded that κ (Si) cannot be determined reliably from the experimental data set despite its large size.

To overcome this problem, a set of theoretical structure factors was calculated for coesite and subjected to the same refinement strategy. The CRYSTAL98 code,³¹ denoted here as C98, was used together with the atomic coordinates of the geometry optimized structure generated for coesite¹⁸ and the (9s5p)/[4s2p] contracted double- ζ contracted Gaussian type basis sets³² for O together with the (12s8p)/[6s4p] contracted double- ζ basis set³³ for Si. The basis sets for both Si and O were augmented with single d-type polarization functions with exponents of 0.85 au for O and 0.5 au for Si. To obtain convergence in the Hartree-Fock calculations, it was necessary to remove the diffuse p-type function on Si. From the resulting Hartree-Fock model electron density distribution, a complete set of structure factors was generated for coesite to a resolution of sin $\theta_{\text{max}}/\lambda$ = 1.21 Å⁻¹. A multipole modeling of these theoretical data is ideal for several reasons: (1) the scale factor is exactly known, (2) the data set is free from thermal motion, (3) no corrections for systematic effects (i.e., extinction, absorption, and anomalous dispersion) are required, and (4) there are no experimental errors. Despite the ideal set of structure factors, the refinement resulted in a *R* factor of 0.21%, suggesting that the multipole refinement remained deficient in its ability to model every aspect of the electron density distribution.

To see how well the chosen multipole model represents the actual electron density distribution, the model deformation electron density distribution resulting from the multipole fitting of this set of theoretical structure factors was compared critically with the deformation density calculated directly from the Hartree–Fock electron density distribution for the crystal. Although the maxima associated with the SiO bond vectors are well-reproduced, it was immediately apparent that the sharper maxima in the lone-pair regions (i.e., outside and inside the SiOSi angle) were very poorly fit. There are two possible causes for this deficiency: (1) the lack of flexibility and bias afforded by the single-exponent radial functions and (2) the limited resolution of the computed data set.

The effect of the resolution of the data was examined by generating sets of theoretical structure factors for given sets of sin $\theta_{\text{max}}/\lambda$ values and computing deformation electron density maps, $\Delta \rho^{\text{Fourier}}$, via Fourier summations $F_{\text{C98}}^{\text{Fourier}} - F_{\text{IAM}}$. Figure 1 illustrates the results of these calculations obtained using this approach for the Si2O2Si2 plane in coesite for structure factors calculated for the six following sin $\theta_{\text{max}}/\lambda$ values: 0.8, 0.9, 1.2, 1.5, 1.8, and 2.0 Å⁻¹. The figure makes it abundantly clear that the fine details of the sharper deformations around the oxide anions are not revealed even for the current experimental data set; with a resolution of sin $\theta_{\text{max}}/\lambda = 1.21$ Å⁻¹ (which is unusually high), the data effectively lacks this information. It



Figure 1. Deformation maps calculated for the Si2O2Si2 angle with amplitudes $F(hkl)_{C98} - F(hkl)_{IAM}$ with VALRAY³⁵ for sin θ_{max}/λ values of 0.8, 0.9, 1.2 (top row, left to right) and 1.5, 1.8, 2.0 Å⁻¹ (bottom row, left to right). $F(hkl)_{C98}$ are structure factors calculated with CRYSTAL98³¹ for the electron density distribution of the geometry optimized structure of coesite,¹⁸ and $F(hkl)_{IAM}$ are structure factors calculated for the procrystal representation of the electron density distribution. The contour line interval is 0.05 e Å⁻³ with positive contours solid, negative ones dotted, and the zero contour dashed.

is only with a resolution near 1.5 Å⁻¹ that these features become reasonably well-defined in shape and magnitude. It is noteworthy that at a resolution of 0.9 Å⁻¹, as in the case of the earlier data set,¹³ virtually no covalent lone-pair features were resolved near the oxide anions.

A comparison of the theoretical deformation Fourier map at the 1.21 $Å^{-1}$ resolution (Figure 1) with the static model of electron density derived from the standard multipole model and applied to the same theoretical data, suggested that it should be possible to fit the lone-pair type features with a sufficiently flexible multipole model. It has previously been observed repeatedly in recent electron density studies (cf. ref 22) that the usual single-exponential radial functions are inadequate for our purposes and a two-term function can provide a significant improvement in a refinement. Hirshfeld's original multipole refinement model, embodied in the FEXP code,34 includes twoterm radial functions for dipole and quadrupole multipoles and, although not commonly used these days, it has previously been shown to be essential to provide an adequate fit to the deformation density on the oxide anion in corundum.²¹ For these reasons, the present multipole refinement on coesite was augmented with extra radial functions added to the dipole and quadrupole sets on the oxide anion. These extra functions shared the same exponent as the first set but with n = 4 in both cases. A subsequent multipole refinement with the theoretical data resulted κ values of 0.91 on Si and 0.97 on O, resulting in good agreement with the values obtained for several diatomic molecules;²¹ exponents for the radial functions converged at values of $\alpha(Si) = 2.25 \text{ au}^{-1}$ and $\alpha(O) = 5.18 \text{ au}^{-1}$. In the final multipole refinement of the experimental data, the same additional dipole and quadrupole radial functions were added to the O atoms and a data cutoff of $F^2 > 3\sigma(F^2)$ was chosen. In addition, κ (Si) was fixed at 0.91 for both Si atoms and the radial exponents for the higher multipoles were fixed at the values obtained in the fit to the theoretical structure factors. Monopole populations were constrained to yield a neutral unit cell. As the extinction in the data was very small, it was modeled with an isotropic extinction correction (type 1, Gaussian mosaic). The refinement converged with $R_w = 2.00\%$, R(F) = 2.24%, and a goodness of fit of 1.33.

The maximum extinction encountered in the refinement was 1.8% for the F(040) reflection. The κ parameter for the O atoms converged to a value of $\kappa(O) = 0.992(2)$ and the atomic charges obtained by summing over the monopole populations on each atom type were found to differ little from neutrality, q(Si) = +0.16(6) and q(O) = -0.08(4). Positional and thermal param-

TABLE 1: Atomic Coordinates^a and VibrationalParameters^b

	Si1	Si2	01	O2	O3	O4	05
x	0.14001	0.50725	0	1/2	0.26453	0.31262	0.01843
у	0.10856	0.15794	0	0.11548	0.12428	0.10340	0.21178
Z	0.07220	0.54138	0	3/4	0.93864	0.32769	0.47672
$U_{11}, Å^2$	0.0027	0.0028	0.0048	0.0053	0.0044	0.0051	0.0048
$U_{22}, Å^2$	0.0024	0.0026	0.0034	0.0049	0.0059	0.0054	0.0031
$U_{33}, Å^2$	0.0026	0.0022	0.0053	0.0033	0.0051	0.0030	0.0060
$-U_{12}, Å^2$	0.0004	0.0002	0.0013	0	0.0008	0.0010	0.0005
$U_{13}, Å^2$	0.0013	0.0013	0.0022	0.0029	0.0032	0.0009	0.0029
$-U_{23}$, Å ²	0.0003	0.0001	0.0005	0	0.0003	0.0007	0.0003
$B_{\rm eq},{ m \AA}^2$	0.202	0.202	0.370	0.331	0.378	0.392	0.360

^{*a*} Given at the 0.00005 significance level. ^{*b*} Given at the at the 0.0005 Å² significance level.

TABLE 2: Bond Lengths (Å),^{*a*} Angles (deg),^{*b*} and Selected Distances (Å)

Si1O1	1.596	Si2O2	1.612	∠Si1O1Si1	180.0
Si1O3	1.614	Si2O3	1.615	∠Si2O2Si2	142.0
Si1O4	1.612	Si2O4	1.607	∠Si1O3Si2	144.2
Si1O5	1.622	Si2O5	1.620	∠Si1O4Si2	149.7
				∠Si1O5Si2	136.7
∠01Si1O3	110.5	∠O2Si2O3	109.7	Si1Si1	3.192
∠01Si1O4	109.2	∠O2Si2O4	109.4	Si2Si2	3.047
∠01Si105	109.8	∠02Si2O5	110.1	Si1Si2	3.074
∠03Si1O4	110.3	∠03Si2O4	108.8	Si1Si2	3.108
∠03Si105	108.0	∠03Si2O5	109.4	Si1Si2	3.013
∠04Si105	109.0	∠04Si2O5	109.5		
0103	2.638	0203	2.639		
0104	2.616	0204	2.626		
0105	2.632	0205	2.648		
0304	2.647	0304	2.622		
0305	2.619	0305	2.640		
0405	2.634	0405	2.634		

 a Given at the 0.001 Å significance level. b Given at the 0.1° significance level.

eters resulting from the multipole refinement are given in Table 1, and the nonequivalent bond lengths, angles, and selected distances are given in Table 2. The bcp properties for the multipole representation for the observed electron density distribution, calculated with VALRAY,³⁵ are given in Table 3. Static deformation density maps were generated and display maxima along each of the SiO vectors and in the lone-pair region of each oxide anion. However, unlike the earlier maps generated with a more limited data set, the spurious maxima about the Si atoms are absent. It is noteworthy that these maxima are displayed in SiOSi $\Delta \rho$ distributions published by earlier workers.³⁶

TABLE 3: Bond Critical Point Properties Experimental $F(hkl)_{obs}$ Multipole Model Representation^{*a*} of ρ

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bond	R(SiO), Å	$\rho(r_{\rm c})$, e Å ⁻³	$\lambda_{1,2}$, e Å ⁻⁵	λ_3 , e Å ⁻⁵	$\nabla^2 \rho(r_{\rm c})$, e Å ⁻⁵		
Si101	1.596(1)	1.02(1)	-7.8(2)	38.4(3)	22.7(3)		
Si2O2	1.612(1)	1.01(1)	-7.7(2)	36.0(4)	20.6(4)		
Si1O3	1.614(2)	1.04(1)	-7.8(2)	37.4(4)	21.9(6)		
Si2O3	1.616(1)	1.00(1)	-7.5(2)	37.7(5)	22.7(5)		
Si104	1.613(4)	1.00(2)	-7.3(1)	37.2(4)	22.6(6)		
Si2O4	1.607(4)	0.96(2)	-7.2(1)	36.2(4)	21.8(5)		
Si105	1.622(1)	0.96(2)	-7.8(2)	34.9(5)	19.4(5)		
Si2O5	1.620(1)	0.99(2)	-7.2(2)	35.3(5)	21.0(5)		
Theoretical $F(hkl)_{C98}$ Multipole Model Representation of ρ							
Si101	1.592	1.01	-7.8	38.6	23.0		
Si2O2	1.610	0.98	-7.4	35.8	21.1		
Si1O3	1.614	0.98	-7.3	35.1	20.4		
Si2O3	1.614	0.97	-7.3	35.1	20.5		
Si1O4	1.611	0.98	-7.4	35.1	20.4		
Si2O4	1.605	0.99	-7.4	36.5	21.6		
Si105	1.621	0.96	-7.2	34.2	19.8		
Si2O5	1.621	0.96	-7.2	34.2	19.9		
Theoretical ρ -Distribution for the Model Coesite Structure ¹⁸							
Si101	1.592	1.00	-6.7	38.8	25.4		
Si2O2	1.610	0.98	-6.4	36.4	23.5		
Si1O3	1.614	0.96	-6.3	35.7	23.2		
Si2O3	1.614	0.97	-6.3	35.7	23.2		
Si104	1.611	0.97	-6.2	36.0	23.5		
Si2O4	1.605	0.98	-6.4	37.0	24.1		
Si105	1.621	0.96	-6.2	34.9	22.5		
Si2O5	1.621	0.96	-6.1	34.8	22.5		

^{*a*} The esds are given in parentheses and refer to the digit quoted.



Figure 2. Drawing of the structure of coesite viewed down \sim [100] displaying the 99.999% probability thermal ellipsoid isosurfaces for the Si and O atoms. The smaller isosurfaces represent the thermal ellipsoids for Si, and the large ones represent those for O. [010] runs vertically and [001] runs horizontally in the drawing. The lines connecting adjacent atoms parallel the bond paths between Si and O.

The equivalent isotropic temperature factors, $B_{eq} = 8\pi^2 \langle \sigma^2 \rangle$ ($\langle \sigma^2 \rangle$ is the average mean square displacement³⁷), for the Si and O atoms determined at 100 K are smaller (Table 1), by a factor of ~2, than those observed in an earlier room-temperature measurement.¹³ However, the orientations of the thermal ellipsoids are in close agreement with those determined at room temperature.¹³ The largest difference is 10° with an average difference of 3°. As observed for the room-temperature data, the thermal ellipsoids are prolate uniaxial in shape (Figure 2) with the larger two root-mean-square amplitude displacements bisecting the SiOSi angles and the shorter ones oriented perpendicular to the bisector of the angles directed roughly in the directions of the SiO bond vectors. Also, the bond lengths and angles observed at 100 K are in excellent agreement with those generated in the first-principle calculations for a model structure of coesite.¹⁸ The observed SiO bond lengths are 0.0018 Å longer, on average, than those of the model structure, and the observed SiOSi angles are 0.3° wider, on average, than those of the model structure. In addition, the OSiO angles agree within 0.2°, on average, with those of the model structure. Given that the model structure was generated at absolute zero with no zero point vibration, its shorter bond lengths are unexpected, as thermal motion results in a decrease in the apparent bond length.

Deformation Density Distributions

For purposes of comparison, three different sets of $\Delta\rho$ maps were generated for each of the five nonequivalent SiOSi angles in coesite (Figure 3): (1) theoretical $\Delta\rho_{C98} = \rho_{C98} - \rho_{IAM}$ deformation maps displayed in column 1 of Figure 3 (ρ_{C98} is the electron density distribution calculated for the observed structure of coesite with C98³¹ and ρ_{IAM} is the relevant procrystal electron density distribution), (2) theoretical static deformation $\Delta\rho_{C98}^{\text{multipole}} = \rho_{C98}^{\text{multipole}} - \rho_{IAM}$ maps displayed in column 2 of Figure 3 (generated in a multipole refinements of $F(hkl)_{C98}$ where $F(hkl)_{C98}$ are the structure factors calculated from the ρ_{C98} electron density for the model structure¹⁸), and (3) observed static $\Delta\rho_{exp}^{\text{multipole}} = \rho_{exp}^{\text{multipole}} - \rho_{IAM}$ deformation maps displayed in column 3 of Figure 3 (where $\rho_{exp}^{\text{multipole}}$ was generated in a multipole refinement of F_{obs}).

Not only do the theoretical $\Delta \rho$ maps in Figure 3 display welldefined maxima along each of the SiO bond vectors and in the lone-pair regions, but the $\Delta \rho_{exp}^{multipole}$ ones do as well. It is clear that the maxima in the lone-pair regions owe their existence to the more extensive data set collected in this study. In addition, the theoretical $\Delta \rho_{C98}$ maps (Figure 3, column 1) are strikingly similar to those calculated earlier for the H₆Si₂O₇ molecule.¹³ The positions of the maxima for the bulk crystals are the same as those in the maps for the molecules, and the heights of the maxima are virtually the same as well. Also, low-lying bridges of electron density occur on the interior of each SiOSi angle as observed earlier.¹³ In each of the theoretical, and in several of the experimental maps, the maxima along the SiO bond vectors are displaced off the vectors toward the interior of the SiOSi angles, an effect that can be ascribed to repulsions between the localization of the electron density in the lone-pair and bondpair regions. Unlike the maps displayed in columns 2 and 3, the $\Delta \rho_{C98}$ maps show maxima adjacent to the oxide anions inside the SiOSi angle that sharpen with decreasing angle. The $\Delta \rho_{C98}^{\text{multipole}}$ maps (Figure 3, column 2) for coesite are topologi-cally similar to the $\Delta \rho_{exp}^{\text{multipole}}$ maps (Figure 3, column 3), but there are differences in the shapes and the heights of the maxima. Overall, despite the limited resolution of the data used to generate the experimental maps, the systematic errors, the bias introduced by the limited flexibility of the radial functions in the multipole refinements,^{21,22} and the defects in the multipole model itself, the agreement between the two sets of maps is considered to be reasonably good.

In an examination of the features in the lone-pair regions, $\Delta \rho_{\rm C98}^{\rm multipole}$ and $\Delta \rho_{\rm exp}^{\rm multipole}$ maps were constructed for the planes bisecting the SiOSi angles. As the maps gave little insight into the shape and spatial distribution of the lone-pair features, isosurface maps at a contour level of 0.35 e Å⁻³ were constructed for the five nonequivalent oxide anions (Figure 4). With the exception of isosurface maps for O1 and the experimental one for O2, each of the theoretical and experimental maps display a banana-shaped isosurface oriented roughly perpendicular to the plane of SiOSi angle centered at



Figure 3. Deformation maps calculated for the planes containing the five nonequivalent SiOSi angles in coesite. Rows: \angle Si1O1Si1 (row 1); \angle Si2O2Si2 (row 2); \angle Si1O3Si2 (row 3); \angle Si1O4Si2 (row 4); \angle Si1O5Si2 (row 5). Columns: column 1, theoretical $\Delta \rho_{C98} = \rho_{C98} - \rho_{IAM}$ deformation maps; column 2, theoretical static deformation $\Delta \rho_{C98}^{\text{multipole}} = \rho_{C98}^{\text{multipole}} - \rho_{IAM}$ maps; column 3, experimental static $\Delta \rho_{exp}^{\text{multipole}} = \rho_{exp}^{\text{multipole}} - \rho_{IAM}$ deformation maps. Contours are defined in the legend of Figure 1.

~0.35 Å from the oxygen atom. As expected, the banana-shaped isosurfaces displayed by the theoretical $\Delta\rho_{\rm C98}^{\rm multipole}$ maps are more uniform in size and less distorted than the experimental ones. The experimental lone-pair feature on O2, rather being

banana-shaped, consists of two symmetrically disposed teardropshaped isosurfaces. Upon an increase in the contour level, each banana-shaped isosurface was found to separate into two isosurfaces. The $\Delta \rho_{exp}^{multipole}$ and $\Delta \rho_{C98}^{multipole}$ isosurfaces about O1



Figure 4. Theoretical $\Delta \rho_{C98}^{\text{multipole}}$ (column 1) and experimental $\Delta \rho_{exp}^{\text{multipole}}$ (column 2) ($\Delta \rho$, isosurfaces displayed for the lone-pair regions of the five nonequivalent oxide anions in coesite O1, O2, O3, O4, and O5). The O1 oxide anion is involved in the straight S11O1Si1 angle whereas the remaining anions are involved in bent angles. The 0.35 e Å⁻³ isosurface is displayed.

are both ring torus-shaped, but again the experimental one is more distorted and tilted rather than being perpendicular to the straight SiOSi angle. Teardrop-shaped isosurfaces in $\Delta \rho_{exp}^{\text{multipole}}$ maps are displayed along the SiO bond vectors involving O2, O3, O4, and O5 with the features along the vectors merging with those in the lone-pair regions for O4 and O5. The $\Delta \rho_{C98}^{\text{multipole}}$ maps fail to show any isosurfaces along the SiO bond vectors inasmuch as the maxima along these vectors are all ~0.33 e Å⁻³ or less in height.

The lone-pair features displayed in Figure 4 are strikingly similar to those displayed by ELF and valence electron density isosurface maps calculated in an earlier study of coesite and the H₆Si₂O₇ molecule.¹¹ Both display banana-shaped isosurfaces in the lone-pair regions of the oxide anions involved in the bent angles.^{10,11} That study also shows that the shape and spatial extent of lone-pair features are both dependent on the size of the SiOSi angle. When the SiOSi angle is $\sim 140^{\circ}$, the ELF maps displayed well-developed banana-shaped isosurfaces oriented perpendicular to the planes of the SiOSi angles, typically located ~ 0.35 Å from the oxide anion. But, with increasing angle, the isosurfaces became progressively more elongated and completely surround the anion in a quasi-spherically shaped isosurface when the angle is 180°. Isosurface maps of the valence electron density distribution and $\Delta \rho$ for the H₆Si₂O₇ molecule likewise display banana-shaped isosurfaces in the lone-pair region when the angle is bent. However, when the angle is straight, they both display a ring torus-shaped isosurface¹¹ about the oxygen oriented perpendicular to the SiOSi angle, as observed in Figure 4. A similar feature was reported for the oxide anion involved in the relatively wide 168° SiOSi angle in beryl.³⁸ The decrease in the ellipticity of the SiO bond with increasing SiOSi angle described above with the bond becoming circular in cross section is consistent with the ring torus distribution of the $\Delta \rho$ and the valence electron density at 180°.

Laplacian Density Distributions

A mapping of the $-\nabla^2 \rho_{\text{C98}}^{\text{multipole}}$ distribution revealed a single (3, -3) critical point associated with each of the lone-pair regions involved with the anions (O2, O3, O4, and O5) involved in the bent SiOSi angles and four distributed at 90° intervals in a ring torus about the anion, O1, involved in the straight angle. In contrast, a mapping of $-\nabla^2 \rho_{exp}^{multipole}$ revealed a single critical point in the lone-pair region on O4 and O5 and two each on O1, O2, and O3. As observed by MacDougall³⁹ and Bader and MacDougall,⁴⁰ (3, -3) critical points in a $-\nabla^2 \rho$ distribution define regions where the electron density distribution is locally concentrated, regions that are ascribed to domains of bonding and nonbonding electrons. An examination of the $-\nabla^2 \rho$ maps for the SiOSi angle of the H₆Si₂O₇ molecule has revealed a belt-shaped isosurface, crescent-shaped in cross section, capping the oxide anion and enclosing a single (3, -3) critical point 0.36 Å from the apex of the SiOSi angle.⁴ The spatial distribution of the nonbonding domain for the molecule¹¹ was found to depend on the width of the angle with the isosurface increasing in its extent around the anion and merging as a ring torus about the anion as the angle is increased to 180°. For purposes of comparison, two sets of $-\nabla^2 \rho$ isosurface maps were generated at the 170 e Å⁻⁵ contour level for the $\rho_{C98}^{\text{multipole}}$ and $\rho_{exp}^{\text{multipole}}$ distributions (Figure 5). As found for the molecule, the $\nabla^2 \rho_{C98}^{\text{multipole}}$ isosurface maps display a belt-shaped isosurface centered at the apex of the angle and encircling O2, O3, O4, and O5 about halfway around each anion whereas a ring torusshaped isosurface encircles O1 (Figure 5). The $-\nabla^2 \rho_{exp}^{\text{multipole}}$ isosurface maps display similar features with the exception that O2 has two isosurfaces, as displayed by the $\Delta \rho_{exp}^{\text{multipole}}$ maps for the anion (Figure 4). Also, unlike the $-\nabla^2 \rho_{C98}^{\text{multipole}}$ maps, the lone-pair isosurfaces displayed by the $-\nabla^2 \rho_{exp}^{\text{multipole}}$ maps ex-tend into the bonding regions and merge in several cases with the maxima along the SiO bond vectors as observed for several $\Delta \rho_{\rm exp}^{\rm multipole}$ maps.

The (3, -3) local maxima of the lone-pair domains associated with O2, O3, O4, and O5 are systematically $\sim 10 \text{ e} \text{ Å}^{-5}$ greater in height than those on O1 for both the experimental and theoretical distributions (see Figure 5 legend). This evidence shows that the electron density is more locally concentrated in the lone-pair domains of the anions involved in the bent angles and less so in the domain of O1. Accordingly, hydrogen can be expected to preferentially dock in the vicinity of the four more nucleophilic O2, O3, O4, and O5 anions and to avoid less nucleophilic O1 in a H-bearing coesite crystal, as predicted by Gibbs et al.^{10,11} and established in a concurrent infrared study by Koch-Müller et al.²⁶ who found that hydrogen is bonded to four of the five nonequivalent oxide anions, forming a defect $v(OH)_4$ group (v is the vacancy created by a missing Si atom). The oxide anions comprising the $v(OH)_4$ group were established to be O2, O3, O4, and O5. Thus, H is observed to avoid O1 and preferentially bonds to anions with domains of greater locally concentrated electron density as predicted. In short, the $-\nabla^2 \rho_{\text{exp}}^{\text{multipole}}$ and $-\nabla^2 \rho_{\text{C98}}^{\text{multipole}}$ isosurface maps generated in



Figure 5. Theoretical $-\nabla^2 \rho_{C98}^{\text{multipole}}$ (column 1) and experimental $-\nabla^2 \rho_{exp}^{\text{multipole}}$ (column 2) isosurfaces displayed for the lone-pair regions of the five nonequivalent oxide anions in coesite, O1, O2, O3, O4 and O5. The 170 e Å⁻⁵ isosufaces are displayed. The heights of the (3, -3) maxima associated with the theoretical lone-pair domains on O1, O2, O3, O4, and O5 are 183, 191, 191, 189, and 192 e Å⁻⁵, respectively, whereas those associated with the experimental lone pairs are 190, 220, 209, 210, and 213 e Å⁻⁵, respectively.

this study provide an experimental and theoretical basis for the strategy used to determine the positions of hydrogen in H-bearing coesite, quartz, and stishovite.^{11,12}

Bond Critical Point Properties

The bond critical point properties determined for the $\rho_{exp}^{\text{multipole}}$ distribution are given in Table 3. Unlike the experimental properties determined earlier,¹⁷ they show a smaller range of values similar to those calculated for the H₁₂Si₅O₁₆ moieties of the coesite structure⁹ and the structure itself.¹⁸ The experimental values for λ_3 and $\nabla^2 \rho$ display a weak negative correlation with *R*(SiO) whereas $\rho(r_c)$ and $|\lambda_{1,2}| = 1/2|\lambda_1 + \lambda_2|$ are both independent of the bond length as found earlier.¹⁷ On the other hand, a well-developed correlation is displayed between the bonded radius of the oxide anion, $r_b(O)$, and R(SiO). In addition, properties were also generated for $\rho_{C98}^{\text{multipole}}$; these together with those generated for the model structure of coesite¹⁸ are also given in Table 3. Considering the small range of SiO bond

lengths and the inflexibility of the radial functions used to generate $\rho_{\text{exp}}^{\text{multipole}}$, the agreement between the theoretical and the experimental properties is considered to be good. It is noteworthy that in each of these cases the theoretical bond lengths correlate with $\rho(r_c)$, $|\lambda_{1,2}|$, λ_3 , and $\nabla^2 \rho(r_c)$, each increasing in value with decreasing R(SiO).

As observed earlier, stishovite²³ is the only other silica polymorph for which the bcp properties have been experimentally determined. The combined experimental properties for these two silica polymorphs are compared in Figure 6 with those calculated for a relatively large number of silicate crystals.^{4,12} The experimental R(SiO) vs $\rho(r_c)$ values for the two polymorphs fall, for the most part, within the scatter of the trend displayed by the silicate data set (Figure 6a). As such, the trend generated for the combined experimental data follows that calculated for the silicates with the shorter bonds involving the larger $\rho(r_c)$ values. The experimental R(SiO) vs $|\lambda_{1,2}|$ data set parallels that calculated, but it is systematically ~ 1 e Å⁻⁵ larger than that calculated (Figure 6b). In addition, the experimental R(SiO) vs λ_3 data set not only parallels but falls close to the silicate trend (Figure 6c). The increase in λ_3 with decreasing bond length reflects an increase in the force constant of the SiO bond, rendering the shorter bonds more resistant to change by compaction.⁸ The *R*(SiO) vs $\nabla^2 \rho(r_c)$ data set also parallels the silicate trend, but on average, they tend to be somewhat smaller overall (Figure 6d). The correlations between R(SiO) and r_{b} -(O) are not only well-developed for both coesite and stishovite, but they agree very well with that defined by the silicates (Figure 6e). Given the relatively wide range of bond lengths, ~ 0.25 Å, displayed for a given $\rho(r_c)$ value of 1.00 e Å⁻³ for the silicates (Figure 6a), perhaps it is not surprising that the bond lengths for coesite, with a range of 0.026 Å, fail to correlate with $\rho(r_c)$. On the other hand, given the small scatter of data for the linear R(SiO) vs $r_b(O)$ trend displayed by the silicates, it may not be surprising that the observed R(SiO) vs $r_b(O)$ correlation is welldeveloped. Overall, however, the agreement displayed in Figure 6 is evidence that computational chemistry and physics have both advanced to the stage where they do a reliable job in reproducing the electronic structure of the SiO bond. It also reflects very well on the quality of the current experimental data and the multipole model used in this study. Also, the good agreement between the experimental bcp properties and those calculated for the H₁₂Si₅O₁₆ moieties is further evidence that the experimental electron density distribution displayed by coesite is strikingly similar to that displayed by representative molecules.

As the observed SiO bond lengths decrease for the large silicate data set from 1.86 to 1.57 Å, $\nabla^2 \rho(r_c)$ increases in value from ~7 to ~27 e Å⁻⁵ with a concomitant increase in $\rho(r_c)$ from ~0.5 to ~1.1 e Å⁻³ (Figure 6). Also, the ratio $|\lambda_1|/\lambda_3$ decreases linearly from 0.22 to 0.17 for the change in bond length. As observed above, the large positive value for $\nabla^2 \rho(r_c)$ calculated for these bonds is typical of a closed-shell ionic interaction, particularly because $|\lambda_1|/\lambda_3$ is less than 0.25. However, the inherent nature of the electron density distributions of the Si and O atoms in the internuclear region of the interaction virtually guarantees that as *R*(SiO) decreases, λ_3 must necessarily increase in value,^{24,41} resulting in a concomitant increase in the value for $\nabla^2 \rho(r_c)$.

As observed by Bader,⁸ the formation of a (3, -1) critical point in the electron density distribution between a pair of bonded atoms such as Si and O indicates that the electron density is localized in the binding region between the nuclei with ρ reaching a local maximum value along the bond path. Further,



Figure 6. Observed SiO bond lengths, R(SiO), plotted against (a) $\rho(r_c)$, (b) $|\lambda_{1,2}| = 1/2|(\lambda_1 + \lambda_2)|$, (c) λ_3 , (d) $\nabla^2 \rho(r_c)$, and (e) $r_b(O)$, where $\rho(r_c)$ is the value of the electron density at the bcp, r_c , $|\lambda_1|$, and $|\lambda_2|$ are the curvatures of $\rho(r_c)$ measured perpendicular to the bond path, λ_3 is the curvature of $\rho(r_c)$ measured parallel to the bond path, and $r_b(O)$ is the bonded radius of the oxide anion bonded to Si. The silicate crystal bcp properties⁴ together with those for other silicates¹² are plotted as open squares, the coesite experimental bcp properties are plotted as solid triangles, and the stishovite experimental bcp properties²³ are plotted as solid squares.

when $\nabla^2 \rho(r_c)$ is negative, the electron density is locally concentrated at the bcp, which in turn is asserted to exert a net attractive force on the nuclei of the bonded atoms, all other things being equal, the larger the magnitude of $-\nabla^2 \rho(r_c)$, the greater the force and the shorter the bond length.⁸ However, as observed above, the separation between Si and O decreases as $\nabla^2 \rho(r_c)$ increases in value (Figure 6d). As $\nabla^2 \rho(r_c)$ is positive, the electron density is locally depleted at the r_c and in its immediate vicinity,⁴¹ indicating a reduction of the net attractive force between Si and O. Under these conditions, the SiO bond may be expected to lengthen as the electron density is progressively locally depleted in the binding region.⁸ However, concomitant with the increase of $\nabla^2 \rho(r_c)$, electron density is localized in the binding region between Si and O as the value of $\rho(r_c)$ increases in a regular way (Figure 6a,d). This evidence suggests that it is the value of $\rho(r_c)$ that plays the dominant role in governing the length of the SiO bond, not the local depletion of $\rho(r_c)$ in the binding region. It also suggests that $\rho(r_c)$ can be used as a measure of bond type, the greater its value, the more covalent a bonded interaction.^{4,24} Indeed, a plot of the average value of $\rho(r_c)$, $\langle \rho(r_c) \rangle$ for a given MO bond vs the spectroscopic electronegativity, χ_{spec} , for first and second row M metal atoms⁴² bonded to an oxide anion shows that $\langle \rho(r_c) \rangle$ increases in a regular way with χ_{spec} .⁴ If traditional arguments hold between electronegativity and bond type, then the character of a bonded interaction can be directly related to $\langle \rho(r_c) \rangle$: the greater its value, the more covalent the bonded interaction.

J J. Phys. Chem. B

In the case of the SiO bonded interactions in coesite, the observed $\langle \rho(r_c) \rangle$ value, 1.0 e Å⁻³, indicates that the bond is more covalent, for example, than KO, NaO, LiO, CaO, MgO, BeO, and AlO bonds, given that these interactions display smaller $\langle \rho(r_c) \rangle$ values⁴ that range between 0.1 and 0.5 e Å⁻³. On the other hand, the bond is indicated to be more ionic than PO, SO, and CO bonded interactions given that these bonds display larger $\langle \rho(r_c) \rangle$ values⁴ that range between 1.2 and 2.5 e Å⁻³. As observed above¹⁷ and as concluded more than 60 years ago,⁴³ these results suggest that the SiO bond is intermediate in character between these two sets of bonded interactions rather than qualifying as a closed-shell ionic interaction,^{8,19} consisting of nearly fully charged and spherical Si⁴⁺ and O²⁻ ions.⁴⁴

Summary and Comments on Hydrogen Positions in Stishovite

The observed $\Delta \rho(r_c)$ and $-\nabla^2 \rho(r_c)$ maps reported in this study display a localization and a local concentration of electron density in both the bonding and nonbonding regions of coesite, compelling evidence that the SiO bonded interaction is intermediate in character between closed-shell ionic and shared covalent.^{14,15} In addition, the preference of H for the oxide anions with well-developed lone pairs is further evidence that the anions involved in bent angles are not spherical like an O²⁻ anion but possess lone-pair features that are typical of covalent interactions. On the basis of electronegativity considerations, Kirfel et al.²³ have concluded that the SiO bond in stishovite is somewhat more ionic than a bond of intermediate character for silica polymorphs such as coesite and quartz. It is noteworthy that static deformation maps for stishovite show well-defined but smaller maxima along the SiO bonds and in the lone-pair region of the oxygen atom.^{23,45,46} Like coesite, the maximum in the lone-pair region has been shown to be a favorable site for docking H in H-bearing stishovite.^{10–12} The location of this site has been substantiated by first-principle calculations for H and Al doped stishovite model structures,⁴⁷ where the OH vector was found to be perpendicular to [001], as observed in a study of the infared spectra.²⁷ Clearly, the presence of the bonded and nonbonded features displayed in the observed electron density distribution indicates that the SiO bond in stishovite likewise has covalent character²³ but to a lesser extent than that for silica polymorphs with four-coordinate Si. On the other hand, arguments based on the bond critical point properties for the bonded interactions in both coesite and stishovite, and in particular the large values for $-\nabla^2 \rho(r_c)$ displayed for coesite, indicate that the bond is closed-shell ionic,¹⁹ a conclusion that is difficult to accept for a second row atom like Si given the bonding and nonbonding features displayed in the ELF, $\Delta \rho$, and $\nabla^2 \rho$ maps for SiO bonded interactions.

Finally, given the problems encountered in collecting and modeling the experimental data, it appears that the theoretical electron density distribution generated for coesite is more accurate and meaningful than that determined with the experimental data. The good agreement between the observed bond lengths and angles⁴ and the bond critical point properties²⁴ and those calculated for representative moieties⁹ lend support to the argument that the SiO bonded interactions in coesite behave as if short ranged and molecular in nature⁵ rather than long ranged as in an ionic crystal consisting of nearly fully charged Si⁴⁺ and O²⁻ ions.^{14,44}

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